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COMPUTER SCIENCE

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~~CSE 10~~ MAT 102

1 $M = p_i - 6j - 3k$

$$N = 4i + 3j - k$$

$$O = i - 3j + 2k$$

a M & N are perpendicular

$$M \cdot N = (p_i - 6j - 3k) \cdot (4i + 3j - k)$$

$$= 4p - 18 + 3$$

$$= 4p - 15$$

Since they are perpendicular

$$4p - 15 = 0$$

$$\frac{4p}{4} = \frac{15}{4}$$

$$p = 15/4$$

b M, N and O are coplanar

$$M \cdot (N \times O) = \begin{vmatrix} p & -6 & -3 \\ 4 & 3 & -1 \\ 1 & -3 & 2 \end{vmatrix}$$

$$= p \begin{vmatrix} 3 & 1 \\ -3 & 2 \end{vmatrix} + 6 \begin{vmatrix} 4 & -1 \\ 1 & -2 \end{vmatrix} - 3 \begin{vmatrix} 4 & 3 \\ 1 & -3 \end{vmatrix}$$

$$p(6-3) + 6(8+1) - 3(12-3)$$

$$= 3p + 6(9) - 3(9)$$

$$= 3p + 54 + 45 = 0$$

$$= 3p + 99 = 0$$

$$\frac{3p}{3} = \frac{-99}{3}$$

$$p = -33$$

2 $\vec{r} = (3i + 2j + 5k) + (2i - j + 6k) + (5i + 2j - 3k)$

$$\vec{r} = 10i + 3j + 8k$$

$$a_x = 10, a_y = 3 \text{ and } a_z = 8$$

$$\begin{aligned}
 |V| &= \sqrt{10^2 + 3^2 + 8^2} \\
 &= \sqrt{100 + 9 + 64} \\
 &= \sqrt{173} = 13.15
 \end{aligned}$$

1 The direction of wires are

$$\cos \alpha = \frac{a_x}{|V|} = \frac{10}{13.15} = 0.761$$

$$\cos \beta = \frac{a_y}{|V|} = \frac{3}{13.15} = 0.228$$

ii Unit vector

$$e_V = \frac{V}{|V|} = \frac{10i + 3j + 8k}{13.15}$$

$$3 F = 3ui + u^2j + (u+2)k$$

$$v = 2vi - 3uj + (u-2)k$$

$$(F \times v) = \begin{vmatrix} i & j & k \\ 3u & u^2 & (u+2) \\ 2u & -3v & (u-2) \end{vmatrix}$$

$$= i \begin{vmatrix} u^2 & (u+2) \\ -3u & (u-2) \end{vmatrix} - j \begin{vmatrix} 3u & (u+2) \\ 2u & (u-2) \end{vmatrix} + k \begin{vmatrix} 3u & -u^2 \\ 2u & -3v \end{vmatrix}$$

$$= i [u^2(u-2) - (-3u(u+2))] - j [3u(u-2)] - 2u(u+2) + k(8u^2 - 2u^2)$$

$$= i [u^3 - 2u^2] - [3u^2 - 6u] - j [3u^2 - 6u - 2u^2 - 4u] + k [-2u^3 - 9u^2]$$

$$= i [u^3 - 2u^2 + 3u^2 + 6u] - j [u^2 - 10u] + k [-2u^3 - 9u^2]$$

$$= i [u^3 + u^2 + 6u] - j [u^2 - 10u] + k [-2u^3 - 9u^2]$$

$$\int (F \times v) = \int i [u^3 + u^2 + 6u] - \int j [u^2 - 10u] + \int k [-2u^3 - 9u^2]$$

$$= i \int u^3 + u^2 + 6u - \int u^2 - 10u + k \int -2u^3 - 9u^2$$

$$= \left[\frac{u^4}{4} + \frac{u^3}{3} + \frac{6u^2}{2} \right] - j \left[\frac{u^3}{3} - \frac{10u^2}{2} \right] + k \left[\frac{-2u^4}{4} - \frac{9u^3}{3} \right] + C$$

$$\vec{f} \times \vec{v} = i \left[\frac{(1)^4}{4} + \frac{(1)^3}{3} + 3(1)^2 \right] - j \left[\frac{(1)^3}{3} - 5(1)^2 \right] + k \left[-\frac{(1)^4}{2} - 3(1)^3 \right] + c - [0+0]$$

$$\vec{f} \times \vec{v} = i \left[\frac{1}{4} + \frac{1}{3} + 3 \right] - j \left[\frac{1}{3} - 5 \right] + k \left[-\frac{1}{2} - 3 \right] + c$$

$$\vec{f} \times \vec{v} = i \left[\frac{43}{12} \right] - j \left[-\frac{14}{3} \right] + k \left[-\frac{7}{2} \right]$$

$$\vec{f} \times \vec{v} = \frac{43}{12} i + \frac{14}{3} j - \frac{7}{2} k$$