

Oshibugie Mukhtar Oshichala

Computer Engineering

19/ENG02/058

$$1) y = \frac{(2 \cos 3x)}{x^3}$$

$$\ln y = \ln 2 \cos 3x - \ln x^3$$

$$\frac{d}{dx}(\ln y) = \frac{d}{dx}(\ln 2 \cos 3x) - \frac{d}{dx}(\ln x^3)$$

$$\frac{1}{y} \left(\frac{dy}{dx} \right) = \frac{1}{2} \cos 3x (-6 \sin 3x) - \frac{1}{x^3} (3x^2)$$

$$\frac{dy}{y} \cdot \frac{dy}{dx} = \frac{-6 \sin 3x}{2 \cos 3x} - \frac{3x^2}{x^3}$$

$$\frac{dy}{dx} = y \left(-3 \sin 3x / \cos 3x - \frac{3}{x} \right)$$

$$\frac{dy}{dx} = \frac{2 \cos 3x}{x^3} \left(-3 \sin 3x / \cos 3x - \frac{3}{x} \right)$$

$$2) y = x e^{2x} \quad u = x, \quad y = e^{2x}$$

$$\frac{dy}{dx} = u \frac{dv}{dx} + v \frac{du}{dx}$$

$$= x \frac{d e^{2x}}{dx} + e^{2x} \frac{dx}{dx}$$

$$= x \cdot e^{2x} \cdot 2 + e^{2x} \cdot 1$$

$$2x e^{2x} + e^{2x}$$

$$\frac{d^2 y}{dx^2} = 2x \frac{d e^{2x}}{dx} + e^{2x} \frac{d 2x}{dx} + \frac{d e^{2x}}{dx}$$

$$= 4x e^{2x} + 2e^{2x} + 2e^{2x}$$

$$= 4x e^{2x} + 4e^{2x}$$

$$\frac{d^2 y}{dx^2} = 4 \frac{dy}{dx} + 4y = 0$$

$$4x e^{2x} + 4e^{2x} - 4(2x e^{2x} + e^{2x}) + 4(x e^{2x})$$

$$4x e^{2x} + 4e^{2x} - 8x e^{2x} + 4e^{2x} + 4x e^{2x}$$

$$8x e^{2x} - 8x e^{2x} + 4e^{2x} - 4e^{2x} = 0$$

$$\frac{d^2 y}{dx^2} - 4 \frac{dy}{dx} + 4y = 0$$

3) Name: Oshibugie Mukhtar Oshiohala

Dept: Computer Engineering

Mat No: 19/ENG02/058

4) $\int e^x \sin 2x dx$

$$U = \sin 2x \quad dU = 2 \cos 2x dx$$

$$dU = 2 \cos 2x dx \quad V = e^x$$

$$\int U dV = UV - \int V dU$$

$$\sin 2x (e^x) - \int e^x 2 \cos 2x dx$$

$$e^x \sin 2x - \int e^x 2 \cos 2x dx$$

$$\int U = 2 \cos 2x \quad dU = -2 \sin 2x dx$$

$$[dU = -2 \sin 2x dx \quad V = e^x]$$

$$[2 \cos 2x (e^x) - \int e^x (-2 \sin 2x) dx]$$

$$[e^x 2 \cos 2x + 2 \sin 2x e^x dx]$$

$$e^x \sin 2x - e^x 2 \cos 2x - \int e^x 2 \sin 2x dx$$

$$\int e^x \sin 2x dx = e^x 2 \sin 2x - \int e^x 2 \cos 2x dx - \int e^x \sin 2x dx$$

$$\text{Let } I = \int e^x 2 \sin 2x dx$$

$$I = e^x 2 \sin 2x - e^x 2 \cos 2x - I$$

$$2I = e^x 2 \sin 2x - e^x 2 \cos 2x$$

$$I = \frac{e^x 2 \sin 2x - e^x 2 \cos 2x}{2}$$

$$\therefore \int e^x \sin 2x dx = \frac{1}{2} [e^x 2 \sin 2x - e^x 2 \cos 2x + C]$$