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18/ENG02/1006
Computer Engineering
ENG 282: Engineering Mathematics II

Answers

(a) From $dy/dt = y_{in} - y_{out}$

$dy/dt = 50(1+\sin t) - 25\%$ of y

$y_{out} = \frac{30}{1200} = 0.025 = 2.5\%$

$y_{out} = 2.5\%$ of $y = 1/40\,y$

$dy/dt = 50(1+\sin t) - 0.025y$

Operating the variables

$dy/dt + 0.025y = 50(1+\sin t)$

$1 + 0.025y \cdot dy = 50(1+\sin t)\,dt$

(b) $dy/dt = 50(1+\sin t) - 0.025y$

$dy/dt + 0.025y = 50(1+\sin t)$

~~Using~~ linear equation method

~~$dy/dt + 1/0.025y = 50(1+\sin t)$~~

$dy/dt + Py = Q$

$P = 0.025$, $Q = 50(1+\sin t)$

$\int p\,dt = 0.025t$

$I.F = e^{\int p\,dt}$

$I.F = e^{0.025t}$

$y \cdot e^{0.025t} = \int 50(1+\sin t)\, e^{0.025t}\,dt$

$y \cdot e^{0.025t} = 50 \int (1+\sin t) \cdot e^{0.025t}\,dt$

$y \cdot e^{0.025t} = 50 \int e^{0.025t}\,dt + \int e^{0.025t} \sin t\,dt$

$y \cdot e^{0.025t} = 50 \cdot \frac{e^{0.025t}}{0.025} + \int e^{0.025t} \sin t\,dt$

$\int$ by Part

$\int e^{0.025t} \sin t\,dt$ $\qquad \int u\,dv = uv - \int v\,du$

$u = e^{0.025t}$ $\quad dv = \sin t$

$du = 0.025\, e^{0.025t}$ $\quad v = -\cos t$

$\therefore \int e^{0.025t} \sin t = e^{0.025t} \cdot -\cos t - \int -\cos t \cdot 0.025 e^{0.025t} + C$

$\int e^{0.025t}\sin t = -e^{0.025t}\cos t + 0.025\int e^{0.025t}\cos t + C$

$\int u\,dv = uv - \int v\,du$

$u = e^{0.025t}$, $dv = \cos t$

$du = 0.025t\,e^{0.025t}$ $v = \sin t$

$= -e^{0.025t}\cos t + 0.025\left[e^{0.025t}\sin t - \int \sin t\, 0.025\, e^{0.025t}\right]$

$= -e^{0.025t}\cos t + 0.025\left[e^{0.025t}\sin t - 0.025\int \sin t\, e^{0.025t}\right]$

$Q = \int e^{0.025t}\sin t$

$Q = -e^{0.025t}\cos t + 0.025\left[e^{0.025t}\sin t - 0.025\,Q\right]$

$Q = -e^{0.025t}\cos t + 0.025\,e^{0.025t} - 0.25^{-4}Q$

$Q + 6.25^{-4}Q = -e^{0.025t}\cos t + 0.025e^{0.025t}$

$1.000621Q = -e^{0.025t}(\cos t - 0.025)$

$Q = \frac{-e^{0.025t}}{1.000625}(\cos t - 0.025) + C$

$y = 2000 - \frac{50}{1.000625}(\cos t - 0.025\sin t) + \frac{50C}{e^{0.025t}}$

$y = 150$, $t = 0$

$150 = 2000 - \frac{50}{1.000625}(1 - 0) + \frac{50C}{1}$

$150 = 2000 - 49.968(1) + 50C$

$150 = 1950.032 + 50C$

$\frac{50C}{50} = \frac{-1800.032}{50}$

$C = -36.00064$

$Q = \frac{-e^{0.025t}}{1.000625}(\cos t - 0.025) + C$

$\int e^{0.025t}\sin t = \frac{-e^{0.025t}}{1.000625}(\cos t - 0.025) + C$

$y\cdot e^{0.025t} = 50\left[\frac{e^{0.025t}}{0.025} - \frac{e^{0.025t}}{1.000625}(\cos t - 0.025\right.$

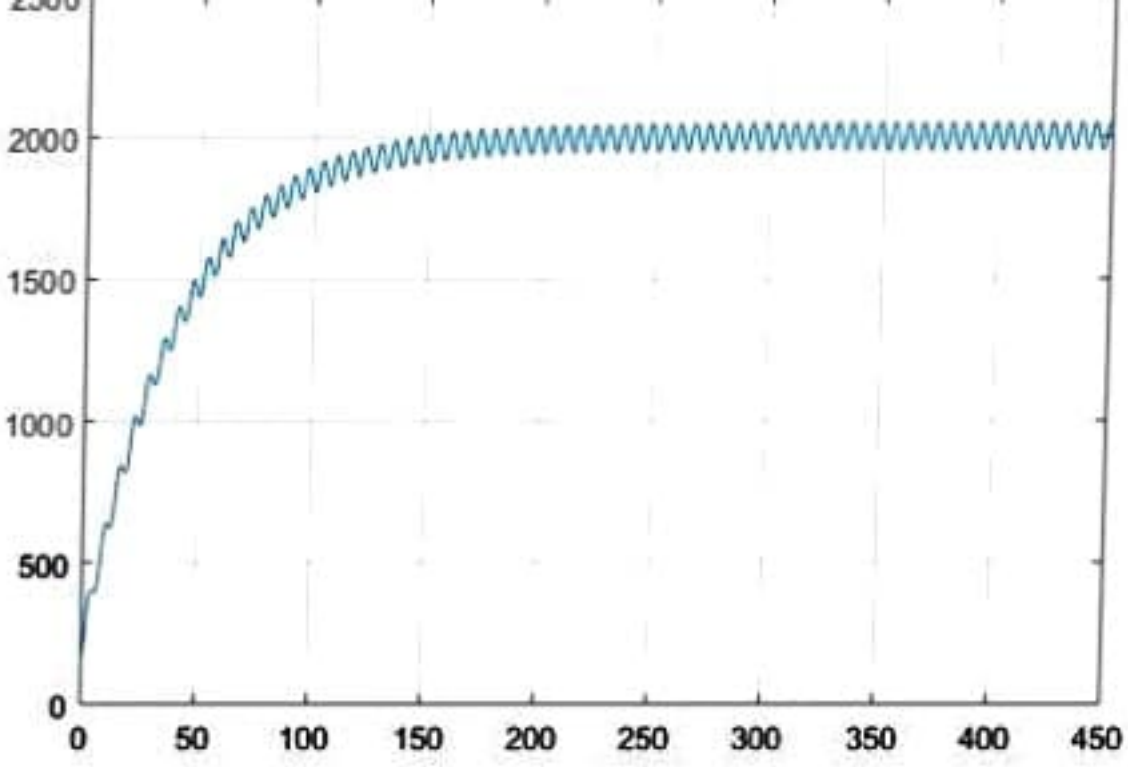
$\left. + C\right]$

$y\cdot e^{0.025t} = 2000e^{0.025t} - \frac{50\cdot e^{0.025t}}{1.000625}(\cos t - 0.$

$+ 50C$

$y = 2000 - \frac{50}{1.000625}(\cos t - 0.025) + \frac{50C}{e^{0.025t}}$

```
commandwindow
clear
clc
close all
syms m t
ans=dsolve('Dm+0.025*m=50+50*sin(t)','m(0)=150')
t=0:0.5:450
tn=subs(ans,t)
plot(t,tn)
grid on
```


2000
1500
1000
500
0
0
50
100
150
200
250
300
350
400
450

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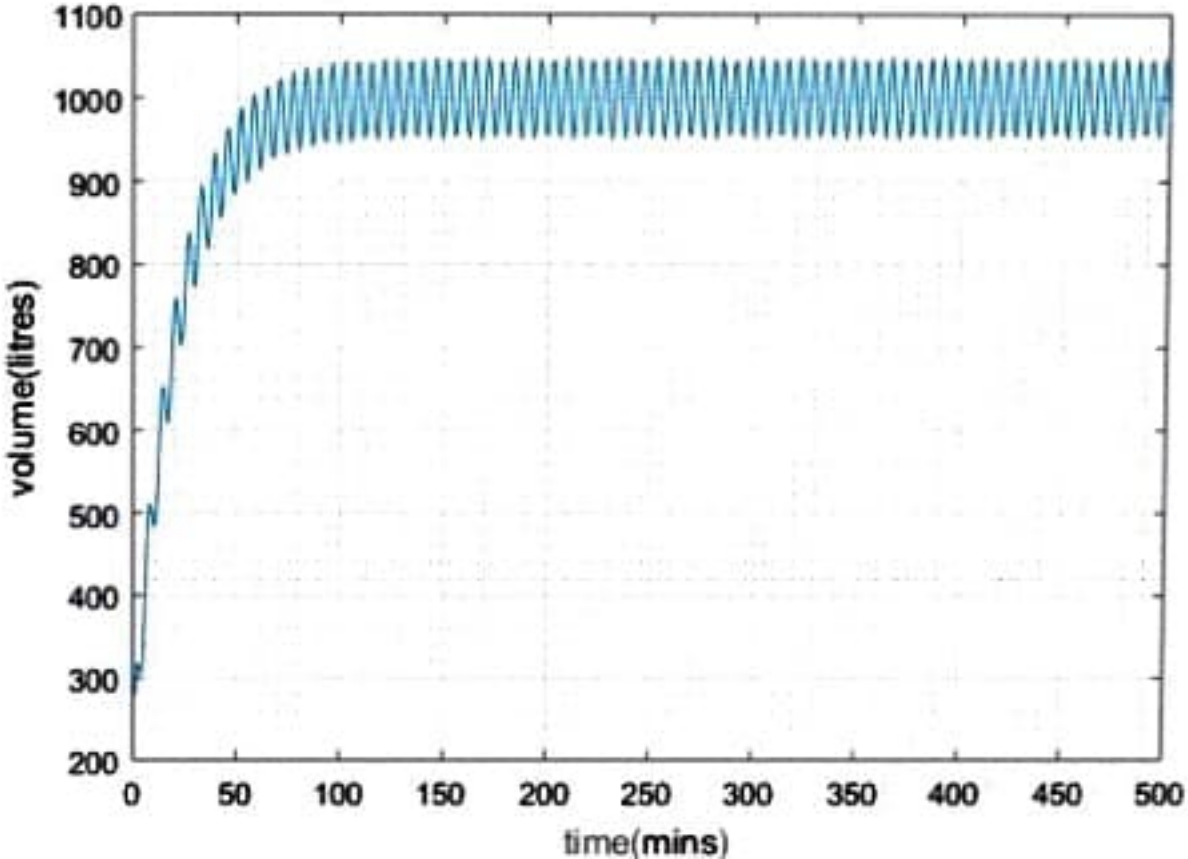
B2 279.963914100068

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U
1	t(min)	V(Litre)																			
2	1	279.9639																			
3	2	318.1907																			
4	3	313.8601																			
5	4	303.601																			
6	5	327.9009																			
7	6	393.9593																			
8	7	469.1423																			
9	8	511.0566																			
10	9	506.5922																			
11	10	484.0395																			
12	11	487.1398																			
13	12	534.9268																			
14	13	604.2824																			
15	14	651.2431																			
16	15	651.4694																			
17	16	622.6706																			
18	17	608.3676																			
19	18	637.9229																			
20	19	699.585																			
21	20	751.3315																			
22	21	759.541																			
23	22	729.9392																			
24	23	702.3679																			
25	24	714.1865																			
26	25	765.9535																			
27	26	820.9421																			
28	27	838.9333																			
29	28	813.2194																			
30	29	776.7953																			

```
clear
clc
close all
syms t
values=[]
t=1:1:500
mean=1000-((exp(-0.05*t))*800)
y=1000+(50/1.0025)*sin(t)+(2.5/1.0025)*cos(t)-((exp(-0.05*t))*80

if rem(t,2) ==0
    values=[values,mean]
else
    values=[values,y]
end
excelvalues=transpose(values)
mins=transpose(t)
plot(t,values)
grid on
grid minor
xlabel ('time(mins)')
ylabel('volume(litres)')
xlswrite('odevbesdata.xlsx',{'t(min)'},'veriler','A1')
xlswrite('odevbesdata.xlsx',mins,'veriler','A2')
xlswrite('odevbesdata.xlsx',{'V(Litre)'},'veriler','B1')
xlswrite('odevbesdata.xlsx',excelvalues,'veriler','B2')
```


1100
1000
900
800
700
600
500
400
300
200
volume(litres)
0
50
100
150
200
250
300
350
400
450
500
time(mins)