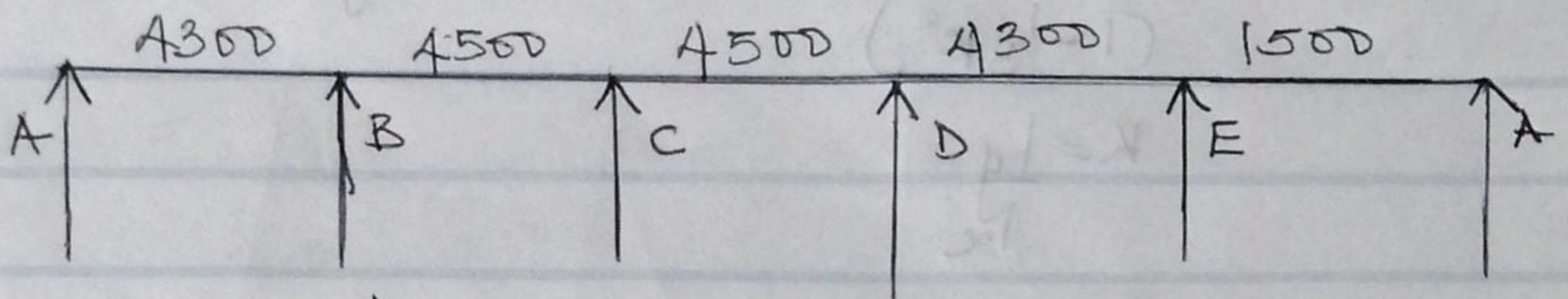


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 17/ENG03/055  
 Civil Engineering  
 Structural Design  
 Assignment II



Assuming thickness : 150mm

$$f_{cu} = 25 \text{ N/mm}^2$$

$$f_y = 410 \text{ N/mm}^2$$

Slab loading

$$\text{Slab weight} = 0.15 \times 24 = 3.6 \text{ kN/m}^2$$

$$\text{Partition} = 1.0 \text{ kN/m}^2$$

$$\text{finishes} = 1.2 \text{ kN/m}^2$$

$$\text{Total G.K} = \underline{\underline{5.8 \text{ kN/m}^2}}$$

assuming for classroom

$$D.L = 1.4(5.8) + 1.6(3.0) = 13 \text{ kN/m}^2$$

Beam loading

$$\text{Self wt of beam} = 0.225 \times 0.6 \times 24 = 3.24 \text{ kN/m}^2$$

$$\text{finishes} = 1.2 \text{ kN/m}^2$$



$$\text{Wall load} = 3 \times 3.47 = 10.41 \text{ kN/m}^2$$

$$\text{Total G.K.} = 14.85$$

$$\text{D.L.} = 14(14.85) = 20.79 \text{ kN/m}^2$$

Slab load on beam in longer direction =  $\frac{1}{2} w_k$   
 $(1 - \frac{1}{3} k^2)$

$$k = \frac{l_y}{l_x}$$

$$\frac{4300}{4000} = 1.075$$

$$\frac{4500}{4000} = 1.125$$

$$\frac{1}{2} \times 13 \times 4.3 \left( 1 - \frac{1}{3} \times (1.075)^2 \right) = 19.89 \text{ kN/m}^2$$

$$\frac{1}{2} \times 13 \times 4.5 \left( 1 - \frac{1}{3} \times (1.125)^2 \right) = 21.55 \text{ kN/m}^2$$

Slab load on beam in shorter direction =  $\frac{1}{3} w_k$

$$= \frac{1}{3} \times 13 \times 1.5 = 6.5 \text{ kN/m}^2$$

$$\text{Total load} = 19.89 + 20.79 = 40.68 \text{ kN/m}$$

$$= 21.55 + 20.79 = 42.34 \text{ kN/m}$$

$$= 6.5 + 20.79 = 27.29 \text{ kN/m}$$



Distribution factor

$$K_{AB} = 1$$

$$K_{BA} = \frac{\frac{1}{I_{BA}}}{\frac{1}{I_{BA}} + \frac{1}{I_{BC}}} = \frac{\frac{1}{4.3}}{\frac{1}{4.3} + \frac{1}{4.5}} = 0.51$$

$$K_{BC} = 1 - 0.51 = 0.49$$

$$K_{CB} = \frac{\frac{1}{4.5}}{\frac{1}{4.5} + \frac{1}{4.5}} = 0.5$$

$$K_{CD} = 1 - 0.5 = 0.5$$

$$K_{DC} = 0.49$$

$$K_{DE} = 0.51$$

$$K_{ED} = \frac{\frac{1}{4.3}}{\frac{1}{4.3} + \frac{1}{1.5}} = 0.26$$

$$K_{EA} = 1 - 0.26 = 0.74$$

$$K_{AF} = 1$$

F.E.M

$$UDL = \frac{wL^2}{12}$$

$$1 \quad \frac{40.68 \times 4.3^2}{12} = 62.68 \text{ kN/m}$$

$$3) \quad \frac{27.29 \times 1.5^2}{12} = 5.1 \text{ kN/m}$$

$$2 \quad \frac{42.34 \times 4.5^2}{12} = 71.45 \text{ kN/m}$$



	A	B		C		D		E		A		
	AB	BA	BC	CB	CD	DC	DE	ED	EA	AA		
DIF	0	1	0.51	0.49	0.5	0.5	0.49	0.51	0.2	0.74	1	0
FEM	<del>62.68</del>	62.68	-71.45	71.45	-71.45	71.45	-62.68	62.68	-5.1	5.1		
OBM	-62.68	-8.77				8.77		57.58		-5.1		
BM	62.68	8.77				-8.77		-57.58		5.1		
DM	0	62.68	4.47	4.80	0	0	-4.80	-4.47	-14.97	-42.61		-5.1
TM		2.235	31.34	0	2.15	-2.15	0	-7.49	-2.24	-2.55		-21.305
OBM	2.235	31.34					-7.44	-4.79		-21.305		
BM	-2.235	-31.34					7.44	4.79		21.305		
DM	0	-2.235	-15.98	-15.36	0	0	2.67	3.82	1.25	3.54		21.31
TM		-7.99	-1.12	0	-7.69	1.84	0	0.68	1.91	10.66		1.77
OBM	-7.99	-1.12		-5.85			0.63	12.57		1.77		
BM	7.99	1.12		5.85			-0.63	-12.57		-1.77		
DM	0	7.99	0.57	0.55	2.93	2.93	-0.81	-0.37	-3.27	-9.29		-1.77
TM		0.29	8.40	1.47	0.28	-0.16	1.47	1.64	-0.16	-0.89		-4.65
OBM	0.29	4.87		0.12			0.17	-1.05		-4.65		
BM	-0.29	-4.87		-0.12			-0.17	1.05		4.65		
DM	0	-0.29	-2.48	-2.39	-0.06	-0.06	0.06	0.09	0.27	0.78		4.65
Σ	0	22.88	-82.88	67.06	-67.06	72.06	-72.06	45.47	-45.46	0		



Moments

$$M_a = 0 \text{ kNm}$$

$$M_b = 82.88 \text{ kNm}$$

$$M_c = 69.06 \text{ kNm}$$

$$M_d = 72.06 \text{ kNm}$$

$$M_e = 45.41 \text{ kNm}$$

$$M_f = 0 \text{ kNm}$$

Free moment

$$A \cdot 2 \cdot D \cdot L = \frac{w l^2}{8}$$

$$1 \quad \frac{40.68 \times 4.3^2}{8} = 94.02 \text{ kNm}^2$$

$$2 \quad \frac{42.34 \times 4.5^2}{8} = 107.17 \text{ kNm}^2$$

$$3 \quad \frac{27.29 \times 1.5^2}{8} = 8.24 \text{ kNm}^2$$

Span moment

$$M_{AB} = M^F - \left( \frac{M_A + M_B}{2} \right) = 94.02 - \left( \frac{0 + 82.88}{2} \right) = 57.58 \text{ kNm}$$

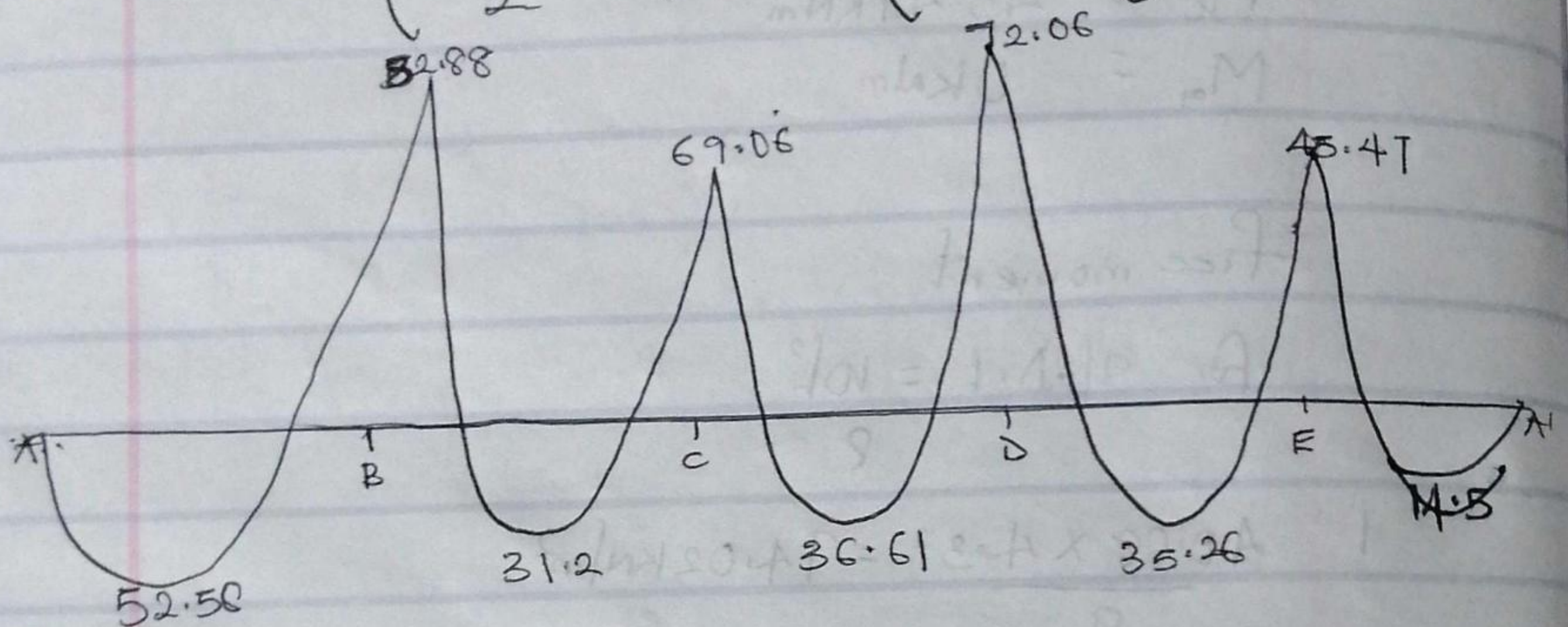
$$M_{BC} = M^F - \left( \frac{M_B + M_C}{2} \right) = 107.17 - \left( \frac{82.88 + 69.06}{2} \right) = 31.2 \text{ kNm}$$



$$M_{CD} = M^R - \left( \frac{M_C + M_D}{2} \right) = 107.17 - \left( \frac{69.06 + 12.06}{2} \right) = 36.6 \text{ kNm}$$

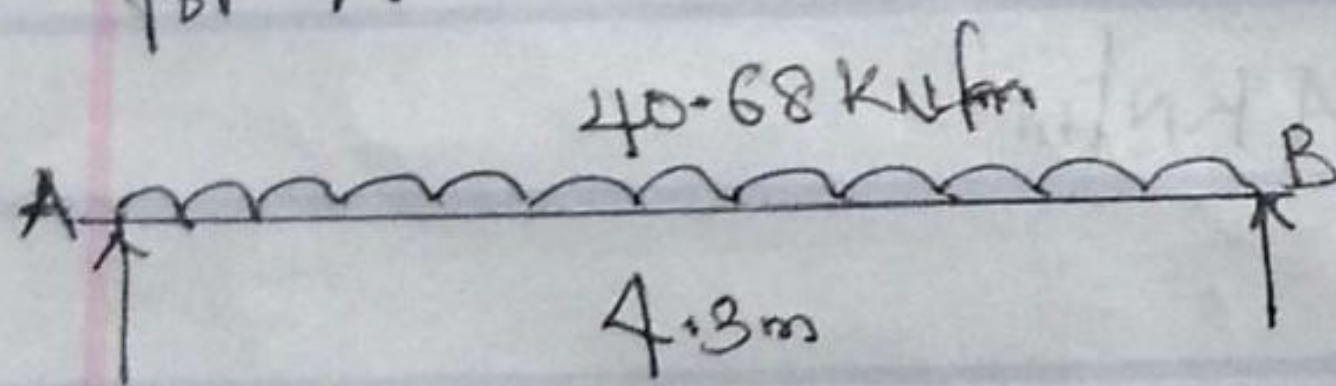
$$M_{DE} = M^R - \left( \frac{M_D + M_E}{2} \right) = 94.02 - \left( \frac{72.06 + 45.47}{2} \right) = 35.26 \text{ kNm}$$

$$M_{EK} = M^R - \left( \frac{M_E + M_K}{2} \right) = 8.24 - \left( \frac{45.47 + 0}{2} \right) = -14.5 \text{ kNm}$$



Shear force

for A



$$V_A = \frac{wl}{2} = V_B$$

$$= \frac{40.68 \times 4.3}{2} = 87.462 \text{ kN}$$

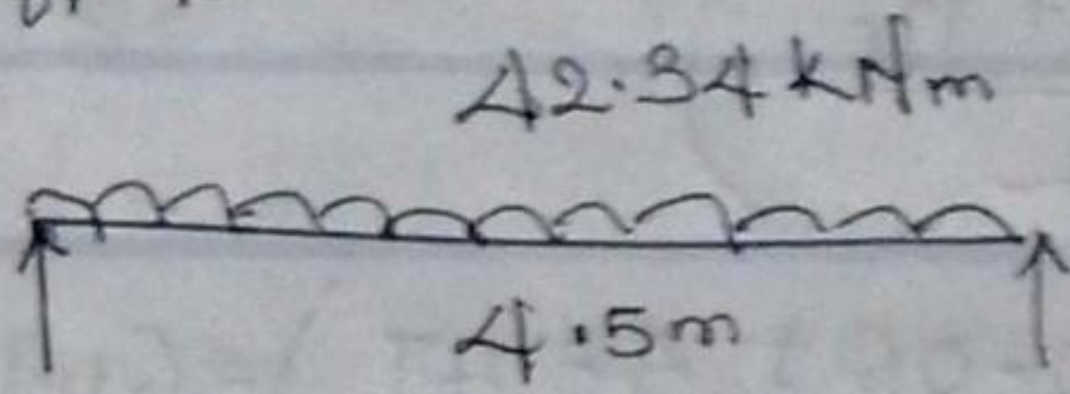
$$V_{AB} = V_A + \left( \frac{M_A - M_B}{L} \right) = 87.462 + \left( \frac{0 - 82.88}{4.3} \right) = 68.19$$

$$V_{BA} = wl - V_{AB}$$

$$= (40.68 \times 4.3) - 68.19 = 106.73 \text{ kN}$$



for B



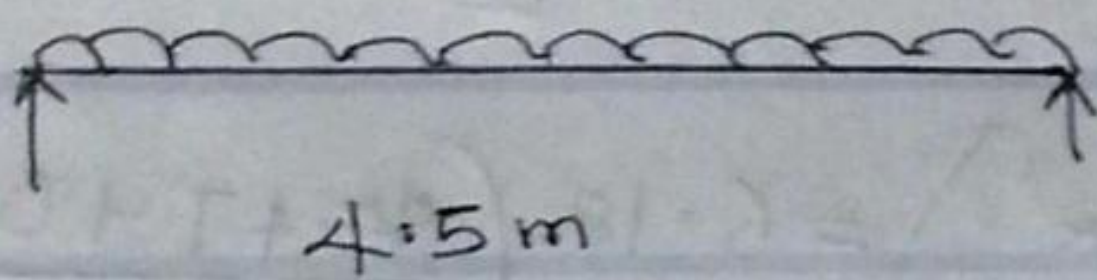
$$V_{BC} = \frac{wL}{2} = V_C$$

$$= \frac{42.34 \times 4.5}{2} = 95.27 \text{ kN}$$

$$V_{BC} = V_B + \left( \frac{M_B + M_C}{L} \right) = 95.27 + \left( \frac{82.68 + 69.06}{4.5} \right)$$
$$= 129.03 \text{ kN}$$

$$V_{CB} = (42.34 \times 4.5) = 129.03$$
$$= 61.5 \text{ kN}$$

for C



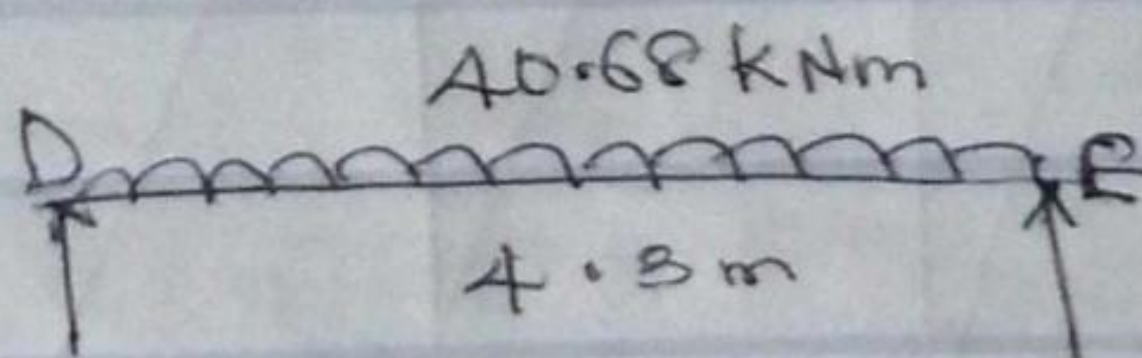
$$V_C = \frac{wL}{2} = V_D$$

$$= \frac{42.34 \times 4.5}{2} = 95.27 \text{ kN}$$

$$V_{CD} = 95.27 + \left( \frac{69.06 + 72.06}{4.5} \right) = 126.63 \text{ kN}$$

$$V_{DC} = (42.34 \times 4.5) - 126.63$$
$$= 63.99 \text{ kN}$$

for D



$$V_D = \frac{wL}{2} = V_E$$

$$= \frac{40.68 \times 4.3}{2} = 87.46 \text{ kN}$$



$$V_{DE} = V_D - \left( \frac{M_D + M_E}{L} \right)$$

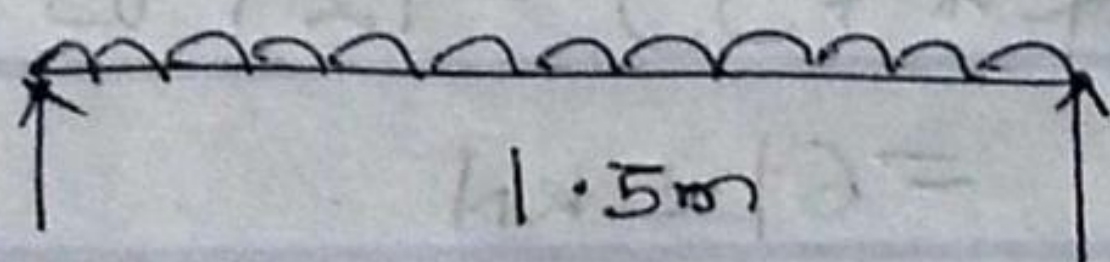
$$= 87.46 - \left( \frac{72.06 + 45.47}{4.3} \right) = 60.13 \text{ kN}$$

$$V_{ED} = wL - V_{DE}$$

$$= (40.68 \times 4.3) - 60.13$$

$$= 114.79 \text{ kN}$$

For E

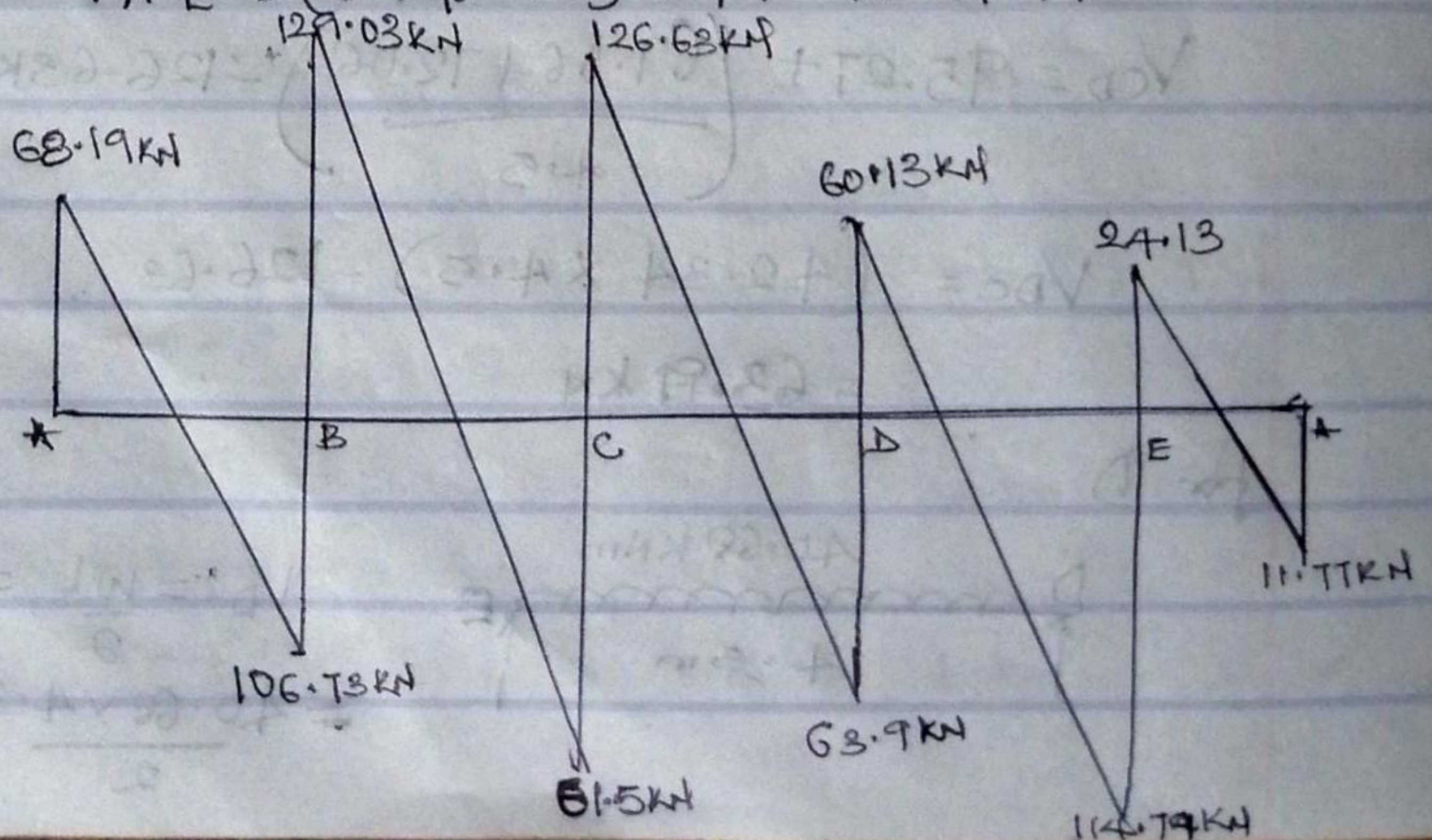


$$V_{E'} = \frac{wL}{2} = V_D'$$

$$= \frac{8.24 \times 1.5}{2} = 6.18 \text{ kN}$$

$$V_{E''} = V_E \left( \frac{M_E + M_{A'}}{L} \right) = 6.18 - \left( \frac{45.47 + 0}{15} \right) = 24.13 \text{ kN}$$

$$V_{A'E} = (8.24 \times 1.5) - 24.13 = 11.77 \text{ kN}$$





Que. 2.

Base Design

$$N = 1200 \text{ kN}$$

$$Strength = 25 \cdot 410 \text{ Nmm}^2$$

$$f_b = 150 \text{ kN/m}^2$$

$$\text{Area of base req} = \frac{N \times 1.1}{1 \times f_b} \quad l = 1.46$$

$$\frac{1200 \times 1.1}{1.46 \times 150} = 6.027 \text{ m}^2$$

$$1.46 \times 150$$

$$\sqrt{6.027} = 2.45 \text{ m} \approx 2.5$$

$$\text{Net pressure, } f_{net} = \frac{N \times 1.1}{B}$$

$$\frac{1200 \times 1.1}{2.5} = 24 \times 0.660 \times 1.4$$

$$= 505.824 \text{ kNm}$$

$$\text{moment; } M = \frac{f_{net} l^2}{2}$$

$$\text{where } l = \frac{1}{2} (B - b) \phi$$

$$= \text{depth of base} = 660$$

$$L = \frac{1}{2} (2.5 - 0.225) = 1.1375 \approx 1.14 \text{ m}$$

$$M = \frac{505.824 \times 1.14^2}{2} = 328.68 \text{ kNm}$$

$$d = h - \text{cover} - \frac{1}{2} \phi$$



$$= 660 - 50 - 10 = 600 \text{ mm}$$

$$k = \frac{M}{bd^2 f_{ov}} = \frac{328.68 \times 10^6}{1000 \times 600^2 \times 25} = 0.037$$

$$R_n = 0.5 + \frac{\sqrt{0.25 + 0.037}}{0.9} = 0.967 \approx 0.95$$

$$z = R_n d = 0.95 \times 600 = 570 \text{ mm}$$

$$A_s = \frac{M}{0.95 f_y z} = \frac{328.68 \times 10^6}{0.95 \times 410 \times 570} = 1480.44 \text{ mm}^2$$

Provide  $\gamma 25 @ 300 \text{ c/c } (1640)$

Punching shear

$$\text{Column size} = 225 \times 450 \text{ mm}$$

$$f_{cu} f_y = 25 - 410 \text{ mm}$$

$$\text{Area footing} = 6.027 \text{ m}^2$$

$$\text{Size of footing} = 2500 \times 2500$$

$$q^s, \text{ Net pressure} = 508.824 \text{ kNm}$$

$$\text{depth} = 600$$

$$\text{critical section } \frac{d}{2} = 300$$

$$300 + 300 + 225 = 825 \text{ mm}$$

$$300 + 300 + 450 = 1050 \text{ mm}$$



Shear force  $V_n = q_n \times [ \text{Area of footing} - (0.3 + d)^2 ]$   
 $= 505824 [ 2.5 \times 2.5 - (0.3 + 0.6)^2 ]$   
 $V_n = 2751.68$

Normal Shear stress  $\tau_v = \frac{V_n}{bd}$

$b$  = parameter of critical section  
 $d$  = effective span/depth

$$\tau_v = \frac{2751.68 \times 10^3}{(2 \times (825) + 2(1050)) \times 600}$$

$$\tau_v = 1.223 \text{ N/mm}^2$$

permissible shear stress

$$\tau_c' = k_s \times \tau_c$$

$k_s = (0.5 + B_c)$  but not greater than 1

$B_c$  = Ratio of shorter to larger side of columns

$$\tau_c = 0.25 \sqrt{f_{ck}}$$

$$k_s = 1$$

$$\tau_c = 0.25 \sqrt{25} = 1.25 \text{ N/mm}^2$$

$$\tau_v = 1.223 \text{ N/mm}^2$$

$$\tau_v \leq \tau_c$$

hence depth assumed is ok ✓



Checking for fb with actual size of footing  
Unit weight of concrete =  $24 \text{ kN/m}^3$   
Unit weight of soil =  $1.091 \times 10^{-6} \text{ kN/m}^3$

Actual pressure footing below

$$Q = (1200 \times 2.5 \times 2.5) + (24 \times 0.660) + (1.091 \times 10^6 \times 0.66)$$

$$Q = 7515.84 \text{ kN/m}^2$$