

1) $x^{1/2} \ln x$

$\int x^{1/2} \ln x$

$u = x^{1/2} \quad du = \frac{1}{2} x^{-1/2} dx$

$\frac{du}{dx} = \frac{1}{2} x^{-1/2}$

$\int v du + \int u dv$

$\ln x \int \frac{2x^{1/2}}{2x} + x^{1/2} \int \frac{dx}{2x}$

$\ln x \left[\frac{2x^{3/2}}{3/2} \right] + x^{1/2} \left[\frac{1}{x} \right] + C$

$\frac{2 \ln x}{3} \cdot 2x^{3/2} + x^{1/2} + C$

$\frac{2}{3} x^{3/2} \ln x + \sqrt{x} + C$

~~1/2~~ $2 \cos 6t \cos 4t$

$A=6t \quad B=4t$

$\cos A \cos B = \frac{1}{2} [\cos(A+B) + \cos(A-B)]$

$\frac{1}{2} [\cos(6t+4t) + \cos(6t-4t)]$

$\frac{1}{2} [\cos 10t + \cos 2t]$

$\int 2 \cos 6t \cos 4t = \frac{1}{2} \int 2 \cos 10t \cos 2t$

$= \frac{1}{2} \left[\frac{\sin 10t}{10} - \frac{\sin 8t}{8} \right]$

$= \frac{\sin 10t}{20} - \frac{\sin 8t}{16} + C$

2) $\int \sin^5 \cos^4 x$

$u = \cos x$

$du = -\sin x \Rightarrow dx = \frac{du}{-\sin x}$

$\int \cos^4 x \sin^5 x dx$

$\int u^4 \sin^4 x \cdot \frac{-du}{\sin x}$

$= \int u^4 \sin^3 x \cdot (-du)$

$= - \int u^4 \sin^2 x \cdot du$

$\sin 2x + \cos^2 x = 1$

$\sin^2 x = 1 - \cos^2 x$

$= \int \sin^2 x \cos^4 x \cdot (-du)$

~~$\int \sin^2 x \cos^4 x$~~

$= \int (1 - \cos^2 x) u^4 du$

$= \int (1 - u^2) u^4 du$

$= \int (u^4 + u^6) du$

$= \left[\frac{u^{4+1}}{4+1} - \frac{u^{6+1}}{6+1} \right] + C$

$= \frac{u^5}{5} - \frac{u^7}{7} + C$

$\frac{(\cos x)^5}{5} - \frac{(\cos x)^7}{7} + C$