

EBONG PRINCE VINCENT

181ENG041028

ELECTRICAL ELECTRONICS

MATHS ENG 282 ASSIGNMENT

1. Tanks holds

- Input rate \rightarrow 50 gal of brine/min [1 gal has (1+5nt) lb of salt]

- Output rate \rightarrow 30 gal of brine/min

$m \rightarrow$ amount of salt of any time t

Using the balance law

$$\frac{dm}{dt} = m_{in} - m_{out}$$

50 gal of water enter per minute and a gallon has (1+5nt) lb of salt

$$\therefore M_{in} = 50 \text{ gal/min} \times (1+5nt) = 50(1+5nt) \text{ lb/min}$$

If the tank contains 1200 gal of water and 30 gal of water leaves per minute. That means $\frac{30}{1200} = \frac{1}{40} = 0.025$

\Rightarrow 2.5% of water in the tank leaves per minute. This also means that 2.5% of salt will also leave the tank per minute

$$m_{out} \Rightarrow 2.5\% \text{ of } m$$

$$\frac{dm}{dt} = 50(1+5nt) - 0.025m \rightarrow (i)$$

b. Differentiating using integration factor method

$$\frac{dm}{dt} + 0.025m = 50(5nt+1) \rightarrow (ii)$$

Let

$$\frac{dy}{dx} + Py = Q \left(\frac{dy}{dx} + Pm = Q \right)$$

$$P = 0.025, \quad Q = 50(5nt+1)$$

$$e^{\int p dt} = \text{Integrating factor}$$

$$\int p dt = \int 0.025 dt = 0.025t$$

$$IF = e^{0.025t}$$

$$\text{From } y \cdot IF = \int Q \cdot IF dt + C$$

$$m \cdot IF = \int Q \cdot IF dt$$

$$m \cdot e^{0.025t} = \int 50(5 \sin t + 1) e^{0.025t} dt$$

$$= 50 \int e^{t/40} (\sin t + 1) dt$$

$$\text{Let } u = t/40 \Rightarrow \frac{du}{dt} = \frac{1}{40}, dt = 40 du$$

$$= 40 \int e^u (\sin 40u + 1) du$$

$$= \int e^u (\sin 40u + 1) du$$

$$6q = 5 \sin 40u + 1$$

$$dp = e^u du$$

$$dq = 40 \cos 40u$$

$$\int df = \int e^u du$$

$$\frac{dq}{du} = 40 \cos 40u$$

$$p = e^u$$

$$\text{From } \int q dp = qp - \int p dq$$

$$\int 40e^u (\cos 40u) du = 540 \int e^u (\cos 40u) du$$

$$\int e^u (\cos 40u) du \Rightarrow \text{Let } q = \cos 40u, dp = e^u du$$

$$\int e^u (\cos 40u) du = e^u \cos 40u - \int 40e^u (\sin 40u) du \quad \text{--- (iii)}$$

Integration by part

$$q = -40 \sin 40u, dp = e^u$$

$$dq = -1600 (\cos 40u) du, p = e^u$$

$$\int e^u (\cos 40u) du = e^u (\cos 40u - (-400 \sin 40u) - \int -1600 e^u (\cos 40u) du$$

$$160 \int e^u (\cos 40u) du = e^u (\cos 40u + 40e^u \sin 40u$$

$$\int e^u (\cos 40u) du = \frac{e^u (\cos 40u + 40e^u \sin 40u)}{160}$$

$$160 \cdot 1$$

$$40 \int e^u (\cos 40u) du = 40 (40e^u \sin 40u + e^u \cos 40u) \quad \text{--- (iv)}$$

$$\Rightarrow \int e^u (\sin 40u + 1) du = e^u \sin 40u + 1 - 540e^u (\cos 40u) du$$

$$\int e^u (\sin 40u + 1) du = e^u \sin 40u + 1 - 40(40e^u \sin 40u + e^u \cos 40u)$$

$$160 \cdot 1$$

$$40e^{t/40} \int_{160}^{400} \frac{1}{u} du = 40e^{t/40} (\ln 400 + 1) - 1600 (40e^{t/40} \ln 400 + e^{t/40} (\ln 400))$$

Put $u = t/40$

$$40e^{t/40} (\sin t + 1) - 1600 (40e^{t/40} + e^{t/40} (\cos t))$$

$$\int 50 e^{t/40} (\sin t + 1) dt$$

$$50 \int e^{t/40} (\sin t + 1) dt \Rightarrow \frac{2000 e^{t/40}}{160} (\sin t - 40(\cos t + 160)) + C \quad (v)$$

Recall the original integration factor

$$m' + 0.025m = 150(\sin t + 1)$$

$$m' e^{0.025t} = \int 150(\sin t + 1) \cdot e^{0.025t} dt$$

$$m' e^{0.025t} = 2000 e^{0.025t} (\sin t - 40(\cos t + 160)) + C$$

$$m = \frac{2000}{160} (\sin t - 40(\cos t + 160)) + m_0 \cdot e^{-0.025t} \quad (vi)$$

at $t = 0, m = 150$

and $m = 150$ lb of salt

$$150 = \frac{2000}{160} (\sin 0 - 40(\cos 0 + 160)) + m_0 \cdot 1$$

$$150 = 1950 \cdot 0.3 + m_0$$

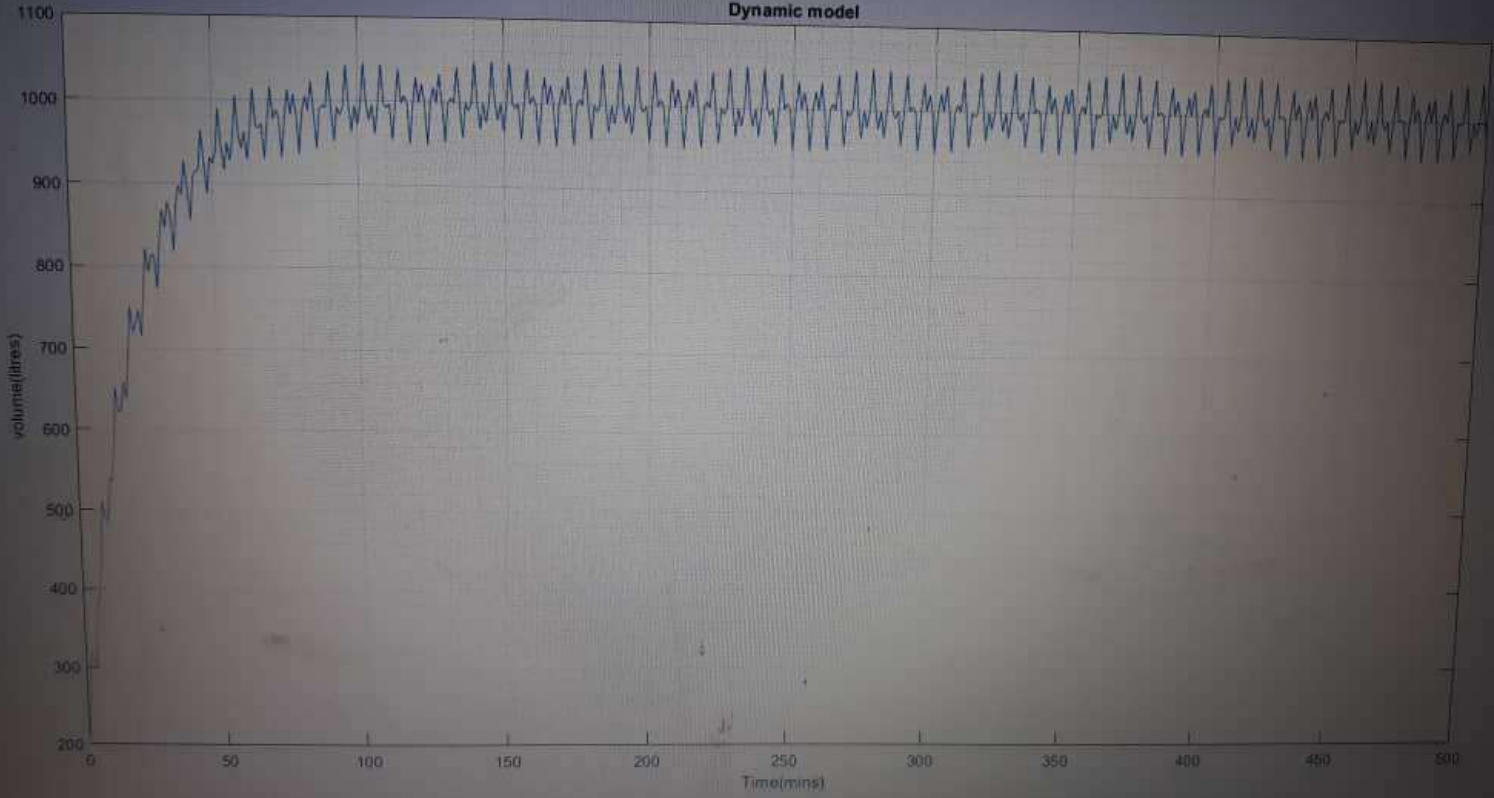
$$m_0 = -1800 \cdot 0.3$$

put m_0 in equation (vi)

$$m = \frac{2000}{160} (\sin t - 40(\cos t + 160)) - 1800 \cdot 0.3 e^{-0.025t}$$

$$m = \frac{2000}{160} (\sin t - 40(\cos t + 160)) - \frac{1800 \cdot 0.3}{e^{0.025t}}$$

Dynamic model



- Name
- m3registry
- registry
- util
- win64
- deploytool.bat
- lodata.xml
- lodata.xsd
- lodata_utf8.xml
- mathassignmenthomeone.m
- matlab.exe
- mbuild.bat
- mcc.bat
- mex.bat
- mex.pl
- mexext.bat
- mexsetup.pm
- mexutils.pm
- mw_mprexec.bat
- worker.bat

```

15 - m=1;
16 - a=[m k];
17 - grid on
18 - grid minor
19 - xlabel("Time (min)")
20 - ylabel("volume (litres)")
21 - title("Dynamic model")
22 - mdata1='odevbesdata.xlsx';
23 - mdata2='veriler';
24 - xlswrite(mdata1,'t(min)',mdata2,'A1')
25 - xlswrite(mdata1,'v (litre)',mdata2,'B1')
26 - xlswrite(mdata1,A,mdata2,'A1')
27 - function Yo=Y(t)
28 -     Yo=50/0.05 + (50/1.0025)*sin(t) + 50*(0.05*cos(t))/1.0025 - 802.49*exp(-0.05*t);
29 - end
30 - function Ymo=Ym(t)
31 -     Ymo=1000-800*exp(-0.05*t);
32 - end
33
34
35

```

mathassignmenthomeone.m (Script)

Command Window

$$43200000 t - 43128000 \cos(t) + 2158800 \sin(t) - 36000 t^2 \cos(t) - 200 t^3 \cos(t) + 600 t^2 \sin(t)$$

```
1 -   commandwindow
2 -   clear
3 -   clc
4 -   m=[0:1:500];
5 -   k=[];
6 -   for i=m
7 -       if(mod(i,2)==0)
8 -           k=[k Y(i)];
9 -       else
10 -           k=[k Ym(i)];
11 -       end
12 -   end
13 -   plot(m, k)
14 -   k=k';
15 -   m=m';
16 -   a=[m k];
17 -   grid on
18 -   grid minor
19 -   xlabel("Time (min) ")
20 -   ylabel("volume (litres) ")
21 -   title("Volume vs Time")
```

Command Window

$$43200000 t - 43128000 \cos(t) + 2158800 \sin(t) -$$

$$\cos(t) + 72000 t \sin(t) + 1090000 t^2 + 12000$$

f_x >>

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