

HONGKONG POLYTECHNIC UNIVERSITY
 MECHANICAL ENGINEERING
 ENA 234

① for figure 12.3 (1)

$$v = (4t - 3t^2) \text{ m/s}$$

$$s = \int v dt$$

$$s = \int (4t - 3t^2) dt = 2t^2 - t^3$$

$$\text{When } t = 1$$

$$s = 2(1)^2 - (1)^3$$

$$= 3 - 1 = 2$$

$$s = 2 \text{ m}$$

$$p = \frac{1}{3}t^3 - p/t + c$$

$$\text{When } t = 0, p = 2$$

$$2 = \frac{1}{3}(0)^3 - \frac{p}{0} + c$$

$$c = 2$$

$$\text{When } t = 2, p = 20, c = 2$$

$$20 = \frac{1}{3}(2)^3 - \frac{p}{2} + 2$$

$$20 = 0.9 + \frac{p}{2}$$

$$c = -1.9$$

$$p = \frac{1}{3}t^3 - t^2 - 1.9t + 2$$

$$\text{When } t = 4$$

$$p = \frac{1}{3}(4)^3 - 4^2 - (1.9 \times 4) + 2$$

$$p = 28.9 \text{ m/s}$$

② for figure 12.4 (2)

$$v = (0.5t^3 - 4t^2) \text{ m/s}$$

$$a = dv/dt$$

$$\frac{dv}{dt} = 3(0.5t^2 - 4t)$$

$$= 1.5t^2 - 8$$

$$a = dv/dt \text{ at } t = 2$$

$$= 1.5(2)^2 - 8$$

$$= 6 - 8 = -2 \text{ m/s}^2$$

③ for figure 12.6 (4)

$$v = (20 - 0.5s) \text{ m/s}$$

$$a = \frac{dv}{dt} \text{ and } dv = \frac{dv}{ds} ds$$

$$a = \frac{dv}{dt} \cdot \frac{dt}{ds} = \frac{dv}{ds} \cdot \frac{ds}{dt}$$

$$\frac{dv}{ds} = -0.5, \frac{ds}{dt} = (20 - 0.5s^2)$$

$$a = (-0.5)(20 - 0.5s^2)$$

$$\text{When } s = 5$$

$$a = (-0.5 \times 5)(20 - 0.5(5)^2)$$

$$a = -15 \cdot 125 \text{ m/s}^2$$

④ for figure 12.7 (3)

$$a = (4t^2 - 2) \text{ m/s}^2$$

$$v = \int \frac{4t^2}{3} - 2t + c$$

$$s = \int v dt$$

$$= \int \frac{4t^3}{3} - 2t + c$$

$$= \frac{4t^4}{12} - \frac{2t^2}{2} + ct$$

$$12$$