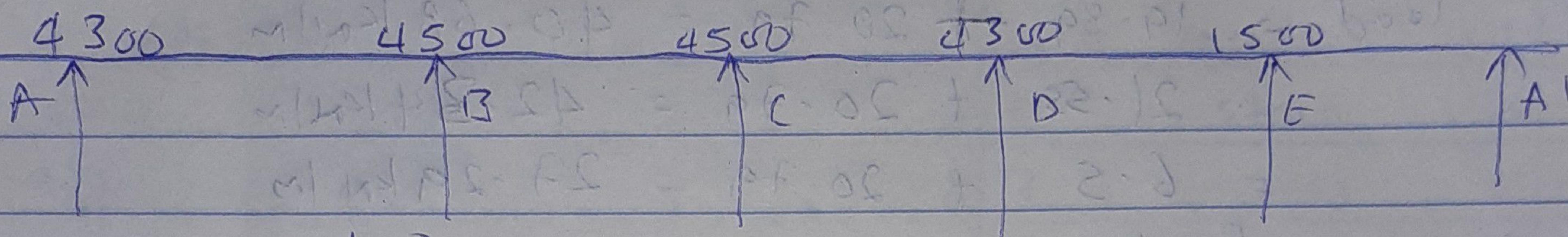


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Assignment 2

Question 1



Assuming thickness = 150mm

$$f_{cu} = 25 \text{ N/mm}^2$$

$$f_y = 410 \text{ N/mm}^2$$

Slab loading

$$\text{Slab weight} = 0.15 \times 2.4 = 3.6 \text{ kN/m}^2$$

$$\text{partition} = 1.2 \text{ kN/m}^2$$

$$\text{Finishes} = 1.2 \text{ kN/m}^2$$

$$\text{Total G.K} = 5.8 \text{ kN/m}^2$$

$$\text{D.L} = 1.4(5.8) + 16(3.0) = 13 \text{ kN/m}^2$$

Beam loading

$$\text{Self wt of beam} = 0.225 \times 0.6 \times 2.48 = 3.24 \text{ kN/m}$$

$$\text{Finishes} = 1.2 \text{ kN/m}^2$$

$$\text{Total load} = 3 \times 3.47 = 10.41 \text{ kN/m}^2$$

$$\text{Total G.K} = 14.85$$

$$\text{D.L} = 14(14.85) = 20.79 \text{ kN/m}^2$$

Slab load on beam in longer direction =  $\frac{1}{2} w l_x$   
(1- $\frac{1}{3}x$ )

$$k = \frac{l_y}{l_x}$$

$$\frac{4300}{4000} = 1.075$$

$$\frac{4500}{4000} = 1.125$$

$$\frac{1}{2} \times 13 \times 4.3 \left(1 - \frac{1}{3} (1.075)^2\right) = 19.89 \text{ kN/m}^2$$

$$\frac{1}{2} \times 13 \times 4.5 \left(1 - \frac{1}{3} (1.125)^2\right) = 21.55 \text{ kN/m}^2$$

Slab load on beam in shorter direction =  $\frac{1}{3} wlx$

$$\frac{1}{3} \times 13 \times 1.5 = 6.5 \text{ kN/m}^2$$

$$\text{Total load} = 19.89 + 20.79 = 40.68 \text{ kN/m}$$

$$= 21.55 + 20.79 = 42.34 \text{ kN/m}$$

$$= 6.5 + 20.79 = 27.29 \text{ kN/m}$$

Distribution factor

$$k_{AB} = 1$$

$$k_{BA} = \frac{\frac{1}{L_{BA}}}{\frac{1}{L_{BA}} + \frac{1}{L_{BC}}} = \frac{\frac{1}{4.3}}{\frac{1}{4.3} + \frac{1}{4.2}} = 0.51$$

$$k_{BC} = 1 - 0.51 = 0.49$$

$$k_{CB} = \frac{\frac{1}{4.5}}{\frac{1}{4.5} + \frac{1}{4.5}} = 0.5$$

$$k_{CD} = 1 - 0.5 = 0.5$$

$$k_{DC} = 0.49$$

$$k_{DE} = 0.51$$

$$k_{ED} = \frac{\frac{1}{4.3}}{\frac{1}{4.3} + \frac{1}{1.5}} = 0.26$$

$$k_{EA} = 1 - 0.26 = 0.79$$

$$k_{AE} = 1$$

FEM

$$w \cdot L^2 = \frac{w^2}{12}$$

$$1) \frac{40.68 \times 4.3^2}{12} = 62.68 \text{ kN/m}$$

$$2) \frac{42.34 \times 4.5^2}{12} = 71.45 \text{ kN/m}$$

$$3) \frac{27.29 \times 1.5^2}{12} = 5.1 \text{ kNm}$$

	A	B		C		D		E		A'		
	AB	BA	BC	CB	CD	DC	DE	ED	EA'	A'E		
DF	0	1	0.51	0.49	0.5	0.5	0.49	0.51	0.26	0.74	1	0
FEM	-62.68	62.68	-71.45	71.45	-71.45	71.45	-62.68	62.68	-5.1	5.1	5.1	0
OBM	-62.68	-8.77		0		8.77		57.58		-5.1		
BM	62.68	8.77		0		-8.77		-57.58		5.1		
DM	0	62.68	4.47	4.30	0	0	-4.30	-4.47	-14.97	-42.26	5.1	0
TM		2.235	31.34	0	2.15	-2.15	0	-7.49	-2.24	-2.55	-21.305	
OBM	2.235	31.34		0		-7.49		-4.79		-21.305		
BM	-2.235	-31.34		0		7.49		4.79		21.305		
DM	0	-2.235	-15.98	-15.36	0	0	3.67	3.82	1.25	3.54	21.31	0
TM		-7.99	-1.12	0	-7.69	1.84	0	0.63	1.91	10.66	1.77	
OBM	-7.99	-1.12		5.85		0.63		12.57		1.77		
BM	7.99	1.12		5.85		-0.63		-12.57		-1.77		
DM	0	7.99	0.57	0.55	2.93	2.93	-0.31	-0.37	-3.27	-9.29	-17.7	0
TM		0.29	3.40	1.47	0.28	-0.16	1.47	-1.64	-0.16	-0.89	-4.65	
OBM	0.29	4.87		0.12		-0.17		-1.05		-4.65		
BM	-0.29	-4.87		-0.12		0.17		1.05		4.65		
DM	0	-0.29	-2.48	-2.39	-0.06	-0.06	0.08	0.09	0.27	0.78	4.15	0
Z	=	0	22.88	-82.88	69.06	-69.05	72.06	-72.06	45.46	-45.46	0	

Moments

- $M_a = 0 \text{ kNm}$
- $M_b = 82.88 \text{ kNm}$
- $M_c = 72.06 \text{ kNm}$
- $M_d = 45.47 \text{ kNm}$

$$M_E = 45.47 \text{ kNm}$$

$$M_{A'} = 0 \text{ kNm}$$

Free moment

$$\text{for U.D.L} = \frac{wl^2}{8}$$

$$1) \frac{40.68 \times 4.3^2}{8} = 94.02 \text{ kNm/m}^2$$

$$2) \frac{42.34 \times 4.5^2}{8} = 107.17 \text{ kNm/m}^2$$

$$3) \frac{27.29 \times 1.5^2}{8} = 8.24 \text{ kNm/m}^2$$

Span moment

$$M_{AB} = M^A = \left( \frac{M_A + M_B}{2} \right) = 94.02 - \left( \frac{0 + 82.88}{2} \right)$$

$$= 52.88 \text{ kNm}$$

$$M_{BC} = M^B = \left( \frac{M_B + M_C}{2} \right) = 107.17 - \left( \frac{82.88 + 69.06}{2} \right)$$

$$= 31.2 \text{ kNm}$$

$$M_{CD} = M^C = \left( \frac{M_C + M_D}{2} \right) = 107.17 - \left( \frac{69.06 + 12.06}{2} \right)$$

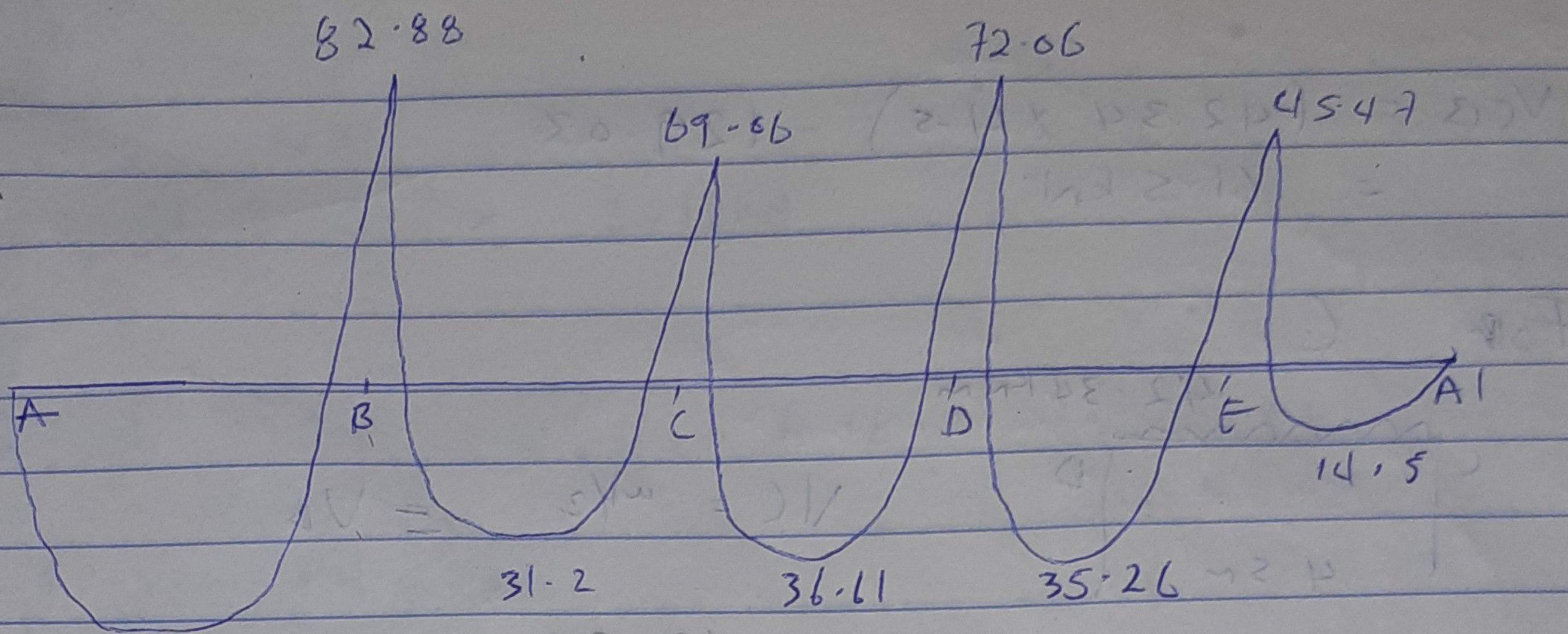
$$= 36.6 \text{ kNm}$$

$$M_{DE} = M^D = \left( \frac{M_D + M_E}{2} \right) = 94.02 - \left( \frac{72.06 + 45.47}{2} \right)$$

$$= 35.26 \text{ kNm}$$

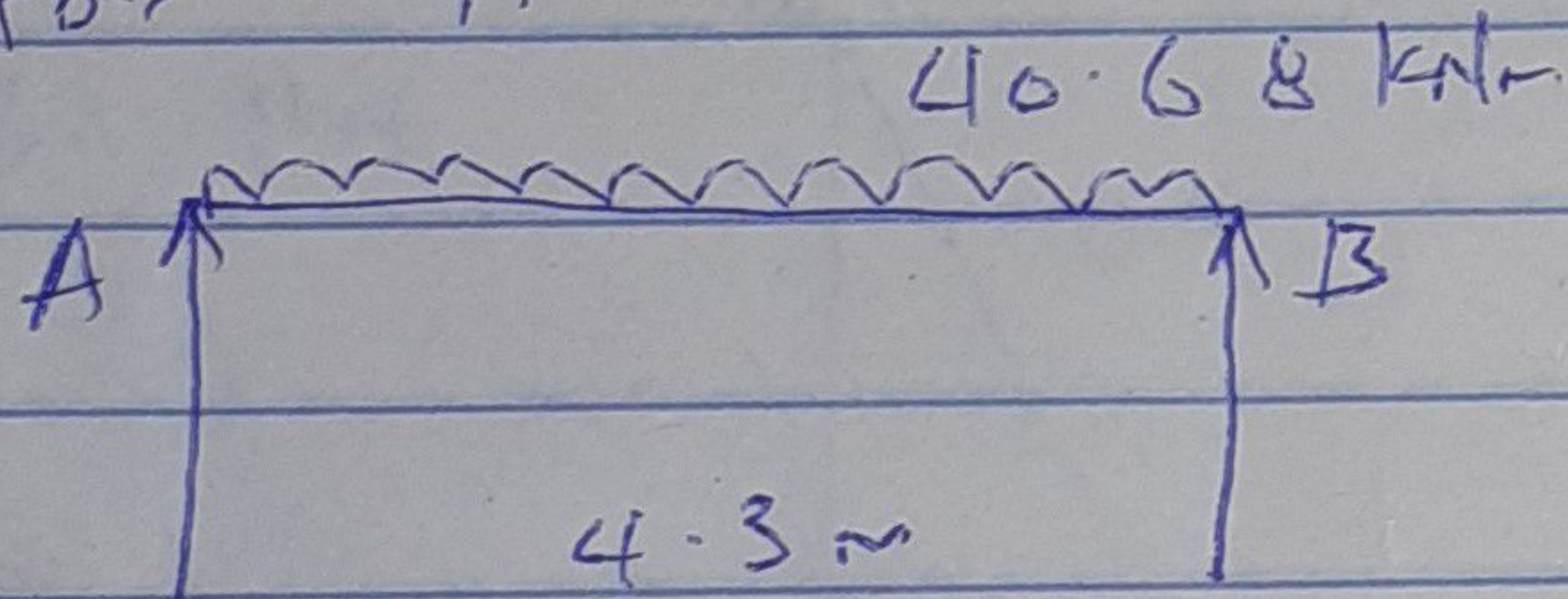
$$M_{E'A'} = M^E = \left( \frac{M_E + M_{A'}}{2} \right) = 8.24 - \left( \frac{45.47 + 0}{2} \right)$$

$$= -14.5 \text{ kNm}$$



Shear force

for A



$$V_A = \frac{wL}{2} = V_B$$

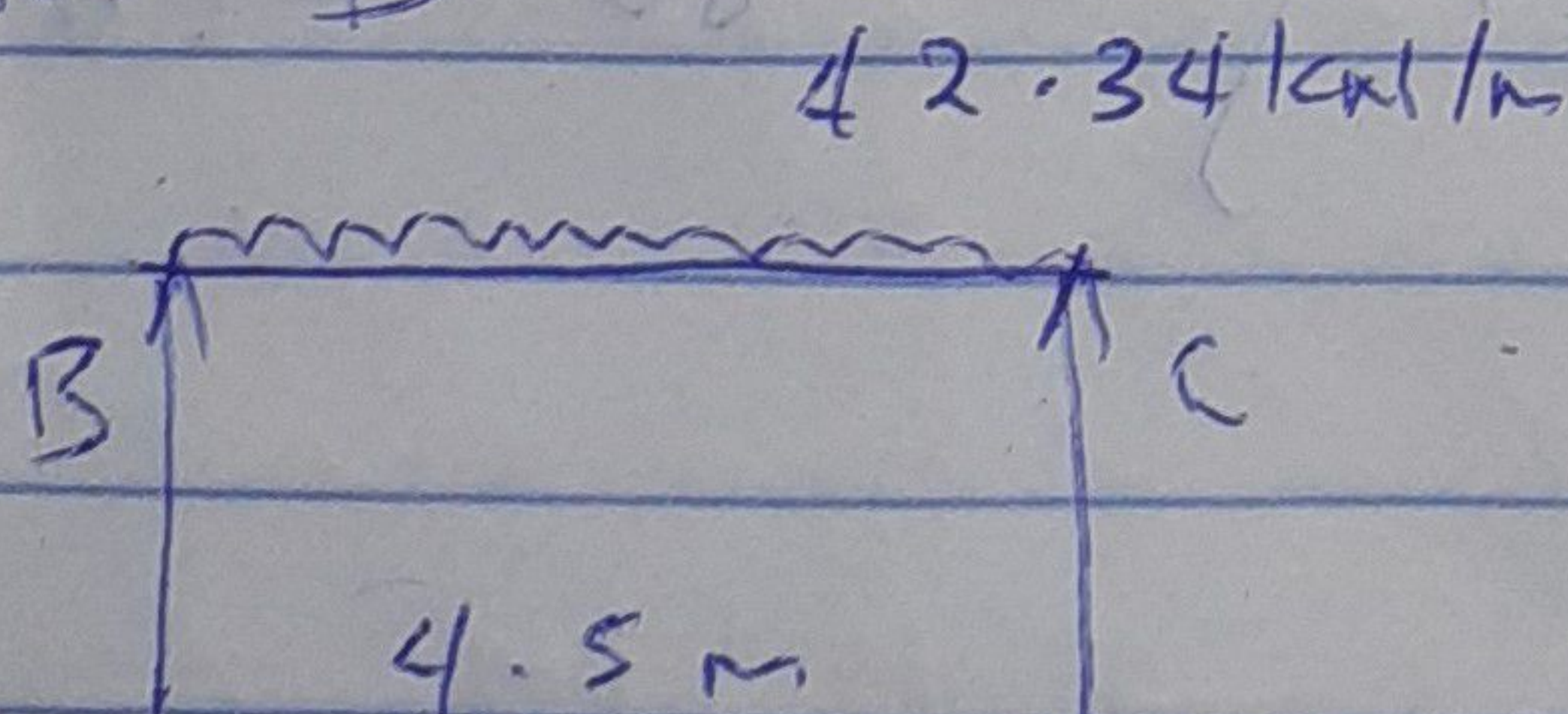
$$= \frac{40.68 \times 4.3}{2} = 87.462 \text{ kN}$$

$$V_{AB} = V_0 + \left( \frac{M_A - M_B}{L} \right) = 87.462 + \left( \frac{0 - 82.88}{4.3} \right)$$

$$V_{BA} = wL - V_{AB}$$

$$= (40.68 \times 4.3) - 68.19 = 106.731 \text{ kN}$$

for B



$$V_B = \frac{wL}{2} = V_C$$

$$= \frac{42.34 \times 4.5}{2} = 95.27 \text{ kN}$$

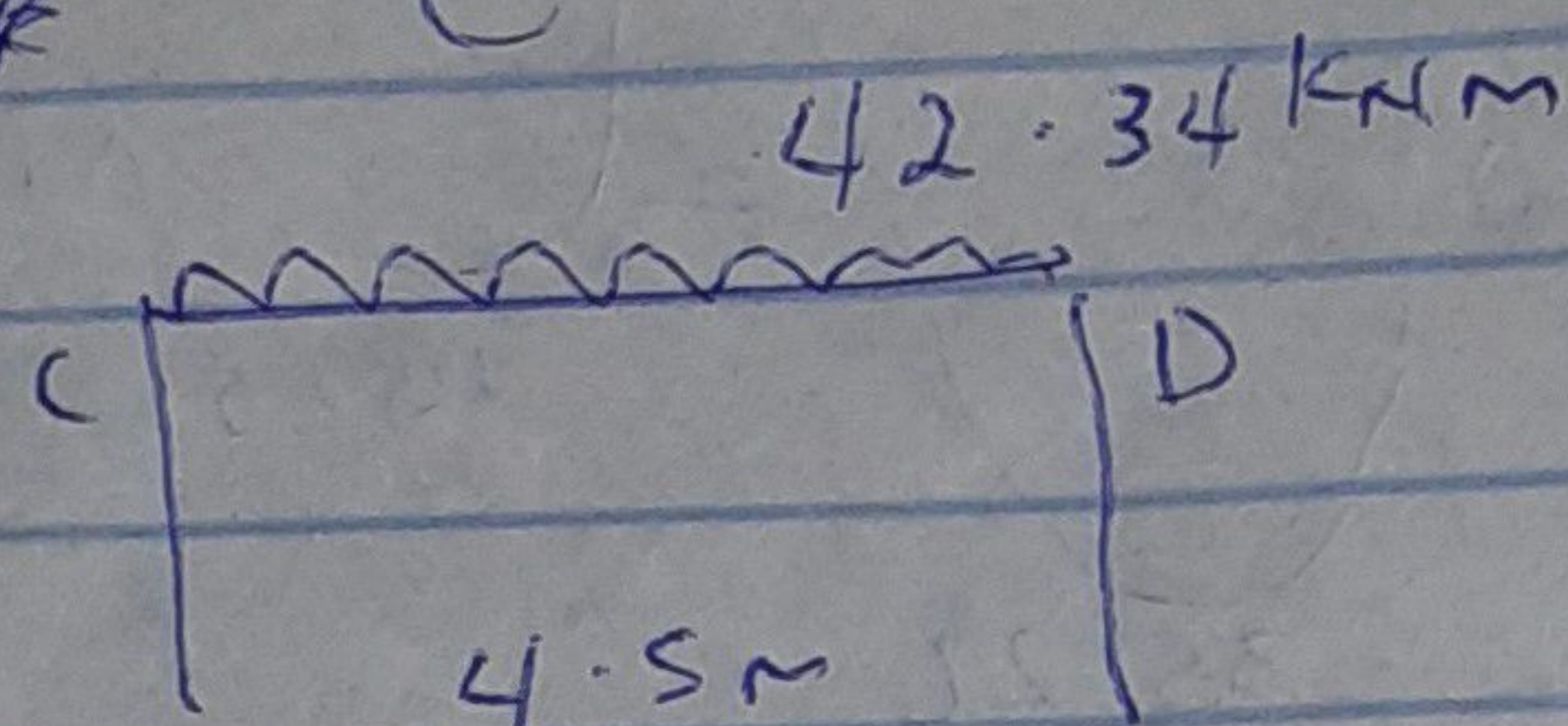
$$V_{BC} = V_B + \left( \frac{M_B + M_C}{L} \right) = 95.27 + \left( \frac{82.68 + 69.06}{4.5} \right)$$

$$= 129.03 \text{ kN}$$

$$V_{CB} = (42.34 \times 4.5) - 129.03$$

$$= 61.5 \text{ kN}$$

For C



$$V_C = wL/2 = V_D$$

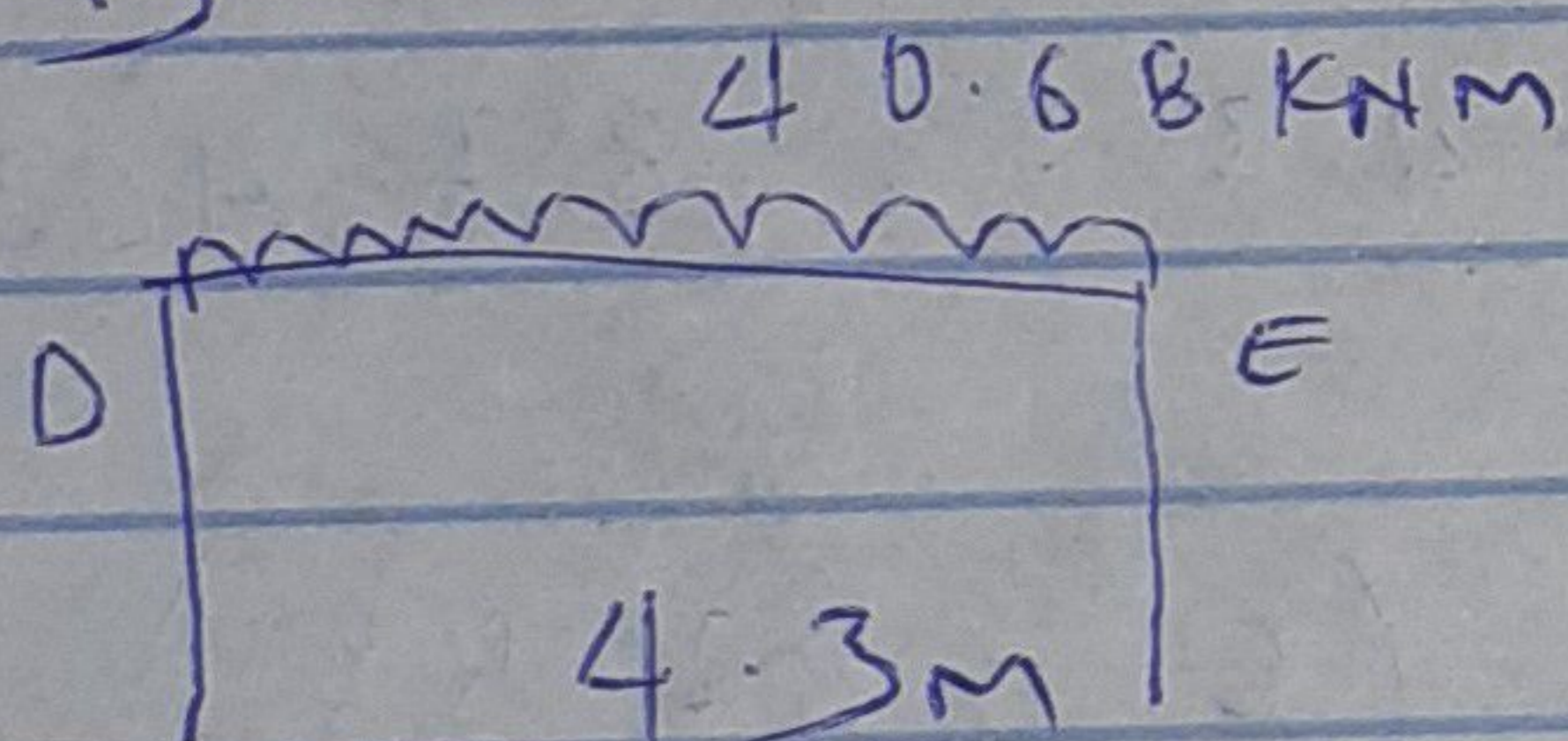
$$= \frac{42.34 \times 4.5}{2} = 95.27 \text{ kN}$$

$$V_{CD} = 95.27 + \left( \frac{69.06 + 72.06}{4.5} \right) = 126.63 \text{ kN}$$

$$V_{DC} = (42.34 \times 4.5) - 126.63$$

$$= \cancel{63.09} \text{ kN} = 63.9 \text{ kN}$$

For D



$$V_D = wL/2 = V_E$$

$$= \frac{40.68 \times 4.3}{2} = 87.46 \text{ kN}$$

$$V_{DE} = V_D - \left( \frac{M_D + M_E}{L} \right)$$

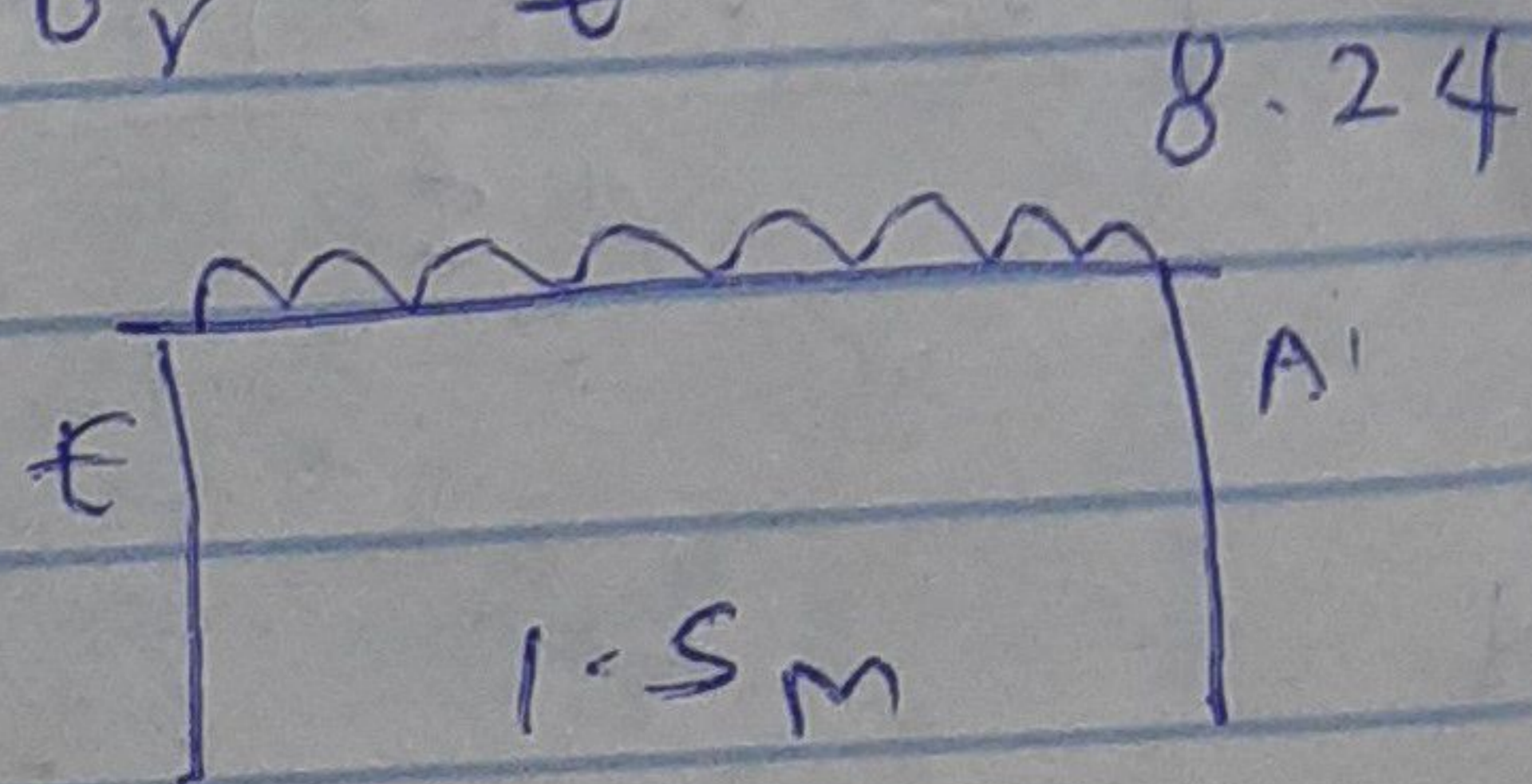
$$= 87.46 - \left( \frac{72.06 + 45.47}{4.3} \right) = 60.13 \text{ kN}$$

$$V_{ED} = wL = V_{DE}$$

$$= (40.68 \times 4.3) - 60.13$$

$$= 114.79 \text{ kN}$$

For E



$$V_E = wL/2 = \sqrt{A'}$$

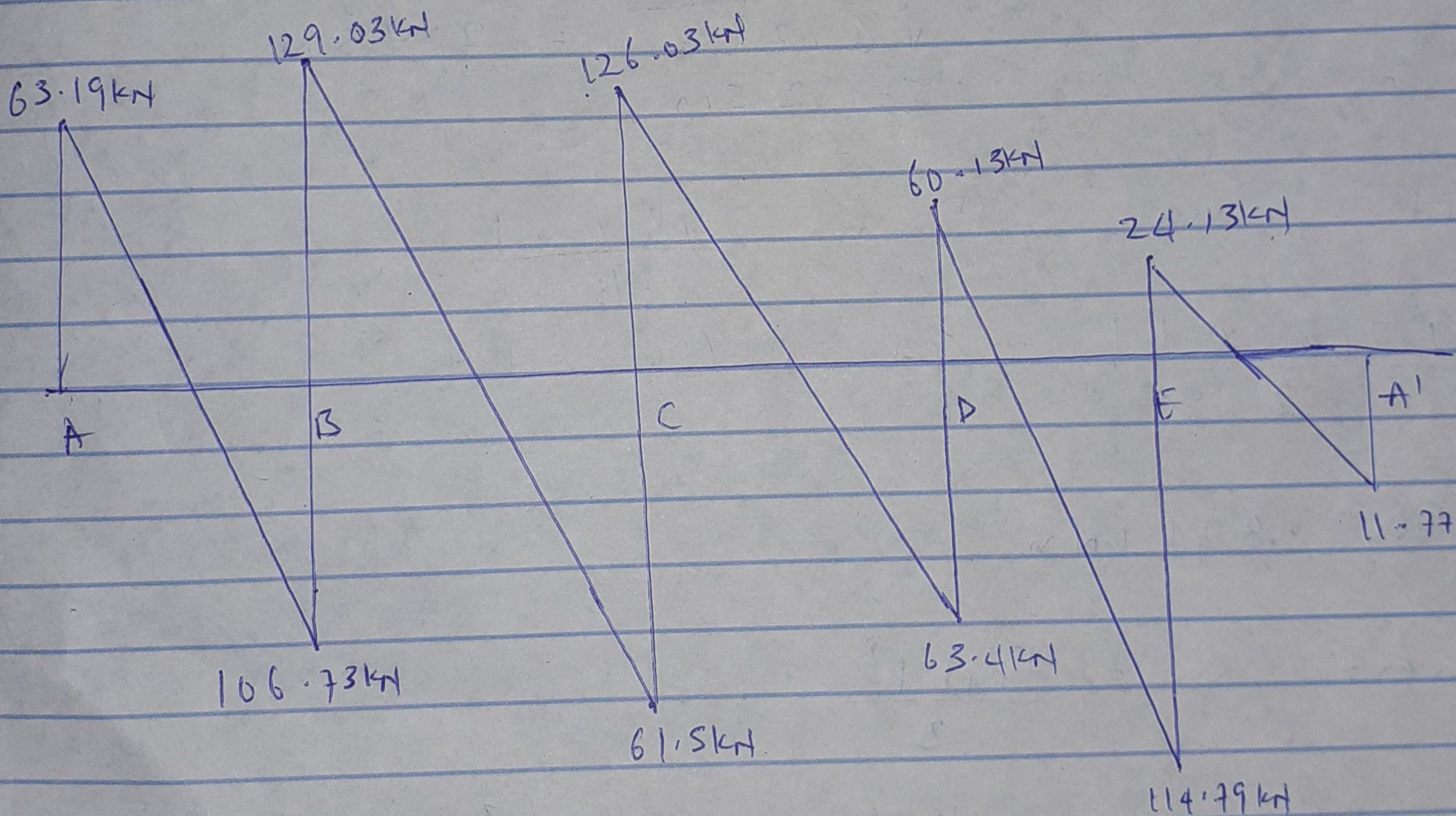
$$= \frac{8 \cdot 24 \times 1.5}{2} = 6.18 \text{ kN}$$

$$V_{EA'} = V_E - \left( \frac{M_E + M_{A'}}{L} \right) = 6.18 - \left( \frac{45.47 + 0}{1.5} \right)$$

$$= 24.13 \text{ kN}$$

$$V_{A'E} = (8 \cdot 24 \times 1.5) - 24.13$$

$$= 11.77 \text{ kN}$$



# Assignment 2

## Question 2

Base design

$$M = 1200 \text{ kNm}$$

$$\text{Strength} = 25 = 410 \text{ N/mm}^2$$

$$F_b = 150 \text{ kN/m}^2$$

$$\text{Area of base req} = \frac{N \times 1.1}{1 + F_b} = 1.46$$

$$\frac{1200 \times 1.1}{1.46 \times 100} = 6.027 \text{ m}^2$$

$$\sqrt{6.027} = 2.45 \text{ m}$$
$$\approx 2.5 \text{ m}$$

$$\text{Net pressure, } F_{\text{net}} = \frac{N \times 1.1}{B}$$

$$= \frac{1200 \times 1.1}{2.5} - 24 \times 0.666 \times 1.4$$

$$= 505.824 \text{ kN/m}$$

$$\text{Moment, } M = \frac{F_{\text{net}} l^2}{2}$$

where  $l = \frac{1}{2}(B - h)$  and  
depth of base = 660

$$l = \frac{1}{2}(2.5 - 0.225) = 1.138 \approx 1.14 \text{ m}$$

$$M = \frac{505.824 \times 1.14^2}{2} = 328.68 \text{ kNm}$$

$$d = h - \text{cover} = \frac{1}{2} \phi$$

$$= 660 - 50 - 10 = 600 \text{ mm}$$



$$k_s = \frac{M}{bd^2 f_{cu}} = \frac{328.68 \times 10^6}{1000 \times 600^2 \times 25} = 0.037$$

$$R_u = 0.5 + \sqrt{\frac{0.25 + 0.037}{0.9}} = 0.96 > 0.95$$

$$z = \frac{M}{R_u} = 0.95 \times 600 = 570 \text{ mm}$$

$$A_s = \frac{M}{0.95 f_y z} = \frac{328.68 \times 10^6}{0.95 \times 410 \times 570} = 1480.44 \text{ mm}^2$$

provide 425 @ 300 c/c (1640)

Punching shear

Column size = 225 x 450 mm

$R_{cu} f_y = 25 - 410 \text{ mm}$

Area of footing = 6.027 m<sup>2</sup>

Size of footing = 2500 x 2500

$q^3$ , Net pressure = 508.824 kN/m

depth = 600

Critical section,  $\frac{d}{2} = 300$

$$300 + 300 + 225 = 825 \text{ mm}$$

$$300 + 300 + 450 = 1050 \text{ mm}$$

$$\text{Shear force } V_u = q_n \left[ \text{Area of footing} - (0.3 + d)^2 \right]$$

$$= 505.824 \left[ 2.5 \times 2.5 - (0.3 + 0.6)^2 \right]$$

$$V_u = 2751.68$$

Normal shear stress  $T_v = \frac{V_u}{b d}$

$b$  = perimeter of Critical section

$d$  = effective span depth

$$T_v = \frac{2751.68 \times 10^3}{(2 \times (825) + 2(1050)) \times 600}$$

$$T_v = 1.223 \text{ N/mm}^2$$

Permissible shear stress

$$T_v' = k_s \times T_c$$

$k_s = (0.5 + \beta_c)$  but not greater than 1

$\beta_c$  = Ratio of shorter to longer side of columns

$$T_c = 0.25 \sqrt{f_{ck}}$$

$$k_s = 1$$

$$T_c' = 0.25 \sqrt{25} = 1.25 \text{ N/mm}^2$$

$$T_v = 1.223 \text{ N/mm}^2$$

$$T_v \leq T_v'$$

Hence depth assumed is ok ✓

Checking for  $f_b$  with actual size of footing

Unit weight of concrete =  $24 \text{ kN/m}^3$

Unit weight of soil =  $1.091 \times 10^{-6} \text{ kN/m}^3$

Actual pressure footing below

$$q = \frac{(1200 \times 2.5 \times 2.5) + (24 \times 0.660) + (10^6 \times 0.66)}{10^6}$$

$$q = 214.94 \text{ kN/m}^2$$