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MAT NO: 18/ENGO21038

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Assignment

1) Applying the balance law

Accumulation rate = input rate of salt - output rate of salt within system into the system salt from the system

Time rate of change is given as

$$\frac{dy}{dt} = y_{in} - y_{out}$$

50 gal of brine enters the tank per minute and one gallon contains $(1 + \sin t)$ lb of salt;

at $t=1$; $(1 + \sin t) = (1 + \sin 1) = 1.02$ lb of salt;

∴ it means that the amount of salt entering the tank is $y_{in} = \frac{50 \text{ gal}}{\text{min}} \times \frac{1.02 \text{ lb}}{\text{gal}} = \frac{51 \text{ lb}}{\text{min}}$

The tank contains 1200 gal of water with the dissolved salt, $\frac{1}{3}$ 30 gallons of the solution leaves the tank per minute. That is $\frac{30 \text{ gal}}{1200 \text{ gal}} = 0.025 =$

2.5 % of the content of the tank. 2.5 % of the salt present in the tank, per minute

$$y_{out} = 2.5 \% \text{ of } y$$

∴ Therefore: $\frac{dy}{dt} \text{ lb} = \frac{51 \text{ lb}}{\text{min}} - 2.5 \% \text{ of } \frac{y \text{ lb}}{\text{min}}$

$$\text{∴ } \frac{dy}{dt} = 51 - 0.025y; \quad \frac{dy}{dt} = -0.025y + 51$$

$$\frac{dy}{dt} = -0.025 \left[\frac{-0.025y + 51}{-0.025} \right]; \quad \frac{dy}{dt} = -0.025y - 2040y$$

$$\frac{dy}{(y-2040)} = -0.025 dt; \int \frac{dy}{(y-2040)} = \int -0.025 dt$$

$$\int \frac{dy}{(y-2040)} = -0.025 \int dt; \ln(y-2040) = -0.025t + C$$

$$y - 2040 = e^{-0.025t} C; y - 2040 = e^{-0.025t} y_0$$

$$y - 2040 = e^{-0.025t} y_0; y - 2040 = y_0 e^{-0.025t}$$

$$y = y_0 e^{-0.025t} + 2040; \text{given that when } t=0 \text{ in (initially),}$$

$$150 = y_0 e^{-0.025 \cdot 0} + 2040; 150 - 2040 = y_0 \times 1;$$

$$y_0 = -1890$$

50;

$$y = -1890 e^{-0.025t} + 2040$$

$$y = 2040 - 1890 e^{-0.025t}$$

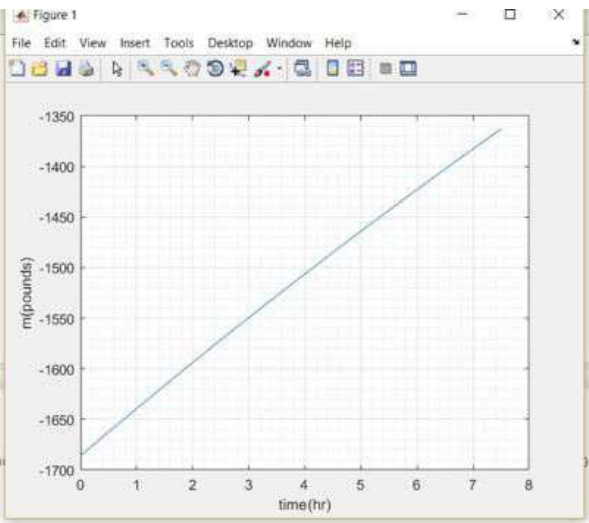
```
okopido.m
1 - clear
2 - clc
3 - close all
4 - syms m t
5 - t = [0:0.5:7.5]
6 - m = 204 - 1890*exp(-0.025*(t))
7 - plot(t,m)
8 - xlabel('time(hr)')
9 - ylabel('m(pounds)')
10 - grid on
11 - grid minor
```

Command Window

t =
0 0.5000 1.0000 1.5000 2.0000 2.5000 3.0000

m =
1.0e+03 *
-1.6860 -1.6625 -1.6393 -1.6164 -1.5938 -1.5715 -1.5494 -1.5277 -1.5061 -1.4849 -1.4639 -1.4432 -1.4227 -1.4025 -1.3826 -1.3629

fx >>



```

1  commandwindow
2  clear
3  clc
4  close all
5  syms t
6  values=[]
7  t=1:1:500
8  mean=1000-((exp(-0.05*t))*800)
9  y=1000+(50/1.0025)*sin(t)+(2.5/1.0025)*cos(t)-((exp(-0.05*t))*802.4
10
11  if rem(t,2) ==0
12      values=[values,mean]
13  else
14      values=[values,y]
15  end
16  excelvalues=transpose(values)
17  mins=transpose(t)
18  plot(t,values)
19  grid on
20  grid minor
21  xlabel('time(mins)')
22  ylabel('volume(litres)')
23  xlswrite('odevbesdata.xlsx',{'t(min)'],'veriler','A1')
24  xlswrite('odevbesdata.xlsx',mins,'veriler','A2')
25  xlswrite('odevbesdata.xlsx',{'V(Litre)'],'veriler','B1')
26  xlswrite('odevbesdata.xlsx',excelvalues,'veriler','B2')
27

```

