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Questions & Answers

Integrate the following with respect to their variables.

(1) $x^{1/2} \ln x$

Solu. : let $u = \ln x$ | $\frac{du}{dx} = x^{-1/2}$

∴ using the formula $\int u dv = uv - \int v du$

let $\frac{du}{dx} \times \frac{1}{x} = \frac{du}{x} = \frac{dx}{x}$ | $\boxed{du = \frac{dx}{x}}$

then $\int dv = \frac{2x^{3/2}}{3}$ ∴ $\boxed{v = \frac{2x^{3/2}}{3}}$

$\int x^{1/2} \ln x = \ln x \cdot \frac{2x^{3/2}}{3} - \int \frac{2x^{3/2}}{3} \cdot \frac{1}{x} dx$ | $u = \ln x$ $v = \frac{2x^{3/2}}{3}$ $du = x^{-1/2}$ $dv = \frac{dx}{x}$
 $= \frac{2x^{3/2} \ln x}{3} - \int \frac{2x^{1/2}}{3} dx = \frac{2x^{1/2+1}}{3(1/2+1)} = \frac{2x^{3/2}}{3(3/2)} = \frac{2x^{3/2}}{9/2} = \frac{4x^{3/2}}{9}$

∴ $\int x^{1/2} \ln x dx = \frac{2x^{3/2}}{3} - \frac{4x^{3/2}}{9} + C$

(2)

$\int 2 \cos 6t \cos t$ Solu

$= 2 \int \cos 6t \cos t = \frac{1}{2} [\cos(6t+t) + \cos(6t-t)]$

$= \frac{1}{2} \cos 7t + \cos 5t$

$2 \times \frac{1}{2} \int \cos 7t + \cos 5t$
 $= \left[\frac{\sin 7t}{7} + \frac{\sin 5t}{5} \right] + C$

∴ $\frac{\sin 7t}{7} + \frac{\sin 5t}{5} + C$

(3)

$$\sin^3 x \cos^4 x \, dx$$

Solu

$$u = \cos x \quad \therefore \frac{du}{dx} = -\sin x \Rightarrow dx = \frac{-du}{\sin x}$$

$$\sin^2 x + \cos^2 x = 1$$

$$\sin^2 x = 1 - \cos^2 x$$

$$= \int \sin x \cdot \sin^2 x \cdot \underbrace{u^4 dx}_{\sin x} - du$$

$$= \int \sin^3 x \cdot u^4 dx$$

$$= - \int \sin^2 x \cdot u^4 du$$

$$= - \int (1 - \cos^2 x) \cdot u^4 du$$

$$= - \int (1 - u^2) u^4 du$$

$$= \int (u^2 - 1) u^4 du$$

$$= \int (u^6 - u^4) du$$

$$= \frac{u^7}{7} - \frac{u^5}{5} + C$$

$$= \frac{(\cos x)^7}{7} - \frac{(\cos x)^5}{5} + C$$