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Civil Engineering

Engineering Mathematics

$$1a) \frac{dm}{dt} = m_{in} - m_{out}$$

$$m_{in} = 50 \times (1 + \sin t)$$

$$m_{out} = 30 \times \left( \frac{m}{1200 + 20t} \right)$$

$$\frac{dm}{dt} = 50(1 + \sin t) - \frac{3m}{120 + 2t}$$

$$\frac{dm}{dt} + \frac{3m}{120 + 2t} = 50(1 + \sin t)$$

using I.F

$$\frac{dy}{dx} + Py = Q$$

$$P = \frac{3}{120 + 2t}, \quad Q = 50(1 + \sin t)$$

$$\int P dx = 3 \ln(120 + 2t)$$

$$I.F = e^{\int P dx} = e^{3 \ln(120 + 2t)} = (120 + 2t)^3$$

$$I.F = (120 + 2t)^3$$

$$y \cdot I.F = \int Q \cdot I.F dx$$

$$m(120 + 2t)^3 = 50 \int (120 + 2t)^3 (1 + \sin t) dt$$

$$m(120 + 2t)^3 = 2t^4 + 480t^3 + 43200t^2 + 1728000t - \cos t (120 + 2t)^3 + 6 \sin t (120 + 2t)^2 + C$$

$$m = \frac{(2t^4 + 480t^3 + 43200t^2 + 1728000t) - \cos t + \frac{6 \sin t}{(120 + 2t)}}{(120 + 2t)^3} + \frac{C}{(120 + 2t)^3}$$

$$\text{at } t = 0$$

$$m = 150$$

$$150 = 50 \left( -1 + \frac{C}{(120)^3} \right)$$

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$$150 = -50 + \frac{50C}{120^3}$$

$$C = 518399$$

$$\eta = \frac{(2t^4 + 480t^3 + 43200t^2 + 172800t) - \cos t + 6 \sin t}{(120 + 2t)^3}$$

$$+ \frac{518399}{(120 + 2t)^3}$$

