

$$3) F = -3u\mathbf{i} + u^2\mathbf{j} + (u+z)\mathbf{k}$$

$$u = 2u\mathbf{i} - 3u\mathbf{j} + (u-z)\mathbf{k}$$

$$(F \times u) = \begin{vmatrix} -3u & u^2 & (u+z) \\ 2u & -3u & (u-z) \end{vmatrix}$$

$$= \mathbf{i} \begin{vmatrix} u^2 & (u+z) \\ -3u & (u-z) \end{vmatrix} - \mathbf{j} \begin{vmatrix} -3u & (u+z) \\ 2u & (u-z) \end{vmatrix} + \mathbf{k} \begin{vmatrix} -3u & u^2 \\ 2u & -3u \end{vmatrix}$$

$$= \mathbf{i} [u^2(u-z) - [-3u(u+z)]] - \mathbf{j} [3u(u-z)] - 2u(u+z)\mathbf{k} + \mathbf{k} [-9u^2 - 2u^3]$$

$$= \mathbf{i} [u^3 - zu^2 - [-3u^2 - 6u]] - \mathbf{j} [3u^2 - 6u - 2u^2 - 2u] + \mathbf{k} [-2u^3 - 9u^2]$$

$$= \mathbf{i} [u^3 - zu^2 + 3u^2 + 6u] - \mathbf{j} [u^2 - 10u] + \mathbf{k} [-2u^3 - 9u^2]$$

$$\int \cdot (F \times u) = \int_1^2 [u^3 + u^2 + 6u] - \int_1^2 [u^2 - 10u] + \int_1^2 k [-2u^3 - 9u^2]$$

$$= \int_1^2 [u^3 + u^2 + 6u] - \int_1^2 [u^2 - 10u] + k \int_1^2 [-2u^3 - 9u^2]$$

$$= \left[\frac{u^4}{4} + \frac{u^3}{3} + \frac{3u^2}{1} \right] - \left[\frac{u^3}{3} - \frac{5u^2}{1} \right] + k \left[-\frac{2u^4}{4} - \frac{3u^3}{1} \right] + C$$

$$= \left[\frac{u^4}{4} + \frac{u^3}{3} + 3u^2 \right] - \left[\frac{u^3}{3} - 5u^2 \right] + k \left[-\frac{u^4}{2} - 3u^3 \right] + C$$

$$\int_0^1 (F \times u) = \left[\frac{(1)^4}{4} + \frac{(1)^3}{3} + 3(1)^2 \right] - \left[\frac{(1)^3}{3} - 5(1)^2 \right] + k \left[\frac{(1)^4}{2} - 3(1)^3 \right] + C - (0+C)$$

$$= \left[\frac{1}{4} + \frac{1}{3} + 3 \right] - \left[\frac{1}{3} - 5 \right] + k \left[\frac{-1}{2} - 3 \right] + C - C$$

$$= \left[\frac{43}{12} \right] - \left[\frac{-14}{3} \right] + k \left[\frac{-7}{2} \right]$$

$$\therefore \int_0^1 (F \times u) = \frac{43}{12} \mathbf{i} + \frac{14}{3} \mathbf{j} - \frac{7}{2} \mathbf{k}$$

Name: Darbek: ~~A~~ Ulkuoc Samuel

Department: Computer Science

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$$\begin{aligned} 1) \quad m &= p\mathbf{i} - 6\mathbf{j} - 3\mathbf{k} \\ n &= 4\mathbf{j} + 3\mathbf{k} - \mathbf{k} \\ o &= \mathbf{i} - 3\mathbf{j} + 2\mathbf{k} \end{aligned}$$

M and N are perpendicular to each other

$$\begin{aligned} m \cdot n &= (p\mathbf{i} - 6\mathbf{j} - 3\mathbf{k}) \cdot (4\mathbf{j} + 3\mathbf{k} - \mathbf{k}) \\ &= 4p - 18 + 3 \\ &= 4p - 15 \end{aligned}$$

Since they are perpendicular

$$\begin{aligned} 4p - 15 &= 0 \\ 4p &= 15 \\ p &= 15/4 \end{aligned}$$

$$b) \quad \bar{m} \cdot |\bar{n} \times \bar{o}|$$

$$|\bar{n} \times \bar{o}| = \begin{vmatrix} 4 & 3 & -1 \\ 1 & -3 & 2 \end{vmatrix}$$

$$= \mathbf{i}(6 - (-3)) - \mathbf{j}(8 - (-2)) + \mathbf{k}(-12 - (-3))$$

$$|\bar{n} \times \bar{o}| = 3\mathbf{i} - 8\mathbf{j} - 13\mathbf{k}$$

$$m \cdot |\bar{n} \times \bar{o}|$$

$$= (p\mathbf{i} - 6\mathbf{j} - 3\mathbf{k}) \cdot (3\mathbf{i} - 8\mathbf{j} - 13\mathbf{k})$$

$$= 3p - 48 + 45$$

$$3p - 48 + 45 = 0$$

$$3p = 3$$

$$p = 1$$

$$2. \quad \underline{V} = (3i + 2j + 5k) + (2i - j + 6k) + (5i + 2j - 3k)$$

$$\underline{V} = 10i + 3j + 8k$$

$a_x = 10, a_y = 3 \text{ and } a_z = 8$

$$|\underline{V}| = \sqrt{10^2 + 3^2 + 8^2}$$

$$= \sqrt{100 + 9 + 64}$$

$$= \sqrt{173} = 13.15$$

i) The direction cosines are

$$\cos \alpha = \frac{a_x}{|\underline{V}|} = \frac{10}{13.15} = 0.761$$

$$\cos \beta = \frac{a_y}{|\underline{V}|} = \frac{3}{13.15} = 0.228$$

$$\cos \gamma = \frac{a_z}{|\underline{V}|} = \frac{8}{13.15} = 0.608$$

ii) Unit Vector

$$\underline{e}_V = \frac{\underline{V}}{|\underline{V}|} = \frac{10i + 3j + 8k}{13.15}$$