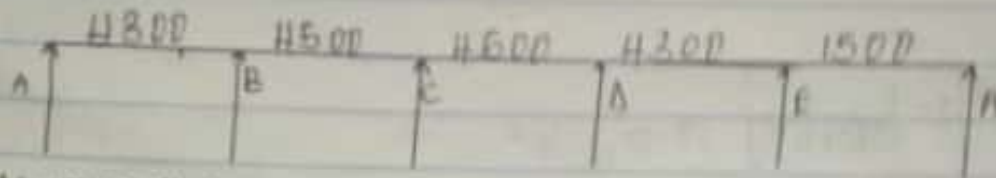


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 17/ENG03/032
 CIVIL ENGINEERING
 STRUCTURAL DESIGN
 ASSIGNMENT 2

QUESTION ONE



Assuming thickness = 150mm = 0.15m
 $f_{cu} = 25 \text{ N/mm}^2$
 $f_y = 410 \text{ N/mm}^2$

slab loading

slab weight = $0.15 \times 24 = 3.6 \text{ kN/m}^2$
 partition = 1.0 kN/m^2
 finishes = 1.2 kN/m^2
 total G-k = 5.8 kN/m^2

$D.L = 1.4(5.8) + 1.46k + 1.60k$
 $D.L = 1.4(5.8) + 1.6(3.0)$
 $= 8.12 + 4.8 = 12.92 \approx 13 \text{ kN/m}^2$

Beam loading

self weight of beam = $0.225 \times 0.6 \times 24 = 3.24 \text{ kN/m}^2$
 finishes = 1.2 kN/m^2
 wall load = $3 \times 3.47 = 10.41 \text{ kN/m}^2$
 total G-k = 14.85 kN/m^2

$D.L = 1.4(6k)$
 $= 1.4(14.85)$
 $= 20.79 \text{ kN/m}^2$

Slab load on beam in distribution = $\frac{1}{2} w l_x (1 - \frac{1}{3} k)$

$$k = \frac{l_y}{l_x}$$

$$\frac{4300}{4000} = 1.075$$

$$\frac{4500}{4000} = 1.125$$

$$\frac{1}{2} \times 13 \times 4.3 \left[1 - \frac{1}{3} (1.075)^2 \right] = 19.89 \text{ kN/m}^2$$

$$\frac{1}{2} \times 13 \times 4.5 \left[1 - \frac{1}{3} (1.125)^2 \right] = 21.55 \text{ kN/m}^2$$

Slab load on beam in short direction = $\frac{1}{3} w l_x$

$$= \frac{1}{3} \times 13 \times 4.5 = 6.5 \text{ kN/m}^2$$

$$\begin{aligned} \text{Total load} &= 19.89 + 20.79 = 40.68 \text{ kN/m} \\ &= 21.55 + 20.79 = 42.34 \text{ kN/m} \\ &= 6.5 + 20.79 = 27.29 \text{ kN/m} \end{aligned}$$

Distribution factor

$$K_{AB} = 1$$

$$K_{BA} = \frac{\frac{1}{l_{AB}}}{\frac{1}{l_{AB}} + \frac{1}{l_{BC}}} = \frac{\frac{1}{4.3}}{\frac{1}{4.3} + \frac{1}{4.5}} = 0.51$$

$$K_{BC} = 1 - 0.51 = 0.49$$

$$K_{CB} = \frac{\frac{1}{4.5}}{\frac{1}{4.5} + \frac{1}{4.5}} = 0.5$$

$$\begin{aligned} K_{CD} &= 1 - 0.5 \\ &= 0.5 \end{aligned}$$

$$K_{DC} = 0.49$$

$$K_{DE} = 0.51$$

$$K_{ED} = \frac{1}{4.3} = 0.26$$

$$\frac{1}{4.3} + \frac{1}{1.5}$$

$$K_{EA} = 1 - 0.26 = 0.74$$

$$K_{AE} = 1$$

F.E.M

$$UDL = \frac{w l^2}{12}$$

$$1) \frac{40.68 \times 4.3^2}{12} = 62.68 \text{ kN/m}$$

$$2) \frac{42.34 \times 4.5^2}{12} = 71.45 \text{ kN/m}$$

$$3) \frac{27.29 \times 1.5^2}{12} = 5.12 \text{ kN/m}$$

	A		B		BC		D		E		A
	A AB	BA BC	CB CD	DC DE	ED EA	EA A	AE A				
DF	0	0.51	0.49	0.5	0.5	0.49	0.51	0.26	0.74	1	0
FEM	-62.68	62.68	-71.45	71.45	-71.45	71.45	-62.68	62.68	-5.1	5.1	0
OBM	-62.68	-8.77	0	8.77	57.58	-5.1					
BM	62.68	8.77	0	-8.77	-57.58	5.1					
DM	0	62.68	4.47	4.30	0	-4.7	-4.47	-14.97	-42.61	-5.1	0
TM	2.235	3.44	0	-2.15	-2.15	0	-7.49	-2.24	-2.55	-2.505	
OBM	2.235	3.44	0	-2.49	-4.79	-2.505					
BM	-2.235	-3.44	0	7.49	4.79	2.505					
DM	0	-2.235	-5.78	-5.36	0	3.67	3.82	1.25	3.54	2.50	0
	-2.79	-1.20	-7.69	-1.84	0	0.63	1.91	10.66	1.77		
OBM	-2.79	-4.12	-5.95	0.63	12.57	1.77					
BM	2.79	4.12	5.95	-0.63	-12.57	-1.77					
DM	0	7.99	0.57	0.55	2.93	2.93	-0.71	-0.31	-3.27	-9.29	-1.77
TM	0.29	3.40	1.47	0.23	-0.16	1.47	-1.64	-0.16	-0.89	-4.65	
OBM	0.29	4.87	0.12	-0.17	-1.05	-4.65					
BM	-0.29	-4.87	-0.12	0.17	1.05	4.65					
DM	0	0.29	-2.48	-2.39	-0.06	-0.06	7.88	0.009	0.27	0.78	4.65
E	0	22.88	82.88	69.8	69.05	72.06	-22.06	45.47	-45.46	0	

Moments

- M_A = 0 kNm
- M_B = 82.88 kNm
- M_C = 69.06 kNm
- M_D = 72.06 kNm
- M_E = 45.47 kNm
- M_A = 0 kNm

free moment

for UDL = $\frac{wL^2}{8}$

$$(1) \frac{40.68 \times 4.3^2}{8} = 94.02 \text{ kN/m}^2$$

$$(2) \frac{42.34 \times 1.5^2}{8} = 107.17 \text{ kN/m}^2$$

$$(3) \frac{27.29 \times 1.5^2}{8} = 8.24 \text{ kN/m}^2$$

span moment

for UDL = $\frac{wL^2}{8}$ $M_{AB} = M^F - \left(\frac{M_A + M_B}{2} \right)$

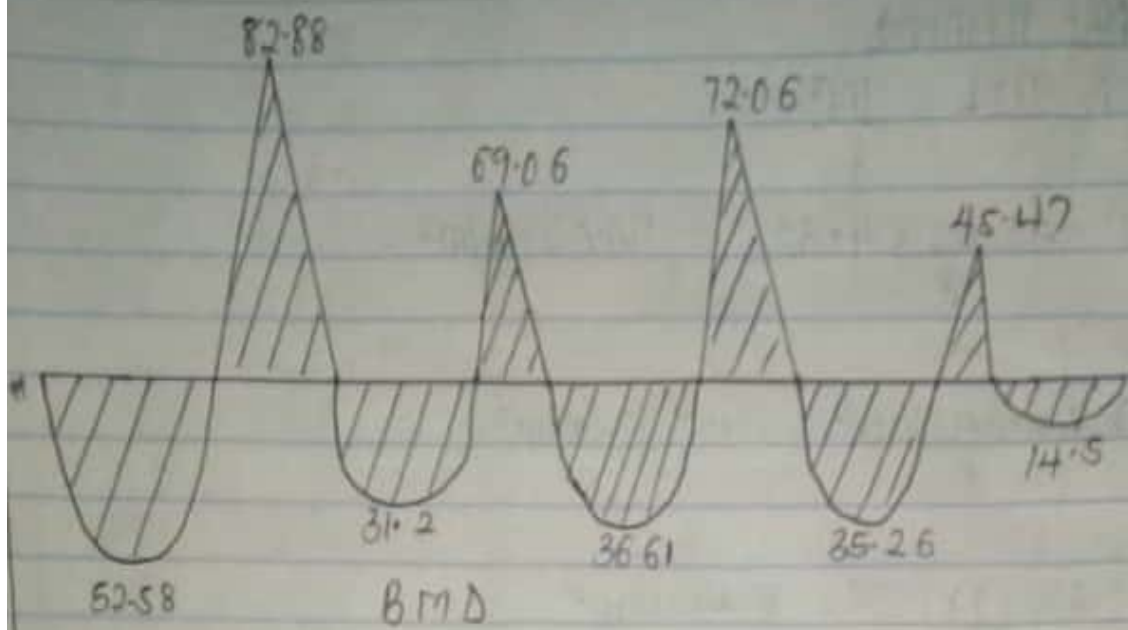
$$(1) 40.6 \cdot \quad = 94.02 - \left(\frac{0 + 82.88}{2} \right) = 52.58 \text{ kNm}$$

$$M_{BC} = M^F - \left(\frac{M_B + M_C}{2} \right) = 107.17 - \left(\frac{82.88 + 69.06}{2} \right) = 31.2 \text{ kNm}$$

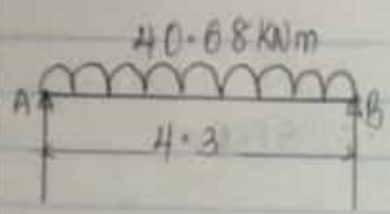
$$M_{CD} = M^F - \left(\frac{M_C + M_D}{2} \right) = 107.17 - \left(\frac{69.06 + 72.06}{2} \right) = 36.61 \text{ kNm}$$

$$M_{DE} = M^F - \left(\frac{M_D + M_E}{2} \right) = 94.02 - \left(\frac{72.06 + 45.47}{2} \right) = 35.26 \text{ kNm}$$

$$M_{EF} = M^F - \left(\frac{M_E + M_A}{2} \right) = 8.24 - \left(\frac{45.47 + 0}{2} \right) = -14.5 \text{ kNm}$$



shear force
for A



$$V_A = \frac{wL}{2} = V_A$$

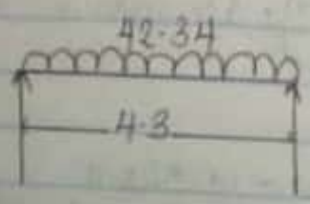
$$= \frac{40.68 \times 4.3}{2} = 87.462 \text{ kN}$$

$$V_{AB} = V_A + \left(\frac{M_B - M_A}{L} \right) = 87.462 + \left(\frac{0 - 82.88}{4.3} \right) = 68.19$$

$$V_B = wL - V_{AB}$$

$$= (40.68 \times 4.3) - 68.19 = 106.73 \text{ kN}$$

for B



$$V_{BC} = \frac{wL}{2} = V_C$$

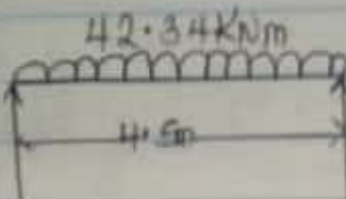
$$= \frac{42.34 \times 4.5}{2} = 95.27 \text{ kN}$$

$$V_{BC} = V_B + \left(\frac{M_B + M_C}{L} \right) = 95.27 + \left(\frac{82.68 + 69.06}{4.5} \right) = 128.99 \text{ kN}$$

$$V_C = (42.34 \times 4.5) - 128.99$$

$$= 61.54 \text{ kN}$$

for C



$$V_C = \frac{wL}{2} = V_D$$

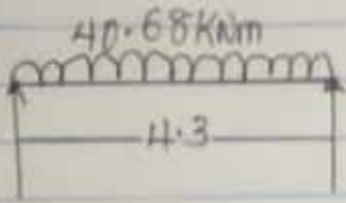
$$= \frac{42.34 \times 4.5}{2} = 95.27$$

$$V_{CD} = 95.27 + \left(\frac{69.06 + 72.06}{4.5} \right) = 126.63 \text{ kN}$$

$$V_{DC} = (42.34 \times 4.5) - 126.63$$

$$= 63.19 \text{ kN}$$

for D



$$V_C = \frac{wL}{2} = V_E$$

$$= \frac{40.68 \times 4.3}{2} = 87.46 \text{ kN}$$

$$V_{DE} = V_D - \left(\frac{M_D + M_E}{L} \right)$$

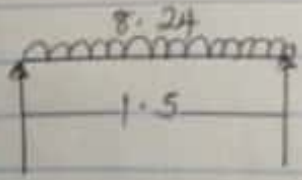
$$= 87.46 - \left(\frac{72.06 + 45.47}{4.3} \right) = 60.13 \text{ kN}$$

$$V_{CD} = wL - V_{DC}$$

$$= (40.68 \times 4.3) - 60.13$$

$$= 114.79 \text{ kN}$$

for E

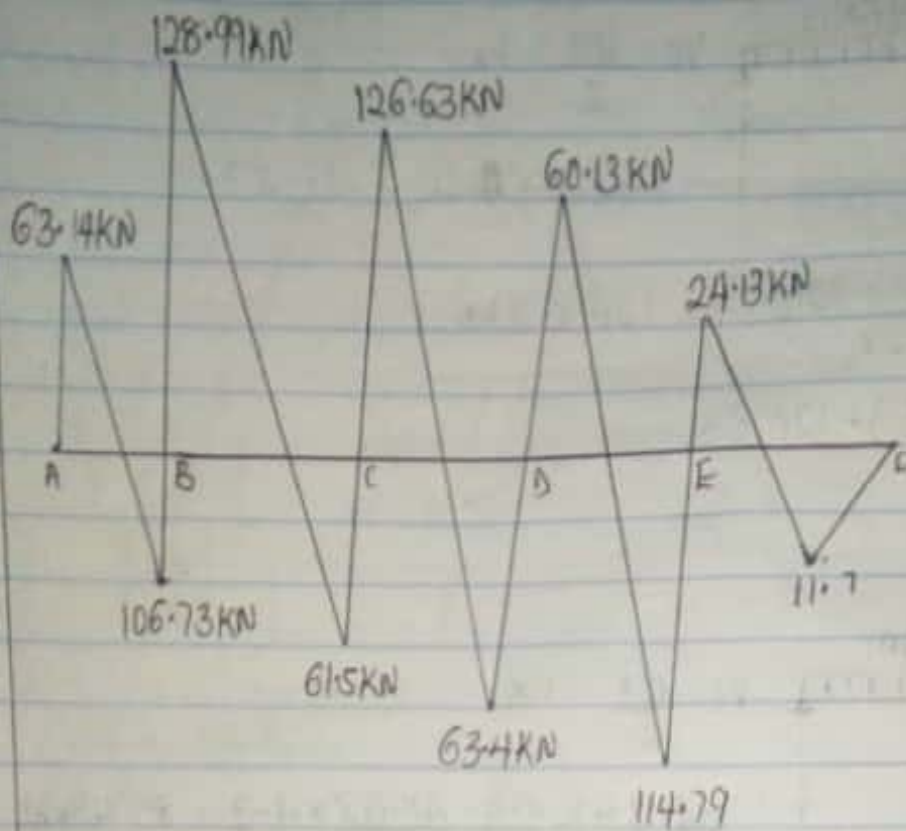


$$V_E = \frac{wL}{2} = V_A$$

$$= \frac{8.24 \times 1.5}{2} = 6.18 \text{ kN}$$

$$V_{EA} = V_A - \left(\frac{M_E + M_A}{L} \right) = 6.18 - \left(\frac{45.47 + 0}{1.5} \right) = 24.13 \text{ kN}$$

$$V_{AE} = (8.24 \times 1.5) - 24.13$$



QUESTION 2

$N = 1200 \text{ kN}$

length = $25 - 410 \text{ N/mm}^2$

$f_b = 150 \text{ kN/mm}^2$

Area of base req = $\frac{N \times 1.1}{1 \times f_b} \quad \lambda = 1.46$

$\frac{1200 \times 1.1}{1.46 \times 150} = 6.027 \text{ m}^2$

1.46×150

$\sqrt{6.027} = 2.45 \text{ m} \approx 2.5$

Net pressure, $F_{net} = \frac{N \times 1.4}{B}$

$\frac{1200 \times 1.1}{2.5} = 24 \times 0.660 \times 1.4$

$= 505.824 \text{ kN/m}$

moment, $m = \frac{F_{net} l^2}{2}$

where $l = \frac{1}{2}(B - b)$: depth of base = 660

$$L = \frac{1}{2}(2.5 - 0.225) = 1.1375 \approx 1.14 \text{ m}$$

$$M = \frac{508.824 \times 1.14^2}{2} = 328.68 \text{ kNm}$$

$$d = h - \text{cover} - \frac{1}{2} \phi$$

$$660 - 50 - 10 = 600 \text{ mm}$$

$$K = \frac{M}{bd^2 f_c} = \frac{328.68 \times 10^6}{1000 \times 600^2 \times 25} = 0.037$$

$$R_{cr} = 0.5 + \sqrt{\frac{0.25 + 0.037}{0.9}} = 0.96 > 0.85$$

$$Z = R_{cr} d = 0.95 \times 600 = 570 \text{ mm}$$

$$A_c = \frac{M}{0.95 f_y Z} = \frac{328.68 \times 10^6}{0.95 \times 410 \times 570} = 1480.44 \text{ mm}^2$$

provide 425 @ 300 c/c (1640)

Punching Shear

Column size = 225 x 450 mm

for $f_y = 25 - 410 \text{ mm}$

Area footing = 6.027 m²

Size of footing = 2500 x 2500

$q =$ net pressure = 508.824 kN/m

depth = 600

ankle Section: $\frac{d}{2} = \frac{600}{2} = 300$

$$300 + 300 + 225 = 825 \text{ mm}$$

$$800 + 300 + 450 = 1050 \text{ mm}$$

$$\text{Shear force } V_u = q_0 \times [\text{Area of footing} - (0.3 + d)^4]$$

$$= 505.824 [2.5 \times 2.5 - (0.3 + 0.6)^2]$$

$$V_u = 505.824 (6.25 - 0.81) = 2751.68$$

NUMER

$$\text{Shear stress } \tau_v = V_u / bd$$

b = parameter of critical section

d = effective span depth

$$\tau_v = \frac{2751.68 \times 10^3}{((2 \times 825) + 2(1050) \times 600)}$$

$$\tau_v = 1.223 \text{ N/mm}^2$$

Permissible shear stress

$$\tau_c = K_s \times \tau_c$$

$K_s = (0.5 + B/C)$ but not greater than 1

B/C = Ratio OR shorter to larger side of columns

$$\tau_c = 0.25 \sqrt{f_{ck}}$$

$$K_s = 1$$

$$\tau_c = 0.25 \sqrt{25} = 1.25 \text{ N/mm}^2$$

$$\tau_v = 1.223 \text{ N/mm}^2$$

$$\tau_v \leq \tau_c$$

Hence depth assumed is OK

Checking for fb with actual size of footing

Limit weight of concrete = 24 kN/mm^3

Limit weight of soil = $1.091 \times 10^{-6} \text{ kN/mm}^3$

Actual pressure footing below

$$q = (1200 \times 2.5 \times 2.5) + (24 \times 0.660) + (1.091 \times 10^6 \times 0.64)$$

$$q = 214.94 \text{ kN/m}^2$$