

Name: ZIDAFAMOR B. ONDUTIMI  
Mat No: 17/ENGO3/060

- i. The design of structure must be safe
- ii. The structure must be economical
- iii. The deformation of the structure must not impair with its integrity

16. Limit state design considers the disadvantages of load factor design and any other failure that can cause the structure to be structurally unfit while Elastic Design is a method of analysis which the design of a structural member is based on a linear stress-strain relationship, assuming that the working stress are only a fraction of the elastic limit of the material.

Staircase Design

$$\text{Slope Factor} = \frac{\sqrt{R^2 + T^2}}{T} = \frac{\sqrt{150^2 + 275^2}}{275} = 1.14$$

Load Analysis

$$\begin{aligned} \text{Weight} &= R \times 24 \text{ kN/m}^2 \\ &= 0.15 \times 24 = 3.6 \text{ kN/m}^2 \end{aligned}$$

$$\text{Finishes} = 1.2 \text{ kN/m}^2$$

$$\begin{aligned} \text{Steps} &= T \times \frac{1}{2} \times 24 \text{ kN/m}^2 \\ &= 0.275 \times 0.5 \times 24 = 3.3 \text{ kN/m}^2 \end{aligned}$$

$$\begin{aligned} \text{D.G.K} &= (A \times B) \times S_F + C \\ &= (4.8 \times 1.14) + 3.3 \\ &= 8.77 \text{ kN/m} \end{aligned}$$

$$D.L F = 1.4 G_k + 1.6 Q_k \\ = 1.4(8.77) + 1.6(1.5) = 14.68 \text{ kN/m}^2$$

$$\text{Span} = T_{\text{total}} + 0.5(l_a + l_b) = (275 \times 12) + 0.5(225 + 225)$$

$$d = h - \text{cover} - \frac{1}{2} \phi \\ = 150 - 25 - 6 = 119 \text{ mm}$$

$$M = \frac{FL^2}{10} = \frac{14.68 \times 3.525^2}{10} = 18.24 \text{ kNm}$$

$$k = \frac{M}{bd^2 f_{cu}} = \frac{18.24 \times 10^6}{1000 \times 119^2 \times 25} = 0.052$$

$$I_a = 0.5 + \sqrt{0.25 - \frac{k}{0.9}} = 0.5 + \sqrt{0.25 - \frac{0.052}{0.9}} = 0.938$$

$$z = I_a d = 0.938 \times 119 = 111.622 \text{ mm}$$

$$A_s = \frac{M}{0.95 f_{yz}} = \frac{18.24 \times 10^6}{0.95 \times 410 \times 111.622} = 419.53$$

$$A_{s\text{prov}} = 452 \text{ mm}^2$$

Provide 412 @ 259 etc

Deflection check

$$f_s = \frac{2}{3} \times \frac{1}{18} \times \frac{A_{\text{req}}}{A_{\text{prov}}} \times f_{yv}$$

$$f_s = \frac{2}{3} \times 1 \times \frac{419.53}{452} \times 250 \\ = 154.69 \text{ N/mm}^2$$

$$M.F = 0.56 + \frac{477 - 154.69}{120 \left( 0.9 + \frac{18.24 \times 10^6}{1000 \times 119^2} \right)}$$

$$= 1.18$$

$$d_{req} = \frac{\text{Span}}{\text{mf. ed.}} = \frac{3525}{1.78 \times 21} = 7617 \text{ mm}$$

since  $d_{req} < d$ , deflection is OK

$$2a) P_1 = P_2 = P_3 = \frac{4300}{4000} = 1.075 < 2 = 2 \text{ way slab}$$

$$P_2 = P_3 = P_4 = \frac{4500}{4000} = 1.25 < 2 = 2 \text{ way slab}$$

$$P_4 = P_5 = P_6 = \frac{4500}{4000} = 1.075 < 2 = 2 \text{ way slab}$$

$$P_{10} = P_{11} = P_{12} = \frac{4000}{1500} = 2.66 > 2 = 1 \text{ way slab}$$

2b) Designing of  $P_2$

$$\frac{l_y}{l_x} = \frac{4500}{4000} = 1.075 \approx 1.1$$

$$\text{Short span coefficient} = 0.054$$

$$\text{Long span coefficient} = \frac{0.058}{0.044}$$

Specifications of slab thickness = 175 mm

$$f_{cu} = 25 \text{ N/mm}^2$$

$$f_y = 410 \text{ N/mm}^2$$

$$DL = 14 \text{ GK} + 1.6 \text{ GK}$$

P4

$$\begin{aligned} \text{Gk} &= \text{weight of slab} = 0.175 \times 24 \\ &\quad \text{Partition} = 1.0 \\ &\quad \text{Finishes} = 1.2 \\ &\quad \underline{\hspace{10em}} \\ &\quad 6.4 \text{ kN/m}^2 \end{aligned}$$

$$\begin{aligned} \text{DL} &= \text{For Parting} \\ &= (1.4 \times 6.4) + (1.6 \times 5) \\ &= 16.96 \approx 17 \text{ kN/m}^2 \end{aligned}$$

$$\begin{aligned} \text{Short span coefficient} &= 0.044 \\ &\quad 0.033 \end{aligned}$$

$$\begin{aligned} \text{Long span coefficient} &= 0.037 \\ &\quad 0.028 \end{aligned}$$

$$\text{Short span mid} = P$$

$$\begin{aligned} M &= B_z \cdot w l^2 \alpha = 0.044 \times 17 \times 4^2 \\ &= 11.968 \end{aligned}$$

$$d = h - \text{cover} - \frac{1}{2} \phi = 144$$

$$k = \frac{M}{b d^2 f_{cu}} = \frac{11.968 \times 10^6}{1000 \times 144^2 \times 25} = 0.023$$

$$\alpha_s = 0.5 + \sqrt{0.25 - k/0.9} = 0.97 > 0.95 = 0.95$$

$$Z = 0.95 \times 144 = 136.8$$

$$A_s = \frac{M}{0.95 f_{ye} Z} = \frac{11.968 \times 10^6}{0.95 \times 410 \times 136.8} = 224.61$$

Provide  $y12 @ 377\text{mm}$

Continues

$$M = B \times w l^2 \alpha = 0.033 \times 17 \times 4^2 = 8.976$$

$$d = 144$$

$$k = \frac{M}{bd^2 f_{cu}} = \frac{8.976 \times 10^6}{0.45 \times 144^2 \times 25} = 0.0173$$

$$P_a = 0.5 + \sqrt{0.25 - \frac{k}{0.9}} = 0.5 + \sqrt{0.25 - \frac{0.0173}{0.9}} = 0.83$$

$$Z = P_a \times d = 0.83 \times 144 = 119.52$$

$$A_s = \frac{M}{0.45 f_{yz}} = \frac{8.976 \times 10^6}{0.45 \times 410 \times 119.52} = 192.81 \text{ mm}^2$$

provide  $y12 @ 377 \text{ mm}$ Long Span  
Mid

$$d = d(\text{shortspan}) - \text{steel thickness} = 144 - 12 = 132 \text{ mm}$$

$$M = B \times w l^2 \alpha = 0.037 \times 17 \times 4^2 = 10.064$$

$$k = \frac{M}{bd^2 f_{cu}} = \frac{10.064 \times 10^6}{1000 \times 132^2 \times 25} = 0.0231$$

$$P_a = 0.5 + \sqrt{0.25 - \frac{k}{0.9}} = 0.97 > 0.95 = 0.95$$

$$Z = P_a \times d = 0.95 \times 132 = 125.4$$

$$A_s = \frac{M}{0.45 f_{yz}} = \frac{10.064 \times 10^6}{0.45 \times 125.4 \times 410} = 206.04$$

provide  $y12 \text{ at } 317 \text{ mm}$

P6

Long span - continuous

$$d = 132 \text{ mm}$$

$$M = B \cdot w l^2 \alpha = 0.028 \times 17 \times 4^2 = 7.616$$

$$k = \frac{M}{l^2 f_{lm}} = \frac{7.616 \times 10^6}{1000 \times 132^2 \times 25} = 0.017$$

$$P_a = 0.5 + \sqrt{0.25 - k/0.9} = 0.98 > 0.95 = 0.95$$

$$Z = I_{ad} = 125.4$$

$$A_s = \frac{M}{0.95 f_{yz}} = \frac{7.616 \times 10^6}{0.95 \times 410 \times 125.4} = 155.93$$

provide  $y/2 @ 377 \text{ mm}$

Deflection Check

$$F_d = \frac{2}{3} \times f_{yv} \times B \times \frac{A_{req}}{A_s \text{ provided}}$$

$$F_d = \frac{2}{3} \times 250 \times 1 \times \frac{224.61}{377} = 99.3$$

$$M.F = 0.55 + \frac{422 - 99.3}{120 \left( 0.9 + \frac{11.968 \times 10^6}{1000 \times 144^2} \right)}$$

$$= 2.68 > 2$$

$$d_{req} = \frac{4 \times 1000}{2 \times 26} = 76.92 \text{ OK}$$