

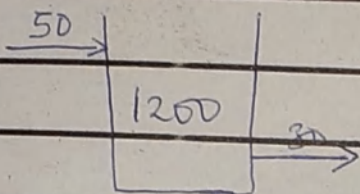
RASI UMMI-SALMAONIZE

18ENG081020

BIOMEDICAL ENGINEERING

ASSIGNMENT

Let $m(t)$ 'lb' be the amount of brine salt in tank at any time t .



By principle of continuity

$$\frac{dm}{dt} = \text{Rate of inflow} - \text{Rate of outflow}$$

$$\frac{dm}{dt} = \frac{50 \text{ gal}}{\text{min}} \times (1 + \sin t) \frac{\text{lb}}{\text{gal}} - \frac{30 \text{ gal}}{\text{min}} \times \left(\frac{x}{1200} \right) \frac{\text{lb}}{\text{gal}}$$

$$\frac{dm}{dt} = 50(1 + \sin t) - \frac{30x}{1200} \quad m(0) = 150 \text{ lbs}$$

Solution

$$\frac{dx}{dt} + \frac{x}{40} = 50(1 + \sin t) \quad [\text{Bernoulli's equation}]$$

Integrating factor;

$$\mu = e^{\int \frac{dt}{40}} = e^{\frac{t}{40}}$$

$$\rightarrow \int d(x e^{\frac{t}{40}}) = \int 50(1 + \sin t) e^{\frac{t}{40}} dt$$

$$x e^{\frac{t}{40}} = \int (50 e^{\frac{t}{40}} + 50 \sin t e^{\frac{t}{40}}) dt + C$$

$$\rightarrow x e^{\frac{t}{40}} = 50 e^{\frac{t}{40}} + 50 \int e^{\frac{t}{40}} \sin t dt + C$$

$$\rightarrow x e^{\frac{t}{40}} = 2000 e^{\frac{t}{40}} + \frac{50 \times 40}{1601} \left[e^{\frac{t}{40}} ((\sin t) - 40 \cos t) + 40 \right] + C$$

$$m(0) = 150 \text{ lb}$$

$$\Rightarrow 150 = 2000 + \frac{2000}{1601} (-40 + 40) + C$$

$$C = -2000 + 150$$

$$C = -1850$$

$$\Rightarrow m(t) = 2000 + \frac{2000}{1601} \left[(\sin t + 40 \cos t) + 40 e^{-\frac{t}{40}} \right] - 1850 e^{-\frac{t}{40}}$$

$$m(t) = 2000 + \frac{2000}{1601} (\sin t - 40 \cos t) + \left(\frac{80000 - 1850}{1601} \right) e^{-\frac{t}{40}}$$

commandwindow

```
clear
```

```
clc
```

```
close all
```

```
syms t m
```

```
s=dsolve('Dm+(0.025*m)=50*(1+sin(t)),m(0)=150')
```

```
kn=0:0.5:450
```

```
rn=subs(s, kn)
```

```
plot(kn, rn)
```

```
title('Graph of dynamic response of the system')
```

```
ylabel('Amount of Salt in tank')
```

```
xlabel('time (t (min))')
```

```
grid on
```

```
grid minor
```

Command Window

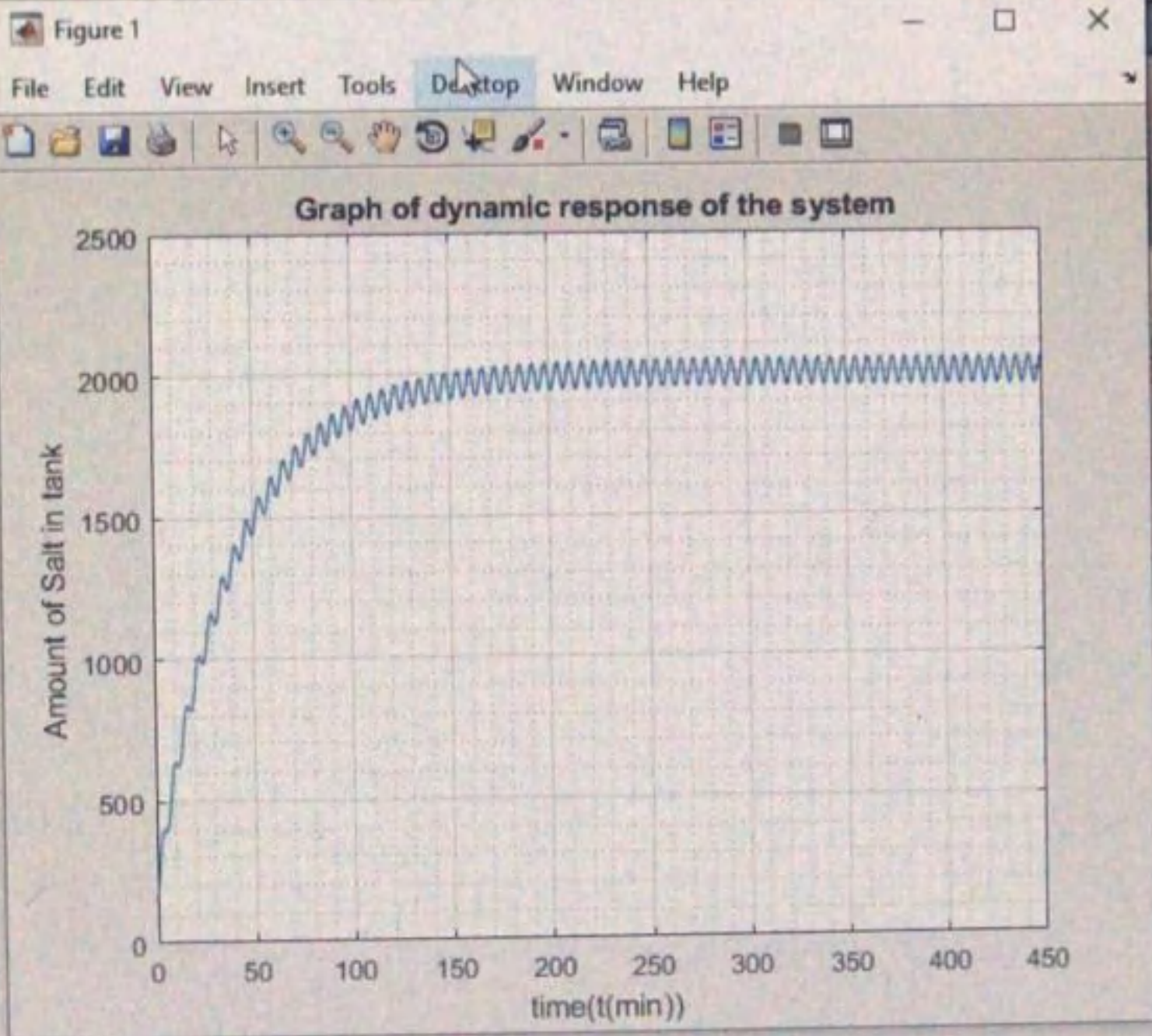
to MATLAB? See resources for [Getting Started](#).

1 =

```
150, 2000 - (2000*1601^(1/2)*cos(atan(1/40) + 1/2))/14
```

>

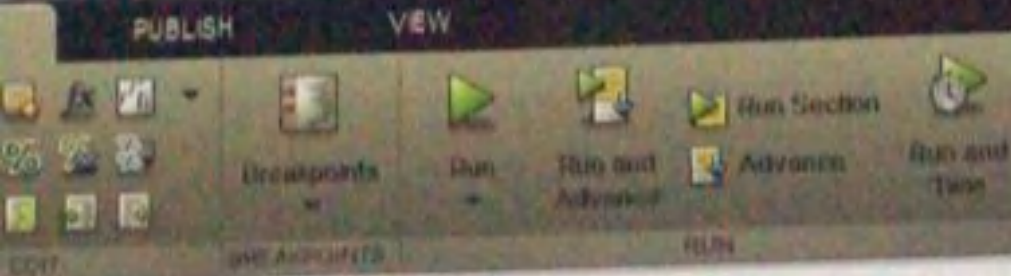




Command Window

new to MATLAB? See resources for [Getting Started](#).

```
rn =
[ 150, 2000 - (2000*1601^(1/2)*cos(atan(1/40) + 1/2))/1601 - (2881850*exp(-1
>>
<
```



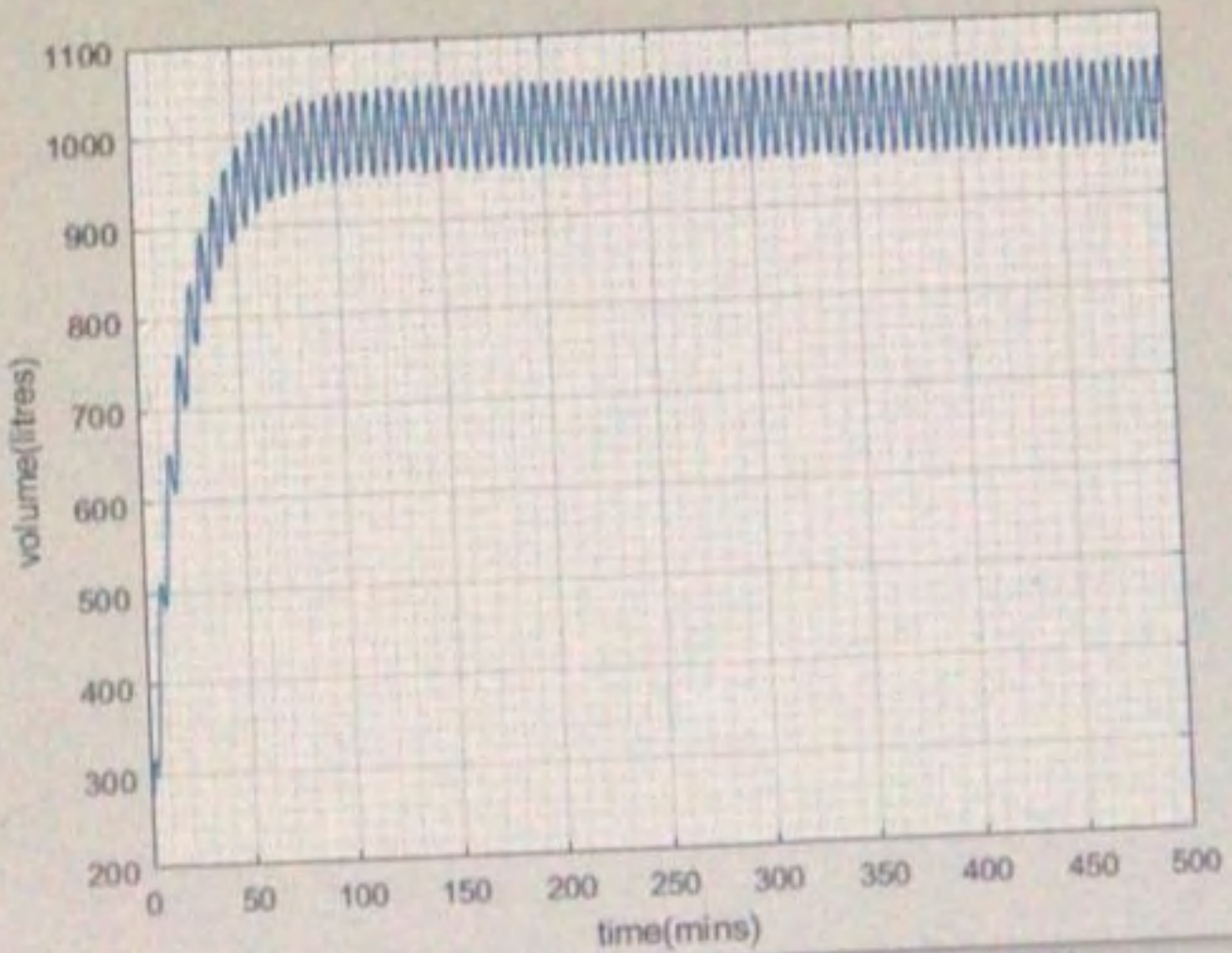
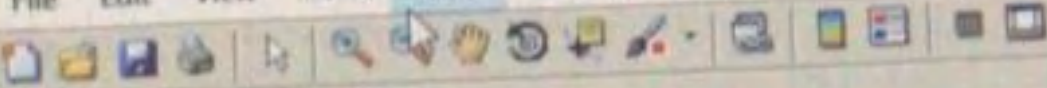
MATLAB
Editor - C:\Users\amanda\Documents\MATLAB\UMMIIII.m
SALMAAA.m x UMMIIII.m x +

```
1 - commandwindow
2 - clear
3 - clc
4 - close all
5 - syms t
6 - values=[]
7 - t=1:1:500
8 - y=1000+((50/1.0025)*sin(t))+(2.5/1.0025)*cos(t)-((exp(-0.05*t))*802.4)
9 - mean=1000-((exp(-0.05*t))*800)
10 - if rem(t,2)==0
11 -     values=[values,mean]
12 - else
13 -     values=[values,y]
14 - end
15 - excelvalues=transpose(values)
16 - mins=transpose(t)
17 - plot(t,values)
18 - grid on
19 - grid minor
20 - xlabel('time (mins)')
21 - ylabel('volume (litres)')
22 - xlswrite('odevbesdata.xlsx',{'t (min)'},'veriler','A1')
23 - xlswrite('odevbesdata.xlsx',mins,'veriler','A2')
24 - xlswrite('odevbesdata.xlsx',{'V (Litre)'},'veriler','B1')
25 - xlswrite('odevbesdata.xlsx',excelvalues,'veriler','B2')
```

Command Window

Figure 1

File Edit View Insert Tools Desktop Window Help



```
xlswrite('odevbesdata.xlsx',('V(Litre)'),'veriler','B1')  
xlswrite('odevbesdata.xlsx',excelvalues,'veriler','B2')
```

Command Window

New to MATLAB? See resources for [Getting Started](#).

498
499
500

fx >>

File Home Insert Page Layout Formulas Data Review View

Cut Copy Format Painter Clipboard

Calibri 11 A A

B *I* U [Grid] [Color] [Text Color]

Alignment

Wrap Text Merge & Center

Number \$ %

B2 279.963914100068

	A	B	C	D	E	F	G	H	I	J
1	t(min)	V(litre)								
2	1	279.9639								
3	2	318.1907								
4	3	313.8601								
5	4	303.601								
6	5	327.9009								
7	6	393.9593								
8	7	469.1423								
9	8	511.0566								
10	9	506.5922								
11	10	484.0395								
12	11	487.1398								
13	12	534.9268								
14	13	604.2824								
15	14	651.2431								
16	15	651.4694								
17	16	622.6706								
18	17	608.3676								
19	18	637.9229								
20	19	699.585								
21	20	751.3351								
22	21	759.541								
23	22	729.9392								
24	23	702.3679								
25	24	714.1865								

Home Insert Page Layout Formulas Data Review View

Cut Copy Format Painter Clipboard

Calibri 11 A A

B *I* U [Grid] [Color] [Text Color]

Font Alignment

Wrap Text Merge & Center

B2 f_x 279.963914100068

A	B	C	D	E	F	G	H	I
5	327.9009							
6	393.9593							
7	469.1423							
8	511.0566							
9	506.5922							
10	484.0395							
11	487.1398							
12	534.9268							
13	604.2824							
14	651.2431							
15	651.4694							
16	622.6706							
17	608.3676							
18	637.9229							
19	699.585							
20	751.3351							
21	759.541							
22	729.9392							
23	702.3679							
24	714.1865							
25	765.9535							
26	820.9421							
27	838.9333							
28	813.2194							
29	776.7935							