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MATRIC NUMBER: 19/MHS01/132

DEPARTMENT: MEDICINE AND SURGERY

COURSE: MAT 104

ASSIGNMENT: Integrate

D $\int \frac{11-3x}{(x+3)(x-1)} dx$

SOLUTION

$$\frac{11-3x}{(x+3)(x-1)} = \frac{A}{x+3} + \frac{B}{x-1}$$
$$\frac{11-3x}{(x+3)(x-1)} = \frac{A(x-1) + B(x+3)}{(x+3)(x-1)}$$
$$11-3x = A(x-1) + B(x+3)$$

$f(1) \Rightarrow 11-3(1) = B(1+3)$

$$8 = 4B$$
$$B = \frac{8}{4}$$
$$B = 2$$

$f(-3) \Rightarrow 11-3(-3) = A(-3-1)$

$$20 = A(-4)$$
$$A = \frac{20}{-4}$$
$$A = -5$$

Substitute the value of A and B in the equation.

$$\frac{11-3x}{(x+3)(x-1)} = \frac{-5}{x+3} + \frac{2}{x-1}$$
$$\int \frac{11-3x}{(x+3)(x-1)} dx = \int \frac{-5}{x+3} dx + \int \frac{2}{x-1} dx$$

let $u = x+3$

$$\frac{du}{dx} = 1$$
$$dx = \frac{du}{1}$$
$$\int \frac{-5}{x+3} dx = \int \frac{-5 \cdot du}{u} = -5 \int \frac{1}{u} du$$
$$= -5 \ln u = -5 \ln(x+3)$$

let $u = x-1$

$$\frac{du}{dx} = 1$$
$$dx = \frac{du}{1}$$
$$\int \frac{2}{x-1} dx = \int \frac{2 \cdot du}{u} = 2 \int \frac{1}{u} du$$

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1.

$$= 2 \ln 4 = 2 \ln(x-1)$$

$$\therefore \frac{11-3x}{(x+3)(x-1)} = -5 \ln(x+3) + 2 \ln(x-1) \\ = -5 \ln(x+3) + 2 \ln(x-1) + C$$

2) Integrate $\frac{4x-16}{(x+3)(x+1)}$

SOLUTION

$$\frac{4x-16}{(x+3)(x+1)} = \frac{A}{x+3} + \frac{B}{x+1}$$

$$\frac{4x+16}{(x+3)(x+1)} = \frac{A(x+1) + B(x+3)}{(x+3)(x+1)}$$

$$4x+16 = A(x+1) + B(x+3)$$

$$f(-1) \Rightarrow 4(-1)+16 = B(-1+3)$$

$$12 = 2B$$

$$B = 12/2$$

$$B = 6$$

$$f(-3) \Rightarrow 4(-3)+16 = A(-3+1)$$

$$4 = (-2)A$$

$$A = 4/-2$$

$$A = -2$$

Substitute the values for A and B

$$\frac{4x-16}{(x-3)(x+1)} = \frac{-2}{x-3} + \frac{6}{x+1}$$

$$\int \frac{4x-16}{(x-3)(x+1)} dx = \int \frac{-2}{x-3} dx + \int \frac{6}{x+1} dx$$

$$\text{let } u = x-3$$

$$dy/dx = 1$$

$$dx = dy$$

$$\int \frac{-2}{x-3} dx = \int \frac{-2}{u} dy = -2 \int \frac{1}{u} dy$$

$$= -2 \ln u$$

$$= -2 \ln(x-3)$$

$$\text{let } u = x+1$$

$$dy/dx = 1$$

$$dx = dy$$

$$\int \frac{6}{x+1} dx = \int \frac{6}{u} \cdot \frac{du}{1} = 6 \int \frac{1}{u} du$$

$$= 6 \ln u$$

$$= 6 \ln(x+1)$$

$$\therefore \frac{x-16}{(x-3)(x+1)} = -2 \ln(x-3) + 6 \ln(x+1)$$

$$= -2 \ln(x-3) + 6 \ln(x+1) + C$$

$$3) \frac{2x^2 - 9x - 35}{(x+1)(x-2)(x+3)} = \frac{A}{x-1} + \frac{B}{x-2} + \frac{C}{x+3}$$

SOLUTION

$$\frac{2x^2 - 9x - 35}{(x+1)(x-2)(x+3)} = \frac{A}{x-1} + \frac{B}{x-2} + \frac{C}{x+3}$$

$$\frac{2x^2 - 9x - 35}{(x+1)(x-2)(x+3)} = \frac{A(x-2)(x+3) + B(x-1)(x+3) + C(x-1)(x-2)}{(x+1)(x-2)(x+3)}$$

$$2x^2 - 9x - 35 = A(x-2)(x+3) + B(x-1)(x+3) + C(x-1)(x-2)$$

$$f(2) \Rightarrow 2(2)^2 - 9(2) - 35 = B(2+1)(2+3)$$

$$-45 = 15B$$

$$B = \frac{-45}{15}$$

$$B = -3$$

$$f(-1) \Rightarrow 2(-1)^2 - 9(-1) - 35 = A(-1-2)(-1+3)$$

$$-24 = 6A$$

$$A = \frac{-24}{6}$$

$$A = -4$$

$$f(-3) \Rightarrow 2(-3)^2 - 9(-3) - 35 = C(-3+1)(-3-2)$$

$$10 = 10C$$

$$C = \frac{10}{10}$$

$$C = 1$$

Put in the values of A, B and C

$$\frac{2x^2 - 9x - 35}{(x+1)(x-2)(x+3)} = \frac{-4}{x+1} + \frac{-3}{x-2} + \frac{1}{x+3}$$

$$\int \frac{2x^2 - 9x - 35}{(x+1)(x-2)(x+3)} dx = \int \frac{-4 dx}{x+1} - \int \frac{3 dx}{x-2} + \int \frac{1 dx}{x+3}$$

$$\text{let } x+1 = u$$

$$\frac{dy}{dx} = 1 \\ dx = dy$$

$$\int \frac{-4 dx}{x+1} = \int \frac{-4 \cdot dy}{u} = -4 \int \frac{1}{u} dy$$

$$= -4 \ln u$$

$$= -4 \ln(x+1)$$

$$\text{let } x-2 = u$$

$$\frac{dy}{dx} = 1 \\ dx = dy$$

$$\int \frac{3 dx}{x-2} = \int \frac{3 \cdot dy}{u} = 3 \int \frac{1}{u} dy$$

$$= 3 \ln u$$

$$= 3 \ln(x-2)$$

$$\text{let } u = x+3$$

$$\frac{dy}{dx} = 1 \\ dx = dy$$

$$\int \frac{1}{x+3} dx = \int \frac{1 \cdot du}{u} = \int \frac{1}{u} du$$

$$= \ln u$$

$$= \ln(x+3)$$

$$\therefore \int \frac{2x^2 - 9x - 35}{(x+1)(x-2)(x+3)} dx = -4 \ln(x+1) - 3 \ln(x-2) + \ln(x+3) + C$$

$$= -4 \ln(x+1) - 3 \ln(x-2) + \ln(x+3) + C$$