

MAT 104 Assignment

1) $\int \frac{11-3x}{x^2+2x-3} dx$

Sol

$$\frac{11-3x}{x^2+2x-3} = \frac{A}{x-1} + \frac{B}{x+3}$$

$$\therefore 11-3x = A(x+3) + B(x-1)$$

To find A, $x=1$

$$11-3(1) = A(1+3) + B(1-1)$$

$$8 = 4A$$

$$A=2$$

To find B; $x=-3$

$$11-3(-3) = A(-3+3) + B(-3-1)$$

$$11+9 = -4B$$

$$20 = -4B$$

$$B=-5$$

$$\therefore \int \frac{11-3x}{x^2+2x-3} dx = \int \frac{2}{x-1} dx - \int \frac{5}{x+3} dx$$

$$2 \ln(x-1) - 5 \ln(x+3) + C$$

$$\therefore \int \frac{11-3x}{x^2+2x-3} = 2 \ln(x-1) - 5 \ln(x+3) + C$$

2) $\int \frac{4x-6}{x^2-2x-3} dx$

Sol

$$\frac{4x-6}{x^2-2x-3} = \frac{A}{x+1} + \frac{B}{x-3}$$

$$\therefore 4x-6 = A(x-3) + B(x+1)$$

To get A, $x=-1$

$$4(-1)-6 = A(-1-3)$$

$$-4-6 = -4A$$

$$-10 = -4A$$

$$A = \frac{5}{2}$$

To get B, $x=3$

$$4(3)-6 = B(3+1)$$

$$12-6 = 4B$$

$$6 = 4B$$

$$B = \frac{3}{2}$$

$$\therefore \int \frac{4x-6}{x^2-2x-3} dx = \int \frac{5}{2(x+1)} dx + \int \frac{3}{2(x-3)} dx$$

$$\frac{5}{2} \ln|x+1| + \frac{3}{2} \ln|x-3| + C$$

$$\therefore \int \frac{4x-6}{x^2-2x-3} dx = \frac{5}{2} \ln|x+1| + \frac{3}{2} \ln|x-3| + C.$$

$$3) \int \frac{2x^2-9x-35}{(x+1)(x-2)(x+3)} dx$$

Sol

$$\frac{2x^2-9x-35}{(x+1)(x-2)(x+3)} = \frac{A}{x+1} + \frac{B}{x-2} + \frac{C}{x+3}$$

$$\therefore 2x^2-9x-35 = A(x-2)(x+3) + B(x+1)(x+3) + C(x+1)(x-2)$$

To get A, $x=-1$

$$2(-1)^2-9(-1)-35 = A(-1-2)(-1+3)$$

$$2+9-35 = -6A$$

$$-24 = -6A$$

$$A=4$$

To get B, $x=2$

$$2(2)^2-9(2)-35 = B(2+1)(2+3)$$

$$8-18-35 = 15B$$

$$-45 = 15B$$

$$B = -3.$$

To get C , $x = -3$

$$2(-3)^2 - 9(-3) - 35 = C(-3+1)(-3-2)$$

$$18 + 27 - 35 = C(-2)(-5)$$

$$10 = 10C$$

$$C = 1$$

$$\therefore \int \frac{2x^2 - 9x - 35}{(x+1)(x-2)(x+3)} dx = \int \frac{4}{x+1} dx - \int \frac{3}{x-2} dx + \int \frac{1}{x+3} dx$$

$$4 \ln(x+1) - 3 \ln(x-2) + \ln(x+3) + C$$

$$\therefore \int \frac{2x^2 - 9x - 35}{(x+1)(x-2)(x+3)} = 4 \ln(x+1) - 3 \ln(x-2) + \ln(x+3) + C$$