

$$\frac{dy}{(y-2040)} = -0.025 dt \Rightarrow \int \frac{dy}{(y-2040)} = \int -0.025 dt$$

$$\int \frac{dy}{(y-2040)} = -0.025 \int dt \Rightarrow \ln(y-2040) = -0.025t + c$$

$$y-2040 = e^{-0.025t+c} \Rightarrow y-2040 = e^{-0.025t} e^c$$

$$y-2040 = e^{-0.025t} \cdot y_0 \Rightarrow y-2040 = y_0 e^{-0.025t}$$

$$y = y_0 e^{-0.025t} + 2040 \Rightarrow \text{initially, when } t=1, y=1800$$

$$180 = y_0 e^{-0.025t} + 2040 \Rightarrow 180 - 2040 = y_0 \cdot (-1)$$

$$y_0 = -1860$$

$$y = -1860 e^{-0.025t} + 2040$$

$$y = 2040 - 1860 e^{-0.025t}$$

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COMPUTER ENGINEERING

ENG 282 (ENGINEERING MATHS B)

1) Using Balance law, The accumulation rate of salt within a is equal to the input rate of salt into the system minus the output rate of salt from the system.

Accumulation rate of salt within a system \dot{y} ,

= input rate of salt into the system

= output rate of salt from the system

Let the amount of salt present in the tank at any time be

'y'

Time rate of change of $y = \frac{dy}{dt} = y_{in} - y_{out}$

If 50 gal of brine enters the tank per minute and one gallon

contains $(1 + 50t)$ lb of salt, then

at $t = 1$, $(1 + 50t) = (1 + 50(1)) = 102$ lb

hence the amount of salt entering into the tank is

50 gal/min \times 102 lb/gal = 5100 lb/min

The tank contains 1200 gal of water with dissolved salt and 30 gal of the solution exits the tank per minute. That is $\frac{30 \text{ gal}}{1200 \text{ gal}} = 0.025 = 2.5\%$

of the content of the tank. So 2.5% of the salt present inside

the tank will also leave the tank per minute. That is

$y_{out} = 2.5\%$ of y

a) $\frac{dy}{dt} = 5100 \text{ lb/min} - 2.5\%$ of y lb/min

b) $\frac{dy}{dt} = 5100 - 0.025y$; $\frac{dy}{dt} = -0.025y + 5100$

$\frac{dy}{dt} = -0.025 \left(\frac{-0.025y}{-0.025} + \frac{5100}{-0.025} \right)$ $\int = 0.025(y - 20400)$