

AKPOMUDJERE OGHENETEKEUWE OBRUCHE
 IP/ENG 06/006
 MECHANICAL ENGINEERING

①

① $\frac{dy}{dx} + y = 8$

$\frac{dy}{dt} = y_{in} - y_{out}$

$$m_{in} = \frac{50 \text{ gal}}{\text{min}} \times \frac{(1 + \sin t) 16}{\text{gal}} = \frac{50(1 + \sin t) 16}{\text{min}}$$

$$m_{out} = \frac{30 \text{ gal}}{1200 \text{ gal}} = 0.025 \text{ m}$$

$$\therefore \frac{dm}{dt} = m_{in} - m_{out}$$

$$\frac{dm}{dt} = 50(1 + \sin t) - 0.025m$$

$$\frac{dm}{dt} + 0.025m = 50(1 + \sin t)$$

Using Integrating Factor Method

$$P = 0.025 \quad \int P dt = 0.025t$$

$$\therefore IF = e^{0.025t}$$

$$\text{Sol } m(IF) = \int Q(IF) dt$$

$$m(e^{0.025t}) = \int 50(1 + \sin t)(e^{0.025t}) dt$$

Using integration by parts

Where $u = 1 + \sin t$ $dv = e^{0.025t}$

$du = \cos t$

$v = \frac{e^{0.025t}}{0.025}$

$$\therefore m(e^{0.025t}) = 50 \left[(1 + \sin t) \left(\frac{e^{0.025t}}{0.025} \right) - \int \frac{e^{0.025t}}{0.025} \cos t dt \right]$$

$$m(e^{0.025t}) = 50 \left[\frac{(1 + \sin t)(e^{0.025t})}{0.025} - \frac{1}{0.025} \int e^{0.025t} \cos t dt \right]$$

$$m(e^{0.025t}) = 2000(1 + \sin t)(e^{0.025t}) - \int 2e^{0.025t} \cos t \cdot dt$$

Applying integration by parts

$$u = \cos t$$

$$du = -\sin t$$

$$dv = e^{0.025t}$$

$$v = \frac{e^{0.025t}}{0.025}$$

$$m(e^{0.025t}) = 2000 \left[(1 + \sin t)(e^{0.025t}) - \left(\frac{\cos t \cdot e^{0.025t}}{0.025} - \int \frac{e^{0.025t}}{0.025} (-\sin t) dt \right) \right]$$

$$m(e^{0.025t}) = 2000 \left[(1 + \sin t)(e^{0.025t}) - \frac{(\cos t)(e^{0.025t})}{0.025} + \frac{1}{0.025} \int e^{0.025t} \sin t dt \right]$$

when simplified

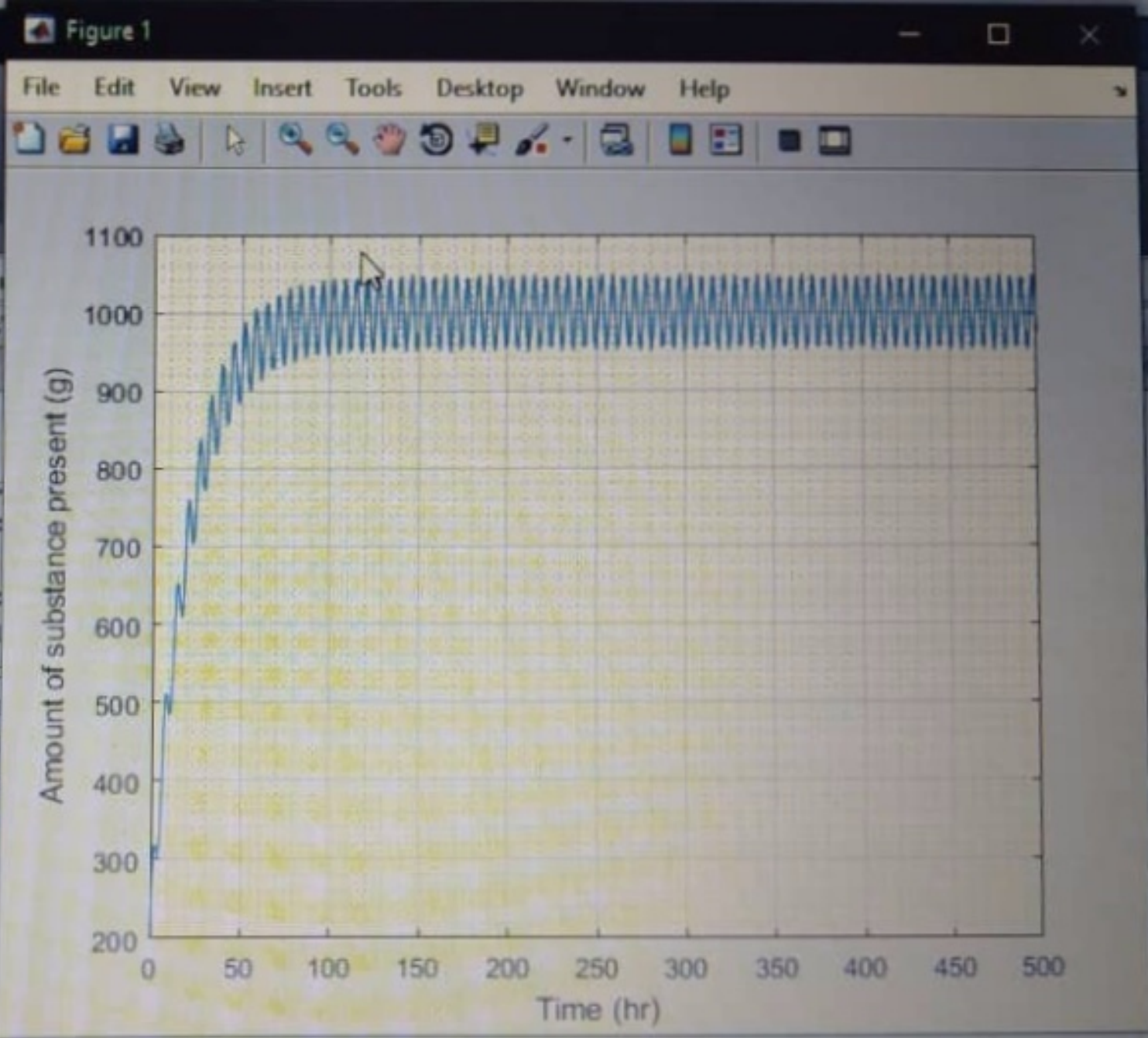
$$m(t) = \frac{2000}{4601} (\sin t - 400 \cos t + 1601) \frac{1800}{e^{0.025t}} \cdot 16$$

APPS EDITOR

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NAVIGATE EDIT

```
Program Files > MATLAB > R2018a > bin  
Editor - C:\Users\...  
LOLOLOL.m  
1 - clc  
2 - close  
3 - clearv  
4 - b=0:1:  
5 - tstep  
6 - t = 0:  
7 - x = ((  
8 - plot(t  
9 - xlabel  
10 - ylabel  
11 - grid o  
12 - grid m
```



Command Window

Column 481...rb rnvwb...501

```
1 - clc
2 - close all
3 - clearvars
4 - y=dsolve('Dy=50*(1+sin(t))-0.025*y','t')
5 - t=[0:0.5:7.5]
6 - ezplot(y,t)
7 - grid on
8 - grid minor
```

Command Window

y =

 $C2 \cdot \exp(-t/40) - (2000 \cdot 1601^{(1/2)} \cdot \cos(t + \text{atan}(1/40)))/1601 + 2000$

t =
fx
<

LOLOLOL.m X

MATeq1.m X

secondmodel.m X

dsolvee.m X

combined1.m X

plotofdsolve1.m

```
1 - clc
2 - close all
3 - clearvars
4 - b=0:1:500;
5 - tstep = rem(b,2)==0
6 - t = 0:tstep:500;
7 - x = ((1000)+(49.88)*(sin(t))+(2.49)*(cos(t))-802.49*exp(-0.05*t));
8 - plot(t,x)
9 - xlabel('Time (hr)')
10 - ylabel('Amount of substance present (g)')
11 - grid on
12 - grid minor
```

Command Window

Columns 481 through 501

1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0

LOLOLOL.m X

MATeq1.m X

secondmodel.m X

dsolvee.m X

combined1.m X

plotofdsolve1.m

```
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8 - plot(t,x)
9 - xlabel('Time (hr)')
10 - ylabel('Amount of substance present (g)')
11 - grid on
12 - grid minor
```

Command Window

Columns 481 through 501

1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0

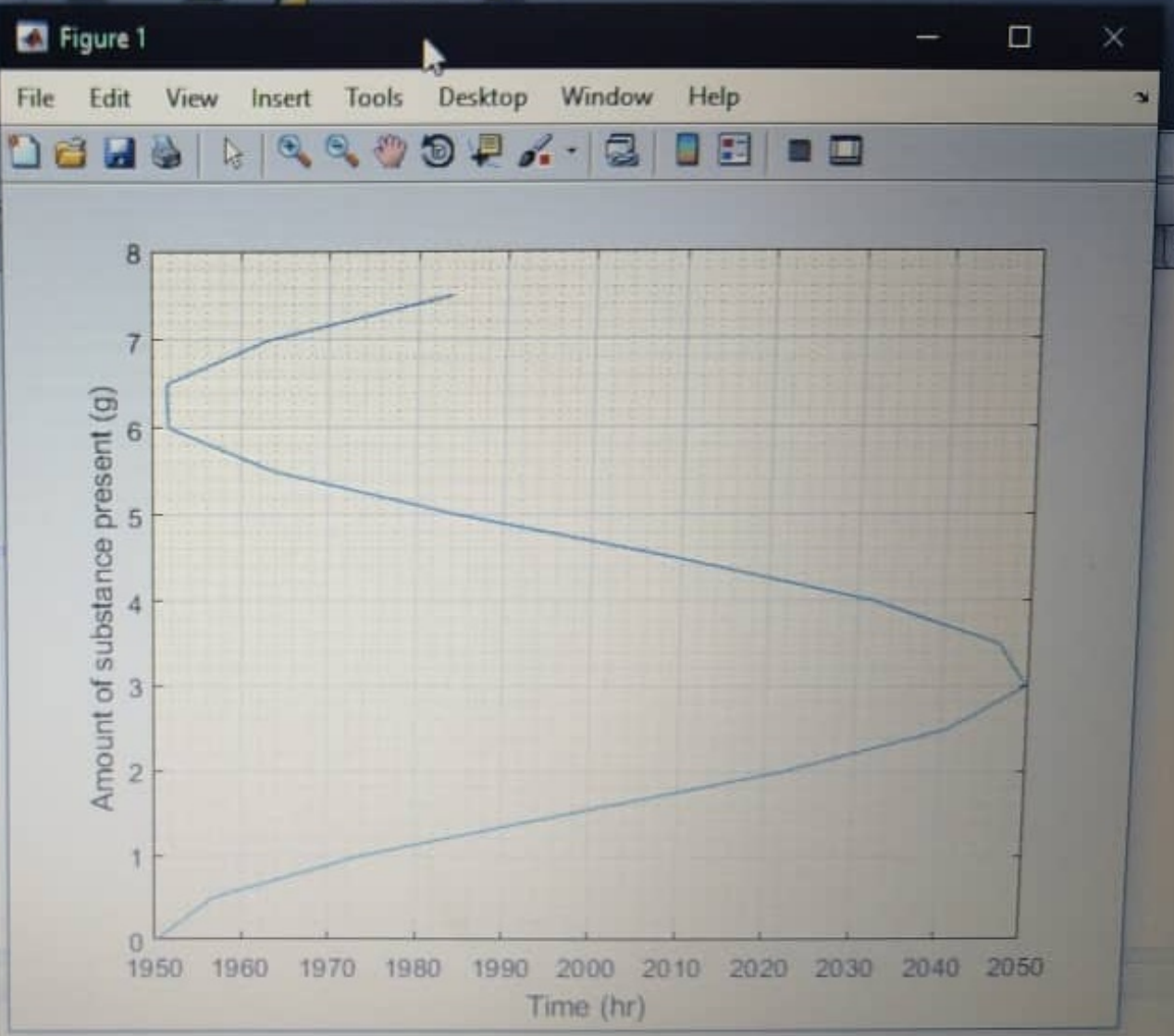
C:\Program Files\MATLAB\R2018a\bin\win64

Editor - C:\Users\EKOK NZIE\plotofds

LOLOLOL.m x MATEq1.m x

```

1 - clearvars
2 - clc
3 - close all
4 - t = 0:0.5:7.5;
5 - y = 0.0769*exp(-t/40)
6 - plot(y,t)
7 - xlabel('Time (hr)')
8 - ylabel('Amount of s
9 - grid on
10 - grid minor
    
```



Value
1x16 double
1x16 double

Command Window

Columns 1 through 12

1.9501 1.9568 1.9741 1.9978 2.0220 2.0409 2.0497 2.0464 2.0318 2.0094

Columns 13 through 16

1.9517 1.9515 1.9632 1.9639