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Mat 104 Assignment

①  $x^2 \sin x \, dx$

$$\int u \, dv = uv - \int v \, du \quad \dots (1)$$

for  $\int u \, dv = \int x^2 \sin(x) \, dx$

$$u = x^2 \quad \frac{du}{dx} = 2x$$

$$du = 2x \, dx$$

$$dv = \sin(x) \, dx$$

$$\int dv = \int \sin(x) \, dx$$

$$v = -\cos x$$

Substitute into (1)

$$\int x^2 \sin(x) \, dx = -x^2 \cos(x) - \int (-2x \cos(x)) \, dx$$

$$\int x^2 \sin(x) \, dx = -x^2 \cos(x) + 2 \int x \cos(x) \, dx \quad \dots (2)$$

$$u = x \Rightarrow \frac{du}{dx} = 1 \therefore du = dx$$

$$dv = \cos(x) \, dx \Rightarrow \int dv = \int \cos(x) \, dx$$

$$\int x \cos(x) \, dx = x \sin(x) - \int \sin(x) \, dx$$

Since  $\int \sin(x) \, dx = -\cos(x)$ , this becomes

$$\int x \cos(x) \, dx = x \sin(x) + \cos(x) \quad \dots (3)$$

$$\int x^2 \sin(x) \, dx = -x^2 \cos(x) + 2 \int x \cos(x) \, dx$$

Substitute (3) into (2)

$$\int x^2 \sin(x) \, dx = -x^2 \cos(x) + 2x \sin(x) + 2 \cos(x) + C$$

$$\textcircled{2} \int 3te^{2t} dt$$

$$\int u dv = uv - \int u du$$

$$\text{let } u = 3t$$

$$\frac{du}{dt} = 3, \quad du = 3 dt$$

$$\text{let } dv = e^{2t} dt$$

$$v = \frac{1}{2} e^{2t}$$

$$\begin{aligned} \int 3t(e^{2t}) dt &= 3t \left(\frac{1}{2}\right) e^{2t} - \int \frac{1}{2} e^{2t} 3 dt \\ &= \frac{3}{2} t e^{2t} - \frac{3}{4} e^{2t} \end{aligned}$$

$$\textcircled{3} \int 2x^2 \ln x dx$$

$$2 \int x^2 \ln(x) \times x^2 dx$$

$$\int u dv = uv - \int u du$$

$$u = \ln(x)$$

$$dv = x^2 dx$$

$$v = \int x^2 dx = \frac{x^3}{3}$$

$$2 \left( \ln(x) \times \frac{x^3}{3} - \int \frac{x^3}{3} \times \frac{1}{x} dx \right)$$

$$\int 2x^2 \ln x dx = 2 \left( \ln(x) \times \frac{x^3}{3} - \int \frac{x^2}{3} dx \right)$$

$$= \frac{2}{3} \left( \ln(x) \times x^3 - \frac{1}{3} \int x^2 dx \right)$$

$$\int x^2 dx = \frac{x^{2+1}}{2+1}$$

$$= \frac{x^3}{3}$$

$$= \frac{2}{3} \left( \ln(x) \times \frac{x^3}{3} - \frac{1}{3} \times \frac{x^3}{3} \right)$$

$$= \frac{2x^3 \times \ln(x)}{3} - \frac{2x^3}{9}$$

$$\therefore \int 2x^2 \ln x dx = \frac{2x^3 \times \ln(x)}{3} - \frac{2x^3}{9} + C$$

$$\textcircled{4} \int \frac{2x - 3x^2}{1-x} dx$$

$$\int \frac{2x}{1-x} - \frac{3x^2}{1-x} dx$$

$$\int f(x) + g(x) dx = \int f(x) dx + \int g(x) dx$$

$$\therefore \int \frac{2x}{1-x} dx - \int \frac{3x^2}{1-x} dx$$

$$2 - 2x - 2 \ln |1-x| + \frac{-9 + 6x + 3}{2} + 3 \ln |1-x|$$

$$= \frac{-5 + 2x + 3x^2}{2} + \ln |1-x|$$

$$\therefore \int \frac{2x - 3x^2}{1-x} dx = \frac{-5 + 2x + 3x^2}{2} + \ln |1-x| + C$$