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DEPT: Civil Engineering

1) Using 'balance law'; the acceleration rate of salt within system is equal to the input rate of salt into the system minus the output rate of salt from the system. ∴

Acceleration rate of Salt within system =

input rate of salt into the system

∴ output rate of salt from outside the system =
 net amount of salt present in the tank at any time t be 'y'; time rate of change

$$\frac{dy}{dt} = y_{in} - y_{out}$$

∴ $\frac{dy}{dt}$ is the rate of change of salt entering into the tank minus the rate of salt leaving the tank

$$\frac{dy}{dt} = 100 - (10 + 5y) = 90 - 5y$$

Hence, the amount of salt entering into

$$\frac{dy}{dt} = 90 - 5y$$

$$\int \frac{dy}{90 - 5y} = \int \frac{dt}{1}$$

$$-\frac{1}{5} \ln|90 - 5y| = t + C$$

$$\ln|90 - 5y| = -5t - 5C$$

$$90 - 5y = e^{-5t - 5C}$$

$$90 - 5y = e^{-5t} \cdot e^{-5C}$$

$$90 - 5y = e^{-5t} \cdot K$$

$$5y = 90 - K e^{-5t}$$

$$y = 18 - \frac{K}{5} e^{-5t}$$

$$y = 18 - A e^{-5t}$$

The tank contains 120 gal. of water with dissolved salt and 30 gal. of solution exits on the other side. If 30 gal

- 0.625 · 20% = or content on the same
 So 25% on the salt present inside. On
 tank now also runs the same formula

$$H \cdot x_{\text{out}} = 2.5x + 20y$$

a) $\frac{dy}{dt} \cdot 15/\text{min} = 511/\text{min} - 25x - y/\text{min}$

b) $\frac{dy}{dt} = 51 - 0.025y$ $\frac{dy}{dt} = 0.025y + 51$

$$\frac{dy}{dt} = 0.025 \left(\frac{-0.025x + 51}{-0.025} - 0.025 \right) \cdot \frac{dy}{dt} =$$

$$0.02 \cdot (y - 2040)$$

$$\frac{dy}{y - 2040} = -0.025 dt; \int \frac{dy}{y - 2040} = \int -0.025 dt$$

$$\frac{dy}{dy-2040} = -0.025 \int dt ; \ln(y-2040) = 0.025 t$$

$$y - 2040 = e^{-0.025 t - 1} ; y = 2040 = e^{-0.24} e^c$$

$$y = 2040 = e^{-0.025 t} ; y = 2040 = y_0 e^{-0.025 t}$$

$$y = y_0 e^{-0.025 t} ; y_0, y - 2040 = y_0 e^{-0.025 t}$$

$$y = y_0 e^{-0.025 t} + 2040 ; \text{Initially when } t=1$$

$$y = 15010 ;$$

$$150 = y_0 e^{-0.025 t} + 2040 ; 150 - 2040 = y_0$$

$$y = -1890$$

$$50 ;$$

$$y = 1890 e^{-0.025 t} + 2040 = y = \underline{\underline{2040 - 180 e^{-0.025 t}}}$$