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18/ENG08/010
BIOMEDICAL ENGINEERING
ENGINEERING MATHEMATICS
ENG 282

$$\frac{dy}{dt} = y_{in} - y_{out}$$

$$\frac{dy}{dt} = 50(1 + \sin t) - 2.5\% \text{ of } y$$

$$\frac{dy}{dt} = 50(1 + \sin t) - 0.025y$$

$$\Rightarrow \frac{dy}{dt} + 0.025y = 50(1 + \sin t)$$

$$1 + 0.025y \, dy = 50(1 + \sin t) \, dt$$

$$\frac{dy}{dt} = 50(1 + \sin t) - 0.025y$$

$$\therefore \frac{dy}{dt} + 0.025y = 50(1 + \sin t)$$

We use Linear equation Method;

$$\frac{dy}{dx} + Py = Q$$

$$\therefore P = 0.025, Q = 50(1 + \sin t)$$

$$\therefore \int P \cdot dt = \int 0.025 \, dt$$

$$= e^{0.025t}$$

$$= e^{0.025t}$$

$$\therefore y + IF = \int Q \cdot IF \cdot dt$$

$$y e^{0.025t} = \int 50(1 + \sin t) e^{0.025t} \, dt$$

$$y e^{0.025t} = 50 \int (1 + \sin t) e^{0.025t} \, dt$$

$$y e^{0.025t} = 50 \int e^{0.025t} + e^{0.025t} \sin t \cdot dt$$

$$y e^{0.025t} = 50 \int e^{0.025t} \cdot dt + \int e^{0.025t} \sin t \cdot dt$$

$$y e^{0.025t} = 50 \cdot \frac{e^{0.025t}}{0.025} + \int e^{0.025t} \sin t \cdot dt + C$$

$$\int e^{0.025t} \sin t \cdot dt$$

$$u = e^{0.025t}$$

$$dv = \sin t$$

$$du = 0.025 e^{0.025t}$$

$$v = -\cos t$$

$$\therefore \int e^{0.025t} \sin t = e^{0.025t} (-\cos t) - \int -\cos t \cdot 0.025 e^{0.025t}$$

$$\int e^{0.025t} \sin t = -e^{0.025t} \cos t - \int -\cos t \cdot 0.025 e^{0.025t} + C$$

$$\int e^{0.025t} \sin t = -e^{0.025t} \cos t + 0.025 \int e^{0.025t} \cos t + C$$

Using integration by part,

$$\int u dv = uv - \int v du$$

$$u = e^{0.025t} \quad dv = \cos t$$

$$du = 0.025 e^{0.025t} \quad v = \sin t$$

$$= e^{0.025t} \cos t + 0.025 \left[e^{0.025t} \sin t - \int \sin t \cdot 0.025 e^{0.025t} \right]$$

$$= -e^{0.025t} \cos t + 0.025 \left[e^{0.025t} \sin t - 0.025 \int \sin t e^{0.025t} \right]$$

$$\text{Let } Q = \int e^{0.025t} \sin t$$

$$\therefore Q = -e^{0.025t} \cos t + 0.025 \left[e^{0.025t} \sin t - 0.025 Q \right]$$

$$Q + 6.25^{-4} Q = e^{0.025t} \cos t + 0.025 e^{0.025t} \sin t$$

$$Q \cdot 0.000625 Q = -e^{0.025t} \cos t + 0.025 e^{0.025t} \sin t$$

$$1.000625 Q = -e^{0.025t} \cos t + 0.025 e^{0.025t} \sin t$$

$$Q = \frac{-e^{0.025t}}{1.000625} (\cos t - 0.025 \sin t) + C$$

$$Q = \frac{-e^{0.025t}}{1.000625} (\cos t - 0.025) + C$$

$$\int e^{0.025t} \sin t = \frac{-e^{0.025t}}{1.000625} (\cos t - 0.025) + C$$

$$\int e^{0.025t} \sin t = \frac{-e^{0.025t}}{1.000625} (\cos t - 0.025) + C$$

$$\therefore ye^{0.025t} = 50 \left[\frac{e^{0.025t}}{0.025} - \frac{e^{0.025t}}{1.000625} (\cos t - 0.025) + C \right]$$

$$ye^{0.025t} = 2000 e^{0.025t} - 50 \cdot \frac{e^{0.025t}}{1.000625} (\cos t - 0.025) + 50C$$

$$y = 2000 \frac{-50}{1.000625} (\cos t - 0.025) + \frac{50C}{e^{0.025t}}$$

$$y = 2000 \frac{-50}{1.000625} (\cos t - 0.025 \sin t) + \frac{50C}{e^{0.025t}}$$

when $y = 150$

$t = 0$

$$150 = 2000 \frac{-50}{1.000625} (1 - 0) + \frac{50C}{1}$$

$$150 = 2000 - 49.968(1) + 50C$$

$$150 = 1950.032 + 50C$$

$$-1850.032 = 50C$$

$$C = -36.00064$$





