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1. A particle moves along a curve $x = 8t^3$, $y = 4t^3 - 7t$
and $z = t + 3$, where t is time find its

- i) Velocity
- ii) Acceleration

i) for velocity along a curve

$$x = 8t^3$$

$$y = 4t^3 - 7t$$

$$z = t + 3$$

where $t = \text{time}$

$$\text{Velocity } v = \frac{\Delta s}{\Delta t}$$

$\Delta s = \text{change in position}$

$\Delta t = \text{change in time}$

where $t = \text{zero}$

$$\therefore t = \frac{1}{2}$$

$$x = 8t^2$$

$$y = 4t^3 - 7t$$

$$z = t + 3$$

$$t = 1$$

Let $P(x, y, z)$ be any point on the curve and
 $\vec{r} = x + y + z$

be the position vector of P

relative to O as origin

$$\therefore \vec{r} = 8t^2 + 4t^3 - 7t + t + 3$$

since velocity

$$= v = \frac{\Delta s}{\Delta t}$$

$$\vec{r} = 8t^2 + 4t^2 - 7t + t + 3$$

$$\vec{v} = \frac{d\vec{r}}{dt} = (8t) + (4t^2) - 7 + 2t + 3$$

$$8t + 4t^2 - 7 - 2t + 3$$

now at time $t = 1$

substitute the value for $t = 1$

$$\vec{v} = \frac{d\vec{r}}{dt} = 8(1) + (4(1))^2 - 7 - 2(1) + 3$$

ii for acceleration

$$\vec{a} = \frac{d\vec{v}}{dt} = \frac{d}{dt} (8t + (4t^2 - 7) - 2t + 3)$$

$$8t + (2t - 7) - 2t + 3$$

$$8t + (2t - 7) - 2t + 3$$

$$\vec{a} = \frac{d\vec{v}}{dt} = \frac{d}{dt} (8t + 2t - 7 - 2t + 3)$$

$$\vec{a} = \frac{d\vec{v}}{dt} = \frac{d}{dt} (8t + 2t - 7 - 2t + 3)$$

2 find the unit tangent vector to the space curve

$$x = 3t$$

$$y = t^3$$

$$z = t^2$$

$$t = 1$$

$$\vec{r} = x + y + z$$

$$\vec{r} = 3t + t^3 + t^2$$

Since velocity

$$v = \frac{\Delta s}{\Delta t}$$

$$\vec{r} = 3t + t^3 + t^2$$

$$v = \frac{d\vec{r}}{dt} = (3t) + t^3 + t^2$$

$$= 3t + t^3 + t^2$$

Since our time = 1

then substitute the value of $t = 1$

$$\vec{v} = \frac{d\vec{r}}{dt} = 3(1) + (1)^3 + (1)^2$$

$$v = \frac{d\vec{r}}{dt} = 3 + 2^5$$