

NAME:- OGUNBANWO OLUWAFISAYO SIKEMI  
 MATRIC NO:- 19/MHS01/295  
 DEPARTMENT:- M\_BBS

$$1.) \int \frac{11-3x}{x^2+2x-3}$$

$$\frac{11-3x}{(x-1)(x+3)} = \frac{A}{(x-1)} + \frac{B}{(x+3)}$$

$$11-3x = A(x+3) + B(x-1)$$

even  $x = -3$

$$11-3(-3) = A(-3+3) + B(-3-1)$$

$$11+9 = -4B$$

$$20 = -4B$$

$$B = 20/-4 = -5$$

$$B = -5$$

when  $x = 1$

$$11-3(1) = A(1+3) + B(1-1)$$

$$8 = 4A$$

$$A = 2$$

$$\frac{11-3x}{(x-1)(x+3)} = \frac{2}{(x-1)} - \frac{5}{(x+3)}$$

$$\int \frac{11-3x}{x^2+2x-3} = \int \frac{2}{(x-1)} - \int \frac{5}{(x+3)}$$

$$= 2 \ln(x-1) - 5 \ln(x+3)$$

$$2.) \int \frac{4x-16}{x^2-2x-3}$$

$$\frac{4x-16}{(x+1)(x-3)} = \frac{A}{(x+1)} + \frac{B}{(x-3)}$$

$$4x-16 = A(x-3) + B(x+1)$$

when  $x = 3$

$$4(3)-16 = A(3-3) + B(3+1)$$

$$-4 = 4B$$

$$B = -1$$

when  $x = -1$

$$4(-1)-16 = A(-1-3) + B(-1+1)$$

$$-20 = -4A$$

$$A = 5$$

$$\frac{4x-16}{(x+1)(x-3)} = \frac{5}{(x+1)} - \frac{1}{(x-3)}$$

$$\int \frac{4x-16}{x^2-2x-3} = \int \frac{5}{(x+1)} dx - \int \frac{1}{(x-3)}$$

$$= 5 \ln(x+1) - \ln(x-3)$$

$$3.) \int \frac{2x^2-9x+35}{(x+1)(x-2)(x+3)} dx$$

$$3x^2-9x+35 = A + B + C$$

cont.

$$3) \int \frac{2x^2 - 9x - 35}{(x+1)(x-2)(x+3)} dx$$

$$\frac{2x^2 - 9x - 35}{(x+1)(x-2)(x+3)} = \frac{A}{x+1} + \frac{B}{x-2} + \frac{C}{x+3}$$

$$2x^2 - 9x - 35 = A(x-2)(x+3) + B(x+1)(x+3) + C(x+1)(x-2)$$

$$2x^2 - 9x - 35 = A(x^2 + x - 6) + B(x^2 + 4x + 3) + C(x^2 - x - 2)$$

$$2x^2 - 9x - 35 = Ax^2 - Ax - 6A + Bx^2 + 4Bx + 3B + Cx^2 - Cx - 2C$$

$$= x^2(A+B+C) + x(-A+4B-C) + (-6A+3B-2C)$$

$$A+B+C = 2 \quad \dots (i)$$

$$-A+4B-C = -9 \quad \dots (ii)$$

$$-6A+3B-2C = -35 \quad \dots (iii)$$

$$(2-B-C) + 4B-C = -9$$

$$2+3B-2C = -9 \quad \dots$$

$$-6(2-B-C) + 3B-2C = -35$$

$$9B+4C = -23$$

$$3B-2C = -11 \quad \dots (i) \times 9$$

$$9B+4C = -23 \quad \dots (ii) \times 9$$

$$27+18C = -99 \quad \dots (i) \times 3$$

$$\underline{-27+12C = -69}$$

$$-36C = -30$$

$$\underline{30} \quad \underline{-30}$$

$$C = 1$$

$$\text{From } 3B-2C = -11$$

$$3B-2 = -11$$

~~Name: OSAYOBA~~

Cont 3.

$$\frac{3B}{3} = \frac{-}{3} \quad A = 2 - B - C$$
$$B = -3 \quad = 2 - (-3) - 1$$
$$A = 4 \quad = 2 + 3 - 1$$

$$\frac{2x^2 - 9x - 35}{(x+1)(x-2)(x+3)} = \frac{4}{(x+1)} - \frac{3}{(x-2)} + \frac{1}{(x+3)}$$

$$\int \frac{2x^2 - 9x - 35}{(x+1)(x-2)(x+3)} = \int \frac{4dx}{(x+1)} - \int \frac{3dx}{(x-2)} + \int \frac{dx}{(x+3)}$$

$$\int \frac{2x^2 - 9x - 35}{(x+1)(x-2)(x+3)} = 4 \ln|x+1| - 3 \ln|x-2| + \ln|x+3|$$