





(Q3)

Using integration by parts

$$u = e^{0.02t}, \quad dv = \sin t \quad du = 0.02e^{0.02t}, \quad v = -\cos t$$

$$\int u \, dv = uv - \int v \, du$$

$$\int \sin t e^{0.02t} = 0.02e^{0.02t}(-\cos t) - \int -\cos t (0.02e^{0.02t})$$

$$= -0.02e^{0.02t} \cos t + 0.02 \int e^{0.02t} \cos t$$

$$\int e^{0.02t} \cos t =$$

$$u = e^{0.02t}, \quad dv = \cos t, \quad du = 0.02e^{0.02t}, \quad v = \sin t$$

$$\int e^{0.02t} \cos t = e^{0.02t} \sin t - \int \sin t (0.02e^{0.02t})$$

$$\int \sin t e^{0.02t} = e^{0.02t} + 0.02e^{0.02t} \sin t - 0.00062e^{0.02t} \sin t$$

$$\sin t e^{0.02t}$$

Using the integral or $\int e^{0.02t} \sin t$

$$I = -e^{0.02t} \cos t + 0.02e^{0.02t} - 0.00062e^{0.02t} I$$

$$1.00062I = e^{0.02t} (-0.02 \sin t - \cos t) + C$$

$$I = \frac{e^{0.02t}}{1.00062} (-0.02 \sin t - \cos t) + C$$

$$50 \int \sin t e^{0.02t} = 50 \left[\frac{e^{0.02t}}{1.00062} (-0.02 \sin t - \cos t) + C \right]$$

O SARO 181416 OMLA PRO
CHEMICAL ENGINEER

Sgn = ~~100%~~

GALLON of water = 200 gal

Amount of salt dissolved = 150 lbs

Initial rate of brine = 5 gal

Output rate = 20 gal

$$\frac{dm}{dt} = M_{in} - M_{out} ; M_{in} = \frac{50 \text{ gal}}{200 \text{ gal}} \times (1 + S_{nt})$$
$$= 50(1 + S_{nt}) \text{ lbs/min}$$

$$M_{out} = \frac{30}{1200} = 0.025 = 25\% \text{ of } M$$

$$\frac{dm}{dt} = 50(1 + S_{nt}) - 0.025m$$

$$\frac{dm}{dt} + 0.025m = 50(1 + S_{nt})$$

Using integration by parts ($\int dy/dx + P_y = Q$)

$$P \cdot dm/dt + P_m = Q$$

$$P = 0.025, Q = 50(Ct + S_{nt})$$

$$\int P dt = \int 0.025 dt = 0.025t ; \text{ If } F = e^{\int P dt} = e^{0.025t}$$

$$M \cdot I \cdot F = \int Q \cdot F dt$$

$$M \cdot e^{0.025t} = \int 50(1 + S_{nt}) e^{0.025t} dt$$

$$M \cdot e^{0.025t} = \int (50 + 50S_{nt}) \cdot e^{0.025t} dt$$

$$M \cdot e^{0.025t} = \frac{50e^{0.025t}}{0.025} + \int 50S_{nt} e^{0.025t}$$

100% 100% 100%