# ASSIGNMENT III 

BY

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SUBMITTED TO

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IN PARTIAL FUFILMENT OF THE REQUIREMENT FOR THE AWARD OF THE DEGREE OF BACHELOR OF ENGINEERING (B.ENG) DEGREE IN CIVIL ENGINEERING
1.

The following non-linear speed-density relationship is assumed for a highway link:

$$
u=0.001(k-250)^{2}-1.4
$$

Where;
u has units of $\mathrm{km} / \mathrm{h}$
k has units of vehicles per km .
Estimate the free-flow speed, the jam density, the speed and density at maximum flow and the lane capacity of the link in question.

## Solution

Free-flow speed is speed at zero density
therefore, $\mathrm{k}=0$

$$
\begin{aligned}
u & =0.001(250)^{2}-1.4 \\
& =61.1 \mathrm{~km} \mathrm{~h}^{-1}
\end{aligned}
$$

Jam density is density at zero speed, therefore putting $u=0$
$0=0.001(k-250)^{2}-1.4=61.1$
$0=0.001\left(k^{2}-500 k+62500\right)^{2}-1.4$
$0.001 k^{2}-0.5 k+62.5-1.4=0$
$0.001 k^{2}-0.5 k+61.1=0$
Solving the quadratic equation:
$\mathrm{K}=287$ or $212 \mathrm{veh} / \mathrm{km}$ ( $287 \mathrm{veh} / \mathrm{km}$ chosen)
$q=u k$
therefore,
$q=\left(0.001 k^{2}-0.5 k+61.1\right) k$
$q=0.001 k^{3}-0.5 k^{2}+61.1 k$
At $\max \mathrm{q}, \frac{d q}{d k}=0$, therefore,
$0.003 k^{2}-k+61.1=0$

Solving this quadratic equation
$k_{\text {qmax }}=252.75$ or 80.58 veh $/ \mathrm{km}($ chosen $80.58 \mathrm{veh} / \mathrm{km})$
If $\mathrm{k}=80.58 \mathrm{veh} / \mathrm{km}$ we can solve for u as follows
$u_{\text {qax }}=0.001(80.58-250)^{2}-1.4=27.30 \mathrm{~km} \mathrm{~h}^{-1}$

Therefore,

$$
\begin{aligned}
q_{\max } & =80.58 \times 27.30 \\
& =2199.83 \text { veh }^{-1}
\end{aligned}
$$

2. 

The following flow-density relationship is assumed for a highway link: $q+60 u(\ln u)=250 u$
Estimate the free-flow speed, the speed at maximum flow, the maximum flow on the link in question and density and maximum flow
Solution
$\mathrm{q}+60 \mathrm{u}(\ln \mathrm{u})=250 \mathrm{u}$
jam density is density at zero, therefore $u=0$
$q+60\left(\ln u^{2}\right)=250 u$
$q+60 u^{2}=e^{250 u}$
$q+60(0)^{2}=e^{250(0)}$
$q=1$
At $\max q=\frac{d q}{d u}=0$
$q+60$ Inu $^{2}=250 u$
$q=250 u-60$ In $^{2}$

$$
\begin{aligned}
& \frac{d q}{d u}=250-60\left(\frac{2}{u}\right) \\
& 250-\frac{120}{u}=0 \\
& U_{\max }=\frac{120}{250} \\
& U_{\max }=0.48 \mathrm{~km} \mathrm{~h}^{-1} \\
& q=u k \\
& 1=0.48 \mathrm{~km} h^{-1} \\
& k=\frac{1}{0.48}=2 \mathrm{veh} / \mathrm{km}
\end{aligned}
$$

3. 

At a given highway location, assuming that vehicle arrivals are Poisson distributed, vehicles are counted in intervals of 30 seconds. 100 such counts are taken and it is noted that no vehicle arrives in 15 of these 100 intervals
(a) In how many of these 100 intervals will 3 cars arrive?
(b) Estimate the percentage of time that headways will be 6 seconds or greater
(c) Estimate the percentage of time that headways will be less than 4 seconds

Solution
a) $t=30 \mathrm{~s}$

$$
\begin{aligned}
& p(0)=\frac{15}{100}=0.15 \\
& p(n)=\frac{(q t)^{n} e^{-q t}}{n!} \\
& p(0)=\frac{(q t)^{0} e^{-q t}}{0!}=0.15
\end{aligned}
$$

$e^{-q t}=0.15$
$-q t=\operatorname{In}(0.15)=-1.89712$
$q=1.89712+30=0.0632 v e h / s$
Therefore,
$p(3)=\frac{(0.0632 \times 30)^{3} e^{-(0.0632 \times 30)}}{3!}$
$=\frac{(1.897)^{3} e^{-(1.897)}=0.171}{6}$
There is a $17.1 \%$ chance that 3 vehicles will arrive within any one interval.
Therefore, over the 100 counts taken, assuming that traffic is Poisson distributed, 3 cars will arrive in just greater than 17 of these:
b) $P($ headway $\geq 6)=e^{-(0.0632 \times 6)}$
$=0.6840 r 68.4 \%$ of the time
c) $P($ headway $\geq 4)=e^{-(0.0632 \times 6)}=0.777$ or $77.7 \%$ of the time

Therefore,
$P($ headway $\geq 4)=1-P($ headway $\geq 4)$
$=1-0.777$
$=0.223$ or $22.3 \%$ of the time

