

multiply through

$$\frac{x^4 - 2x^3 + 2x^3 - 4x^2 + x^2 - 2x - \frac{1}{2}}{2x^5 - x^4} \times (x-3)$$

$$= \frac{x^4 - 2x^3 + 2x^3 - 4x^2 + x^2 - 2x - \frac{1}{2}}{(2x^5 - x^4) \times (x-3)}$$

using elimination method

$$\frac{x^4 - 4x^2 + x^2 - 2x - \frac{1}{2}}{(2x^5 - x^4) \times (x-3)}$$

collect like terms

$$\frac{x^4 - 3x^2 - 2x - \frac{1}{2}}{(2x^5 - x^4) \times (x-3)}$$

$$\frac{x^4 - 3x^2 - 2x - \frac{1}{2}}{2x^6 - 6x^5 - x^5 + 3x^4}$$

rewriting

$$\frac{2x^4 - 6x^2 - 4x - 1}{2x^6 - 6x^5 - x^5 + 3x^4}$$

collected like term

$$\frac{2x^4 - 6x^2 - 4x - 1}{2x^6 - 7x^5 + 3x^4}$$

Simplify

$$\frac{(2x^4 - 6x^2 - 4x - 1) \times 3}{2(2x^6 - 7x^5 + 3x^4)}$$

multiply through by 3

$$\frac{6x^4 - 18x^2 - 12x - 3}{2(2x^6 - 7x^5 + 3x^4)}$$

multiply by 2

$$\frac{6x^4 - 18x^2 - 12x - 3}{4x^6 - 14x^5 + 6x^4}$$

$$y = \frac{6x^4 - 18x^2 - 12x - 3}{4x^6 - 14x^5 + 6x^4}$$

2 $y = \frac{[3e^k \sin 2k]}{k^{5/2}}$

finding the derivative of the function

$$y = \frac{d}{dx} \left(\frac{3e^k \sin 2k}{k^{5/2}} \right)$$

since $\frac{d}{dx} \left(\frac{f}{g} \right) = \frac{\frac{d}{dx} (f) \times g - f \times \frac{d}{dx} (g)}{g^2}$

$$\therefore y = \frac{\frac{d}{dx} (3e^k \sin (2k)) \times k^{5/2} - 3e^k \sin (2k) \times \frac{d}{dx} (k^{5/2})}{(k^{5/2})^2}$$

derivative of the product

$$y = \frac{(3e^k \sin (2k)) \times 3e^k \times \cos (2k) \times 2 \times k^{5/2} - 3e^k \sin k \times \frac{d}{dx} (k^{5/2})}{(k^{5/2})^2}$$

$$\therefore y = \frac{(6k^2 \sqrt{x} e^k \sin (2k)) + 12k^2 \sqrt{x} e^k \times \cos (2k) - 15 \sqrt{x} e^k \times \sin (2k) \times k}{2k^5}$$

Integration

1 $4 \sec^2 (3m+1)$

in exponential form

$$2^2 \times \sec (3m+1)^2$$

multiply through by bases

$$= (2 \sec (3m+1))^2$$

2 $2t (3t-1)^{1/2}$

using $a^{m/n} = \sqrt[n]{a^m}$

$$= 2t \sqrt{3t^2-1}$$

3 $\frac{2x}{(4x^2-1)^{1/2}}$

since any number raised to the power of 1 = the number

$$\therefore \frac{2x}{\frac{4x^2-1}{2}}$$

$$= \frac{2x}{4x^2-1}$$

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