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 Computer Engineering

1) Applying the balance law  
 Accumulation rate of input rate of salt - output rate of salt.

~~Rate of change of system~~

Denoting the amount of salt present in the tank at any time  $t$  as  $y$ , its time rate of change is given by

$$\frac{dy}{dt} = y_{in} - y_{out}$$

Since 50 gal of brine enter the tank <sup>per minute and</sup> ~~per min~~ of any time ~~per min~~ <sup>per minute</sup> and ~~the tank contains 20 gal of brine~~ <sup>change in the tank</sup> one gallon contains  $\frac{y}{20}$  (1 pint) lb of salt;

it means that the amount of salt entering the tank is  $y_{in} = \frac{50 \text{ gal}}{\text{min}} \times \frac{1.02 \text{ lb}}{\text{gal}} = 51 \frac{\text{lb}}{\text{min}}$

The tank contains 20 gal of water with the dissolved salt and 50 gal of the solution leaves the tank per minute. That is  $\frac{20 \text{ gal}}{20 \text{ gal}} = 0.025 = 2.5\%$  of the content of the tank.

If that's the case, 2.5% of the salt present in the tank will also leave the tank per minute in other words;

$$y_{out} = 2.5\% \text{ of } y$$

a) therefore,  $\frac{dy}{dt} \frac{\text{lb}}{\text{min}} = 51 \frac{\text{lb}}{\text{min}} - 2.5\% \text{ of } y \frac{\text{lb}}{\text{min}}$

b)  $\frac{dy}{dt} = 51 - 0.025y$ ;  $\frac{dy}{dt} = -0.025y + 51$ ;

$$\frac{dy}{dt} = 0.025 \left[ \frac{-0.025y}{-0.025} + \frac{51}{-0.025} \right]; \frac{dy}{dt} = \frac{0.02}{0.025} \ln \left| \frac{-0.025y + 51}{-0.025 \cdot 2040} \right|$$

$$\frac{dy}{(y-2040)} = -0.025 dt, \int \frac{dy}{(y-2040)} = \int -0.025 dt$$

$$\int \frac{dy}{(y-2040)} = -0.025 \int dt; \ln(y-2040) = -0.025t + C$$

$$y-2040 = e^{-0.025t} \cdot e^C$$

$$y-2040 = y_0 e^{-0.025t}; y = y_0 e^{-0.025t} + 2040$$

(Initially)

$$y = 150 \text{ lb}$$

$$150 = y_0 e^{0.025t} + 2040; 150 - 2040 = y_0 e^{0.025t}$$

$$y_0 = -1890$$

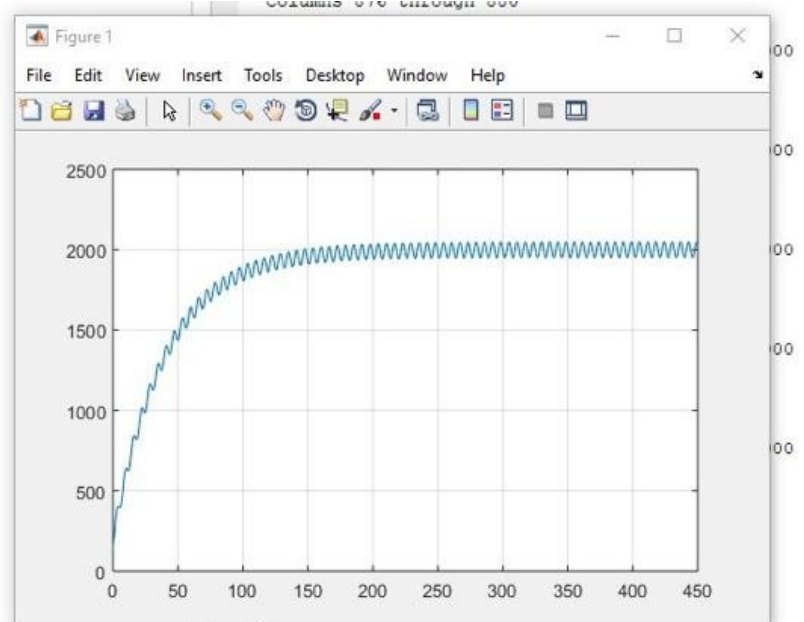
$$y = -1890 e^{-0.025t} + 2040$$

$$y = 2040 - 1890 e^{-0.025t}$$

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1 - commandwindow
2 - clear
3 - clc
4 - close all
5 - syms m t
6 - ans=dsolve('Dm+0.025*m=50+50*sin(t)', 'm(0)=150')
7 - t=0:0.5:450
8 - tn=subs(ans,t)
9 - plot(t,tn)
10 - grid on

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[ 150, 2000 - (2000*1601^(1/2)*cos(atan(1/40) + 1/2))/1
fx >>
<

```

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1  commandwindow
2  clear
3  clc
4  close all
5  syms t
6  values=[]
7  t=1:1:500
8  mean=1000-((exp(-0.05*t))*800)
9  y=1000+(50/1.0025)*sin(t)+(2.5/1.0025)*cos(t)-((exp(-0.05*t))*802.4
10
11  if rem(t,2) ==0
12      values=[values,mean]
13  else
14      values=[values,y]
15  end
16  excelvalues=transpose(values)
17  mins=transpose(t)
18  plot(t,values)
19  grid on
20  grid minor
21  xlabel('time(mins)')
22  ylabel('volume(litres)')
23  xlswrite('odevbesdata.xlsx',{'t(min)'),'veriler','A1')
24  xlswrite('odevbesdata.xlsx',mins,'veriler','A2')
25  xlswrite('odevbesdata.xlsx',{'V(Litre)'},'veriler','B1')
26  xlswrite('odevbesdata.xlsx',excelvalues,'veriler','B2')
27

```

