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 MATRIC No: 19/ENGG04/015 SERIAL NUMBER: 19
 MATHEMATICS ASSIGNMENT

(1) $y = (2\cos 3x)/x^3$
 $\frac{dy}{dx} = \frac{u \cdot \frac{dv}{dx} - v \cdot \frac{du}{dx}}{v^2}$

$u = 2\cos 3x$ $v = x^3$
 $\frac{du}{dx} = -6\sin 3x$ $\frac{dv}{dx} = 3x^2$

$\frac{dy}{dx} = \frac{(x^3)(-6\sin 3x) - (2\cos 3x)(3x^2)}{(x^3)^2}$
 $= \frac{-6x^3 \sin 3x - 6x^2 \cos 3x}{x^6} = -\frac{6x^2(x \sin 3x + \cos 3x)}{x^6}$
 $= -\frac{6(x \sin 3x + \cos 3x)}{x^4}$

$\frac{dy}{dx} = \frac{(x^3)(-6\sin 3x) - (2\cos 3x)(3x^2)}{(x^3)^2}$
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(2) $y = xe^{2x}$
 $u = x$ $v = e^{2x}$
 $\frac{du}{dx} = 1$ $\frac{dv}{dx} = 2e^{2x}$

$\frac{dy}{dx} = u \cdot \frac{dv}{dx} + v \cdot \frac{du}{dx}$

$\frac{dy}{dx} = 2xe^{2x} + e^{2x}$

$\frac{d^2 y}{dx^2} [2xe^{2x} + e^{2x}]$

$u = 2x$ $v = e^{2x}$
 $\frac{du}{dx} = 2$ $\frac{dv}{dx} = 2e^{2x}$

$\frac{d}{dx} [2xe^{2x}] = 4xe^{2x} + 2e^{2x}$
 $\frac{d}{dx} [e^{2x}] = 2e^{2x}$

$\frac{d^2 y}{dx^2} = 4xe^{2x} + 2e^{2x} + 2e^{2x} = 4xe^{2x} + 4e^{2x}$

$$d^2y/dx^2 - 4dy/dx + 4y = 0$$

$$= [4xe^{2x} + 4e^{2x}] - 4[2xe^{2x} + e^{2x}] + 4[xe^{2x}]$$

$$= 4xe^{2x} + 4e^{2x} - 8xe^{2x} - 4e^{2x} + 4xe^{2x}$$

$$= 4xe^{2x} - 8xe^{2x} + 4xe^{2x} + 4e^{2x} - 4e^{2x}$$

$$= \underline{\underline{0}}$$

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(4) $\frac{d}{dx} \frac{e^x \sin 2x}{dx} = u \cdot \frac{dv}{dx} + v \cdot \frac{du}{dx}$

$u = e^x$ $v = \sin 2x$
 $\frac{du}{dx} = e^x$ $\frac{dv}{dx} = 2\sin 2x$

$$\frac{dy}{dx} = (e^x)(2\sin 2x) + (\sin 2x)(e^x)$$

$$= 2e^x \sin 2x + e^x \sin 2x$$

$$= \underline{\underline{3e^x \sin 2x}}$$

(4) $\int e^x \sin 2x$

$\int u \cdot dv = uv - \int v \cdot du$

$u = \sin 2x$ $dv = e^x dx$
 $\frac{du}{dx} = 2\cos 2x$ $v = e^x$

$$\int e^x \sin 2x = e^x \sin 2x - \int 2e^x \cos 2x$$

$u = \cos 2x$ $dv = 2e^x$
 $\frac{du}{dx} = -2\sin 2x$ $v = 2e^x$

$$= e^x \sin 2x - [2e^x \cos 2x + \int 2e^x (-2\sin 2x)]$$

$$= e^x \sin 2x - 2e^x \cos 2x - \int 4e^x \sin 2x$$

Let $I = \int 4e^x \sin 2x$

Let $I = \int e^x \sin 2x dx$

$$I = e^x \sin 2x - 2e^x \cos 2x - 4I$$

$$5I = e^x \sin 2x - 2e^x \cos 2x$$

$$I = \frac{e^x \sin 2x - 2e^x \cos 2x}{5}$$

$$\therefore \int e^x \sin 2x = \frac{1}{5} \left[e^x \sin 2x - 2e^x \cos 2x \right] + C$$