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MECHANICS ENGINEERING
19 / ENVS 1020

D. Oyelami / Mr. Okunola's class

1. $x - y - 14 = 0$

$$x - y = 14$$

$$x = 14 + y \quad \text{--- (1)}$$

$$x^2 + y^2 - 6x + 8y = 0$$

By putting (1) in 1

$$(14 + y)^2 + y^2 - 6(14 + y) + 8y = 0$$

$$196 + 28y + y^2 + y^2 - 84 - 6y + 8y = 0$$

$$y^2 + y^2 + 8y - 6y + 28y + 196 - 84 = 0$$

$$2y^2 + 30y + 112 = 0 \quad \text{--- (2)}$$

$$y^2 + 15y + 56 = 0$$

$$(y + 7)(y + 8) = 0$$

$$y = -7$$

$$\text{or } y = -8$$

$$\text{if } y = -7$$

$$\text{or if } y = -8$$

$$x = 14 + -7$$

$$x = 14 + -8$$

$$x = 7$$

$$x = 6$$

The points of intersection are $(7, -7)$ & $(6, -8)$

2. $2x + y - 10 = 0$

~~$$x^2 + y^2 + 4x - 6y = 0$$~~

$$x^2 + y^2 + 4x - 6y = 0$$

$$y = 10 - 2x$$

By Substitution

$$x^2 + (10 - 2x)^2 + 4x - 6(10 - 2x) = 0$$

$$x^2 + (10-2x)^2 + 4x - 6(10-2x) = 0$$

$$x^2 + 100 - 40x + 4x^2 + 4x - 60 + 12x = 0$$

$$x^2 + 4x^2 - 40x + 4x + 12x + 100 - 60 = 0$$

$$5x^2 - 24x + 40 = 0$$

$$x = \frac{12}{5} + \frac{2\sqrt{14}}{5}i \quad \text{or} \quad x = \frac{12}{5} - \frac{2\sqrt{14}}{5}$$

Since the values of x are imaginary, ~~the~~ line does not intersect with the circle.

$$x - 5y - 2 = 0$$

$$x^2 + 25y^2 - 6xy - 16 = 0$$

$$x = 5y + 2 \quad \text{By substitution}$$

$$(5y+2)^2 + 25y^2 - 6(5y+2)y - 16 = 0$$

$$25y^2 + 20y + 4 + 25y^2 - 30y^2 - 12y - 16 = 0$$

$$25y^2 + 25y^2 + 30y^2 + 20y - 12y - 16 = 0$$

$$20y^2 + 8y - 12 = 0 \quad \text{Divide by 4}$$

$$5y^2 + 2y - 3 = 0$$

$$(5y-3)(y+1) = 0$$

$$y = 3/5 \quad \text{or} \quad y = -1$$

$$\text{If } y = 3/5$$

$$x = 5(3/5) + 2$$

$$x = 3 + 2 = 5$$

$$\text{If } y = -1$$

$$x = 5(-1) + 2$$

$$x = -5 + 2 = -3$$