

ORAKPO MIRABEL

18/SCI01/074

$$A \begin{pmatrix} 1 & -3 \\ 6 & 0 \\ 4 & 2 \\ 2 & 0 \end{pmatrix} \quad B \begin{pmatrix} 1 & 1 \\ 2 & -2 \\ 1 & 1 \\ 1 & 1 \end{pmatrix} \quad C \begin{pmatrix} 0 & 4 \\ 3 & -7 \\ 6 & 1 \\ 1 & 1 \end{pmatrix}$$

## i. RANK OF A

$$|A| = \begin{pmatrix} 1 & -3 \\ 6 & 0 \\ 4 & 0 \\ 2 & 0 \end{pmatrix}$$

$$|A| = 1(0 - 10) + 3(4 - 16) + 6(20 - 0)$$

$|A| = -10 - 36 + 120 = 74$  IT IS NOT EQUAL TO 0; HENCE THE RANK OF A IS 3

## ii. RANK OF B TRANSPOSE

$$|B| = \begin{pmatrix} 1 & 1 \\ 0 & -2 \\ 1 & 1 \\ 2 & 1 \end{pmatrix}$$

$$|B| = 1(8 + 3) - 1(-4 - 6) + 0(1 + 4)$$

$|B| = 5 + 10 + 0 = 15$  IT IS NOT EQUAL TO 0; HENCE THE RANK OF B TRANSPOSE IS 3

## iii. RANK OF (A + C) TRANSPOSE

$$|A+C| = \begin{pmatrix} 1 & 1 \\ 9 & -7 \\ 10 & 1 \end{pmatrix}$$

$$|A+C|^T = \begin{pmatrix} 1 & 10 \\ 9 & \\ 1 & -7 \\ 2 & \end{pmatrix}$$

$$|A+C| = 1(-21 - 6) - 10(3 - 18) + 9(3 + 63)$$

$$|A+C| = -27 + 150 + 594 = 717$$

IT IS NOT EQUAL TO 0; HENCE THE RANK OF  $(A + C)$  TRANSPOSE IS 3

#### iv. RANK OF $(B + C)$

$$|B+C| = \begin{pmatrix} 1 & 5 \\ 5 & \\ 7 & -9 \\ 2 & \end{pmatrix}$$

$$|B+C| = 1(18 - 0) - 5(-14 - 2) + 5(0 + 9)$$

$$|B+C| = 18 + 80 + 45 = 143$$

IT IS NOT EQUAL TO 0; HENCE THE RANK OF  $(B + C)$  IS 3

#### v. RANK OF $(A+B+C)$

$$|A+B+C| = \begin{pmatrix} 2 & 2 \\ 11 & \\ 11 & -9 \\ 4 & \end{pmatrix}$$

$$|A+B+C| = 2(9 - 20) - 2(-11 - 36) + 11(55 + 81)$$

$$|A+B+C| = -22 + 94 + 1496 = 1568$$

IT IS NOT EQUAL TO 0; HENCE THE RANK OF  $(A+B+C)$  IS 3

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