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18/ENG06/015

Mechanical Engineering

ENG 282 (Engineering Math II)

1) Applying the balance law
Accumulation rate ~~of~~ input rate of salt - output
of salt

Salt within a system, denoting the amount of salt
present in the tank at any time (t) as y , its time
rate of change is given as,

$$\frac{dy}{dt} = y_{in} - y_{out}$$

Since, 50 gal of brine water the tanks per min
and one gallon contains (1 + 810t) lb of salt;

$$\text{At } t = 1, (1 + 810t) = (1 + 810(1)) = 1.02 \text{ lb}$$

Hence, the amount of salt entering into the tanks

$$50 \text{ gal/min} \times 1.02 \text{ lb/gal}$$

$$= 51 \text{ lb/min}$$

The tanks contains 1200 gal of water with
dissolved salt and 30 gal of the solution exist the
tanks per min 30 gal

$$1200 \text{ gal}$$

$$= -0.025\%$$

$$= 2.5\% \text{ of the content}$$

Therefore, 2.5% of the salt present in the salt
will leave the tanks per minute;

$$y_{out} = 2.8\% \text{ of } y$$

$$a) \frac{dy}{dt} \text{ lb/min} = 81 \text{ lb/min} - 2.8\% \text{ of } y \text{ lb/min}$$

$$b) \frac{dy}{dt} = 81 - 0.028y, \quad \frac{dy}{dt} = -0.028y + 81$$

$$\frac{dy}{dt} = -0.028 \left(\frac{-0.028y + 81}{-0.028y - 0.028} \right)$$

$$\frac{dy}{dt} = -0.028(y - 2040)$$

$$\frac{dy}{(y - 2040)} = -0.028 dt, \quad \int_{y-2040} dy = \int -0.028 dt$$

$$\int \frac{dy}{(y - 2040)} = -0.028 \int dt; \quad \ln(y - 2040) = -0.028t + c$$

$$y - 2040 = e^{-0.028t + c}$$

$$; y - 2040 = e^{-0.028t} e^c$$

$$y - 2040 = e^{-0.028t}$$

$$y_0; y - 2040 = y_0 e^{-0.028t}$$

$$y = y_0 e^{-0.028t}$$

$$+ 2040; \text{ initially, when } t = 1,$$

$$y = 180 \text{ lb}$$

$$180 = y_0 e^{-0.028t}$$

$$+ 2040; 180 - 2040 = y_0 x$$

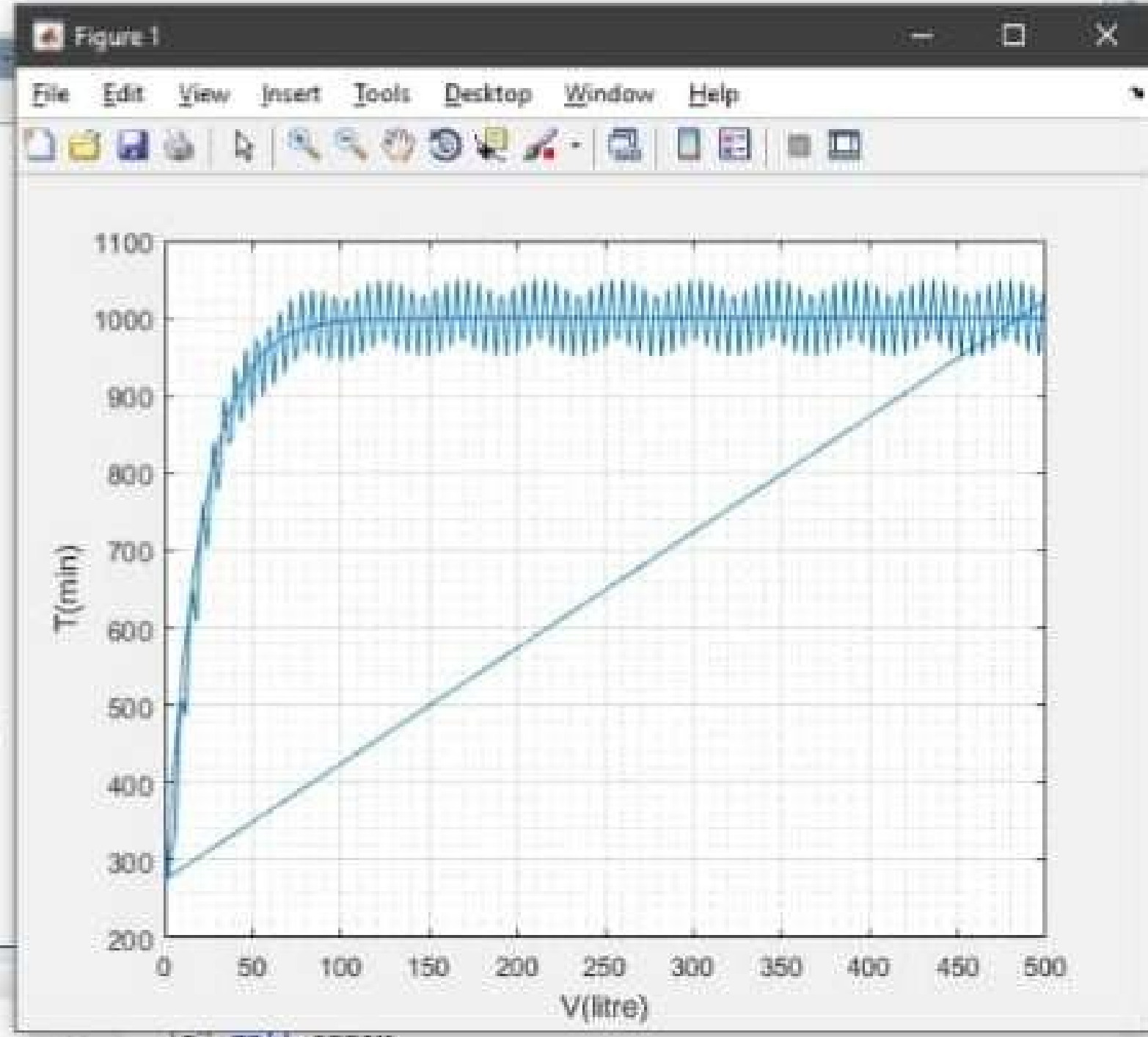
$$y_0 = -1890$$

so,

$$y = -1890 e^{-0.028t} + 2040$$

$$y = 2040 - 1890 e^{-0.028t}$$

```
1 - commandwindow
2 - clear
3 - cloc
4 - close all
5 - ta=2:2:500
6 - tb=1:2:500
7 - y=(50/0.05)+((50/1.0025)*sin(tb))+(((50*0.05)/(1.0025))*cos(tb))-802.49*exp(-0.05*tb)
8 - ym=1000-(800*exp(-0.05*ta))
9 - yg=[y ym]
10 - tg=[ta tb]
11 - plot (tg,yg)
12 - grid on
13 - grid minor
14 - xlabel ('V(litre)')
15 - ylabel ('T(min)')
16 - col_header={'t (min)', 'v(litre)'}
17 - xlswrite('C:\Users\Seyitan\Documents\MATLAB\odevbesdata.xlsx',[tg(:),yg(:)],'veriler','A2')
18 - xlswrite('C:\Users\Seyitan\Documents\MATLAB\odevbesdata.xlsx',col_header,'veriler','A1')
```



Current Folder

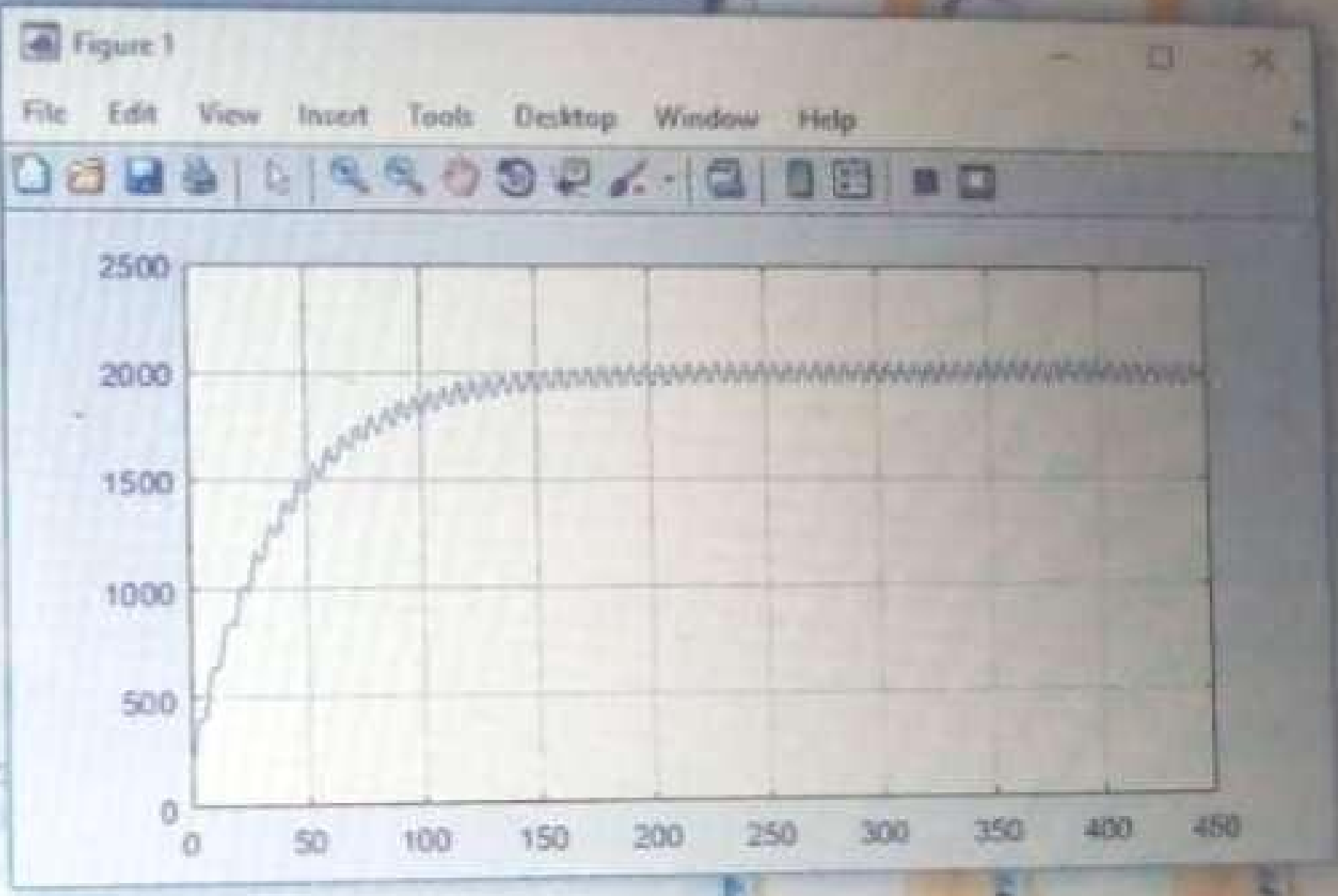
Name

Workspace

Name	Value
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```
l = cell array
    {'t (min)'} {'v(litre)'}
>>
```

```
1 - commandwindow
2 - clear
3 - clc
4 - close all
5 - syms m t
6 - ans=dsolve('Dm+0.025*m=50+50*sin(t)', 'm(0)=150')
7 - t=0:0.5:450
8 - tns=subs(ans,t)
9 - plot(t,tns)
10 - grid on
```



Command Window

```
tns =
[ 150, 2000 - (2000*1601^(1/2)*cos(atan(1/40) + 1/2))/1601 - (2881850*exp(-1/80))/1601, 2000]
```