

ERFH ISAIHA UREDO

19/ENG02/017

Computer Engineering

11) $y = (2 \cos 3x) / x^3$

$$\ln y = \ln 2 \cos 3x - \ln x^3$$

$$d/dx(\ln y) = d/dx(\ln 2 \cos 3x) - d/dx(\ln x^3)$$

$$\frac{1}{y} \left(\frac{dy}{dx} \right) = \frac{1}{2 \cos 3x} (-6 \sin 3x) - \frac{1}{x^3} (3x^2)$$

$$\frac{dy}{y} \cdot \frac{dy}{dx} = \frac{-6 \sin 3x}{2 \cos 3x} - \frac{3x^2}{x^3}$$

$$\frac{dy}{dx} = y \left(-3 \sin 3x / \cos 3x - \frac{3}{x} \right)$$

$$\frac{dy}{dx} = \frac{2 \cos 3x}{x} \left(-3 \sin 3x / \cos 3x - \frac{3}{x} \right)$$

2) $y = x e^{2x}$ $u = x, \quad v = e^{2x}$

$$\frac{dy}{dx} = u \frac{dv}{dx} + v \frac{du}{dx}$$

$$= x \frac{d e^{2x}}{dx} + e^{2x} \frac{dx}{dx}$$

$$= x \cdot e^{2x} \cdot 2 + e^{2x} \cdot 1$$

$$= 2x e^{2x} + e^{2x}$$

$$\frac{d^2 y}{dx^2} = 2x \frac{d e^{2x}}{dx} + e^{2x} \frac{d 2x}{dx}$$

$$+ \frac{d e^{2x}}{dx}$$

$$= 4x e^{2x} + 2e^{2x} + 2e^{2x}$$

$$= 4x e^{2x} + 4e^{2x}$$

$$\frac{d^2 y}{dx^2} = 4 \frac{dy}{dx} + 4y = 0$$

$$4x e^{2x} + 4e^{2x} - 4(2x e^{2x} + e^{2x}) + 4(x e^{2x})$$

$$4x e^{2x} + 4e^{2x} - 8x e^{2x} + 4e^{2x} + 4x e^{2x}$$

$$8x e^{2x} - 8x e^{2x} + 4e^{2x} - 4e^{2x} = 0$$

$$\frac{d^2 y}{dx^2} - 4 \frac{dy}{dx} + 4y = 0$$

3) EREH ISHITH UBEDD

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COMPUTER ENGINEERING

$$4 \int e^x \sin 2x \, dx$$

$$u = \sin 2x \quad dv = e^x$$

$$du = 2 \cos 2x \, dx \quad v = e^x$$

$$\int u \, dv = uv - \int v \, du$$

$$\sin 2x (e^x) - \int e^x 2 \cos 2x \, dx$$

$$e^x \sin 2x - \int e^x 2 \cos 2x \, dx$$

$$u = 2 \cos 2x \quad dv = e^x$$

$$du = -2 \sin 2x \, dx \quad v = e^x$$

$$\int 2 \cos 2x (e^x) - \int e^x (-2 \sin 2x)$$

$$\int e^x 2 \cos 2x + 2 \sin 2x e^x \, dx$$

$$e^x \sin 2x - e^x 2 \cos 2x - \int e^x 2 \sin 2x \, dx$$

$$\int e^x \sin 2x \, dx = e^x 2 \sin 2x - \int e^x 2 \cos 2x -$$

$$\int e^x 2 \sin 2x$$

$$\text{Let } K = \int e^x 2 \sin 2x \, dx$$

$$K = e^x 2 \sin 2x - e^x 2 \cos 2x - K$$

$$2K = e^x 2 \sin 2x - e^x 2 \cos 2x$$

$$K = \frac{e^x 2 \sin 2x - e^x 2 \cos 2x}{2}$$

$$\therefore \int e^x \sin 2x \, dx = \frac{1}{2} [e^x 2 \sin 2x - e^x 2 \cos 2x]$$