

1) Figure 12-3(c)

$$v = \frac{ds}{dt}$$

$$u = (4t - 3t^2)$$

$$(4t - 3t^2) dt = ds$$

$$\int_{t_1}^{t_2} (4t - 3t^2) dt$$

$$= \int_{s_1}^{s_2} ds$$

$$\left[4 \times \frac{t}{2} - 3 \times \frac{t^3}{3} \right]_{t_1}^{t_2} = [s]_{s_1}^{s_2}$$

$$[2 \times t^2 - t^3]_{t_1}^{t_2} = s_2 - 0$$

$$s_2 = [2 \times 4^2 - 4^3] + 0$$

$$s_2 = -32 \text{ m}$$

2) Figure 12-4

$$v = 0.5t^3 - 8t$$

$$a = dv/dt$$

$$a = 1.5t^2 - 8$$

$$t = 2$$

$$a = \underline{\underline{-2 \text{ m/s}^2}}$$

3) Fig 12-7

$$a = (4t^2 - 2) \text{ m/s}^2$$

$$v = \int (4t^2 - 2) dt$$

$$v = \left[\frac{4}{3} t^3 - 2t - C \right]$$

$$s = \int \left(\frac{4}{3} t^3 - 2t + C_1 \right) dt$$

$$s = \frac{1}{3} t^4 - \frac{2}{2} t^2 + C_1 t + C_2$$

$$\text{at } t = 0, s = -2 = C_2$$

$$\text{at } t = 2, s = -20, C_1 = -9.70$$

$$\text{at } t = 4$$

$$s(4) = \frac{1}{3} (4)^4 - (4)^2 + (-9.70)(4) +$$

$$(-2)$$

$$= 38.7 \text{ m}$$

4) Fig 12-8

$$v = (20 - 0.03s^2) \text{ m/s}$$

$$\frac{ds}{dt} = \frac{dv}{ds} \text{ and } dt = \frac{dv}{a}$$

$$\frac{ds}{v} = \frac{dv}{a}$$

$$a = \frac{dv}{ds}$$

$$dv = 0.05s \times 2 ds$$
$$= 0.1s ds$$

$$a = (20 - 0.03s^2) \cdot (-0.15) ds$$

$$a = -2s + 0.005s^3$$

$$a(s=15) = -2 \times 15 + 0.005 \times$$
$$15^3$$

$$a = -13.125 \text{ m/s}^2$$