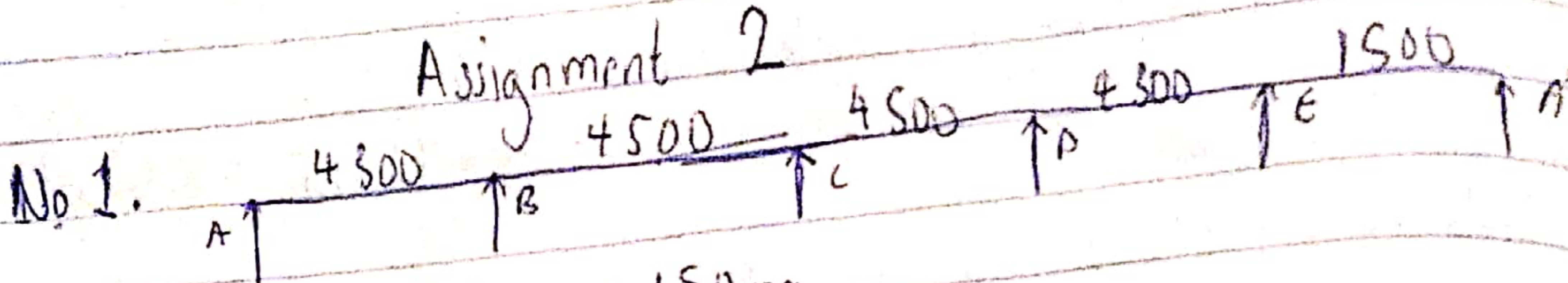


Assignment 2



Assuming thickness = 150 mm
 $f_{cu} = 25 \text{ N/mm}^2$
 $f_y = 410 \text{ N/mm}^2$

Slab loading

Slab weight = $0.15 \times 24 = 3.6 \text{ kN/m}^2$
 Partition = 1.0 kN/m^2
 Finishes = 1.2 kN/m^2
 Total Gk = 5.8 kN/m^2

$$D.L = 1.4(5.8) + 1.6(3.0) \rightarrow \text{for classroom} = 13 \text{ kN/m}^2$$

Beam Loading

Self weight of beam = $0.225 \times 0.6 \times 24 = 5.24 \text{ kN/m}^2$
 Finishes = 1.2 kN/m^2
 Wall loading = $3 \times 3.47 = 10.41 \text{ kN/m}^2$
 Total Gk = 14.85

$$D.L = 1.4(14.85) = 20.79 \text{ kN/m}^2$$

Slab load on beam in longer direction = $\frac{1}{2} w l_x (1 - \frac{1}{3} k)$

$$k = \frac{l_y}{l_x}$$

$$\frac{4300}{4000} = 1.075$$

$$\frac{4500}{4000} = 1.125$$

$$\frac{1}{2} \times 13 \times 4.3 \left(1 - \frac{1}{3 \times (1.075)^2} \right) = 19.89 \text{ kN/m}^2$$

$$\frac{1}{2} \times 13 \times 4.5 \left(1 - \frac{1}{3 \times (1.125)^2} \right) = 21.55 \text{ kN/m}^2$$

Slab loading on beam in shorter direction = $\frac{1}{3} wL^2$
 $= \frac{1}{3} \cdot 18 \times 1.5^2 = 6.5 \text{ kN/m}^2$

Total load = $19.89 + 20.79 = 40.68 \text{ kN/m}$
 $= 21.55 + 20.79 = 42.34 \text{ kN/m}$
 $= 6.5 + 20.79 = 27.29 \text{ kN/m}$

Distribution factor

$K_{AB} = 1$

$K_{BA} = \frac{1/L_{BA}}{\frac{1}{L_{BA}} + \frac{1}{L_{BC}}} = \frac{1/4.5}{1/4.5 + 1/4.5} = 0.51$

$K_{BC} = 1 - 0.51 = 0.49$

$K_{CB} = \frac{1/4.5}{1/4.5 + 1/4.5} = 0.5$

$K_{CD} = 1 - 0.5 = 0.5$

$K_{DC} = 0.49$

$K_{DE} = 0.51$

$K_{ED} = \frac{1/4.5}{1/4.5 + 1/1.5} = 0.26$

$K_{EA} = 1 - 0.26 = 0.74$

$K_{AE} = 1$

F.E.M

U.D.L = $\frac{wL^2}{12}$

1.) $\frac{40.68 \times 4.5^2}{12} = 62.68 \text{ kN/m}$

2. $\frac{42.34 \times 4.5^2}{12} = 71.45 \text{ kN/m}$

3. $\frac{27.29 \times 1.5^2}{12} = 5.1 \text{ kN/m}$

	A	B		C		D		E		A'
	AB	BA	BC	CB	CC	DC	DE	ED	EA'	A'A'
DF	0	1	0.51	0.49	0.5	0.5	0.47	0.51	0.26	0.77
FEM	-62.68	62.68	-71.45	71.45	-71.45	71.45	-62.68	62.68	-51	51
DBM	-62.68	-8.77	0	0	8.77	51.58	-5.1	5.1	-5.1	5.1
BM	62.68	8.77	0	0	-8.77	-57.68	5.1	-5.1	5.1	-5.1
DM	0	62.68	4.95	4.50	0	0	-4.50	4.49	14.98	4.26
TM	2.255	31.34	0	2.15	-2.15	0	7.44	-2.24	-2.55	-2.15
OBM	2.235	31.34	0	0	-7.49	-4.79	-21.308	21.303	0	0
BM	-2.235	-31.34	0	0	7.49	4.79	21.308	-21.303	0	0
DM	0	-2.235	-15.98	-15.36	0	0	3.67	3.82	1.25	3.54
TM	-7.99	-1.12	0	-7.67	1.84	0	0.63	1.91	10.66	1.77
OBM	-7.99	-1.12	-5.85	0.63	12.57	1.77	0	0	0	0
BM	7.99	1.12	5.85	-0.63	-12.57	-1.77	0	0	0	0
DM	0	7.99	0.57	0.55	2.93	2.93	-0.31	-0.32	-3.28	-4.24
TM	0.24	3.40	1.47	0.28	-0.10	1.47	4.64	-0.16	0.89	-4.65
OBM	0.29	4.87	0.12	-0.17	-1.05	-4.65	0	0	0	0
BM	-0.29	-4.87	-0.12	0.17	1.05	4.65	0	0	0	0
DM	0	-0.29	-2.49	-2.59	-0.06	-0.06	0.09	0.01	0.27	0.18
Σ	0	22.88	-82.88	69.06	-69.06	72.06	-72.06	45.47	-45.47	0

OBM
BM
DM
TM

Moments

- $M_A = 0 \text{ kNm}$
- $M_B = 82.88 \text{ kNm}$
- $M_C = 69.06 \text{ kNm}$
- $M_D = 72.06 \text{ kNm}$
- $M_E = 45.47$
- $M_{A'} = 0 \text{ kNm}$

Free Moment

$$F_{01} = \frac{wl^3}{8} = \frac{40.68 \times 4.5^3}{8} = 94.02 \text{ kN/m}^2$$

$$F_{12} = \frac{42.54 \times 4.5^3}{8} = 107.17 \text{ kN/m}^2$$

$$F_{23} = \frac{27.29 \times 1.5^3}{8} = 7.68 \text{ kN/m}^2$$

Span Moment

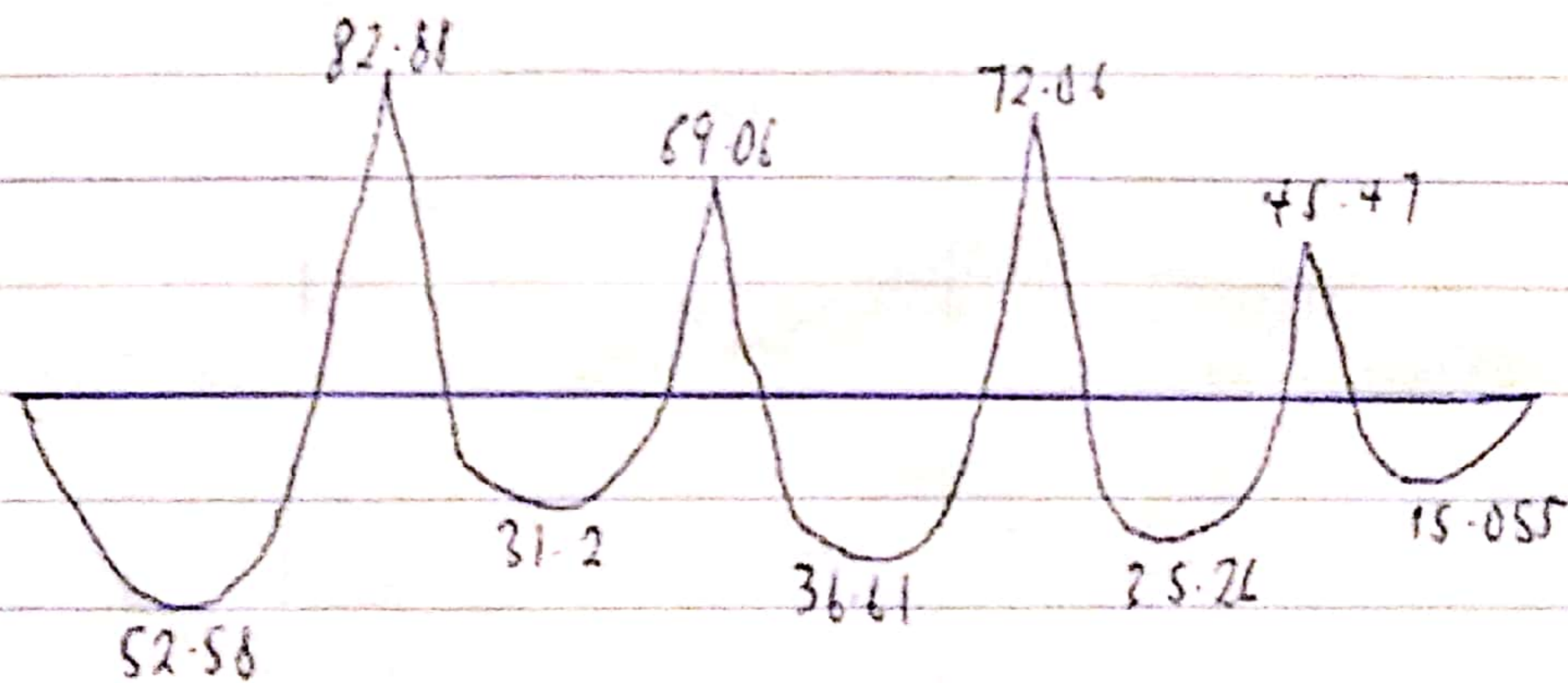
$$M_{AB} = M^F - \left(\frac{M_A + M_B}{2} \right) = 94.02 - \left(\frac{0 + 82.88}{2} \right) = 52.58 \text{ kNm}$$

$$M_{BC} = M^F - \left(\frac{M_B + M_C}{2} \right) = 107.17 - \left(\frac{82.88 + 69.06}{2} \right) = -31.2 \text{ kNm}$$

$$M_{CD} = M^F - \left(\frac{M_C + M_D}{2} \right) = 107.17 - \left(\frac{69.06 + 12.06}{2} \right) = -36.61 \text{ kNm}$$

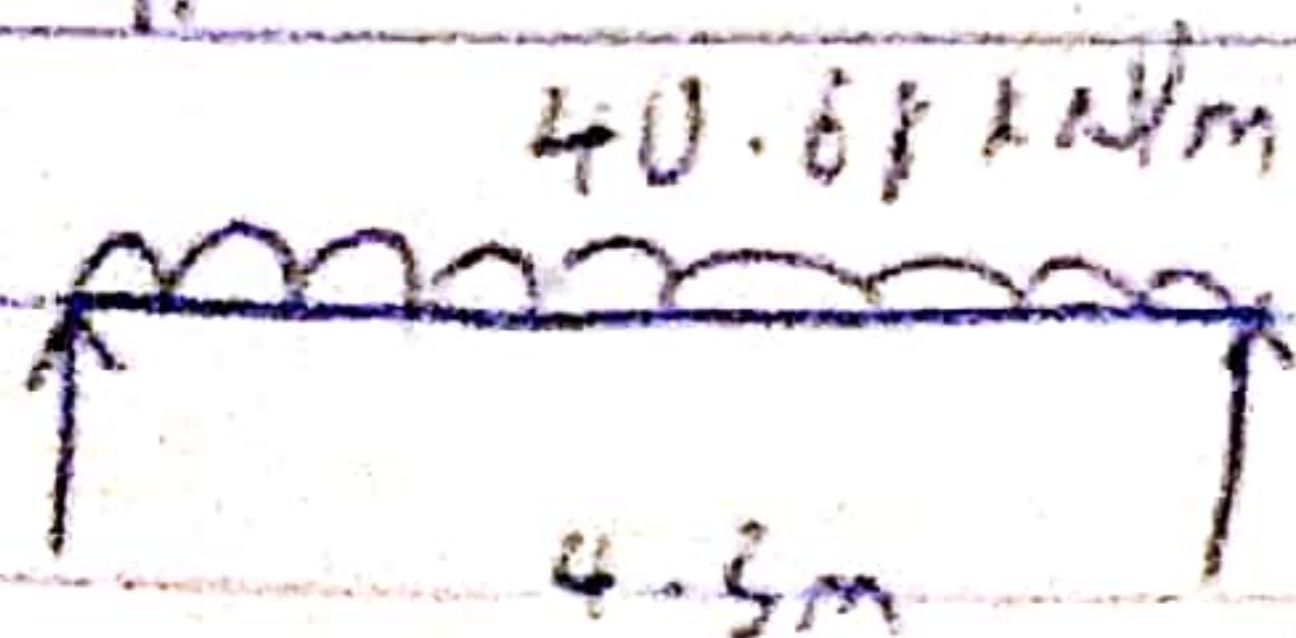
$$M_{DE} = M^F - \left(\frac{M_D + M_E}{2} \right) = 94.02 - \left(\frac{72.06 + 45.47}{2} \right) = -35.26 \text{ kNm}$$

$$M_{EA} = M^F - \left(\frac{M_E + M_{A'}}{2} \right) = 7.68 - \left(\frac{45.47 + 0}{2} \right) = -15.055 \text{ kNm}$$



Shear Force

For A



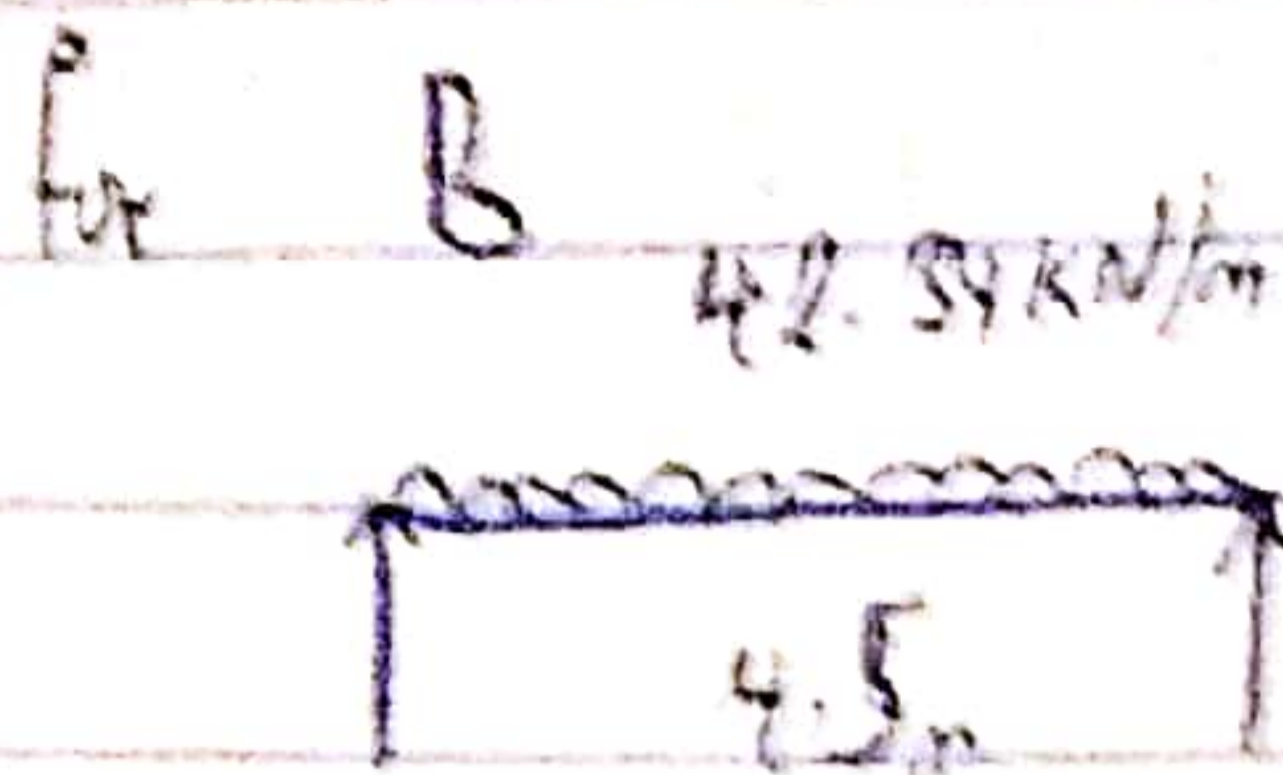
$$V_A = \frac{wl}{2} = V_B$$

$$= \frac{40.68 \times 4.5}{2}$$

$$= 87.462 \text{ kN}$$

$$V_{AB} = V_c + \left(\frac{M_A - M_B}{L} \right) = 87.462 + \left(\frac{0 - 82.88}{4.3} \right) = 81.19$$

$$V_{BA} = wL - V_{AB} = (40.68 \times 4.3) - 81.19 = 106.73 \text{ kN}$$

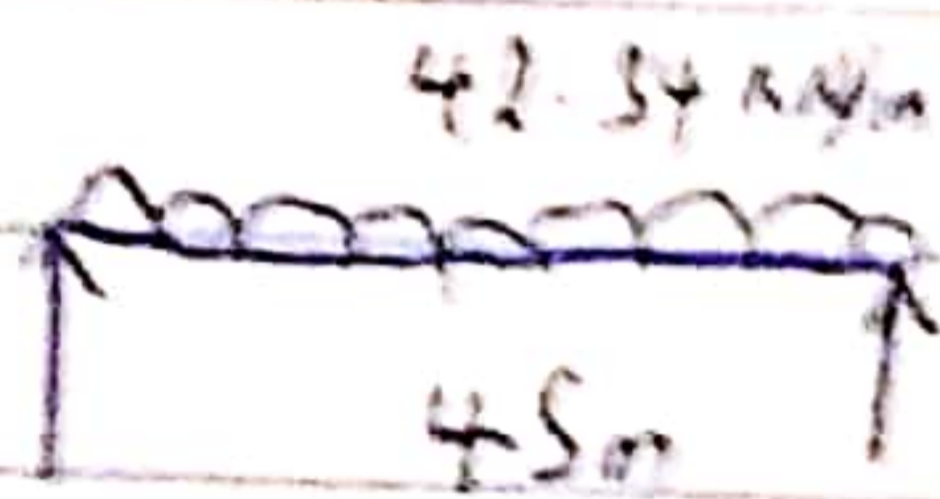


$$V_{DE} = \frac{wl}{2} = V_c = \frac{42.34 \times 4.5}{2} = 95.27 \text{ kN}$$

$$V_{BC} = V_B + \left(\frac{M_B + M_C}{L} \right) = 95.27 + \left(\frac{82.88 + 69.06}{4.5} \right) = 129.03 \text{ kN}$$

$$V_{CB} = (42.34 \times 4.5) - 129.03 = 61.5 \text{ kN}$$

For C



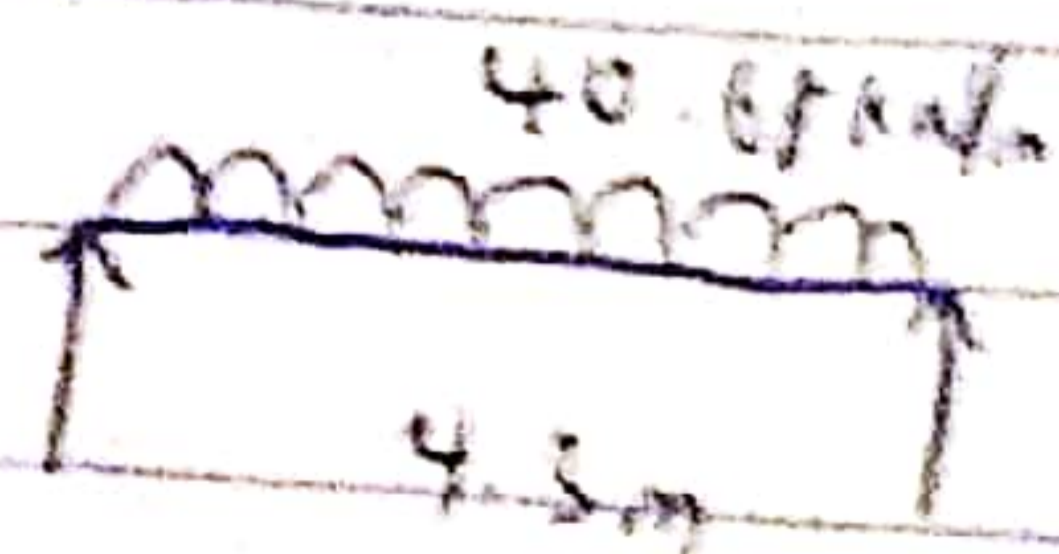
$$V_c = \frac{wl}{2} = V_D$$

$$= \frac{42.34 \times 4.5}{2} = 95.27 \text{ kN}$$

$$V_{CD} = 95.27 + \left(\frac{69.06 + 72.06}{4.5} \right) = 126.63 \text{ kN}$$

$$V_{DC} = (42.34 \times 4.5) - 126.63 = 63.19 \text{ kN}$$

For D



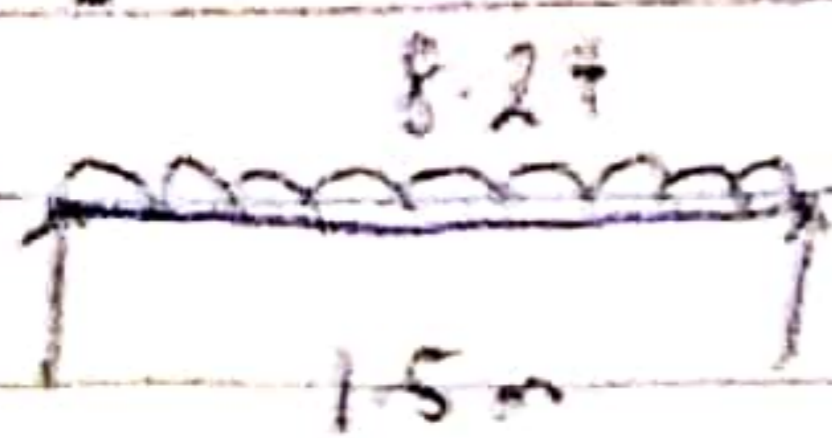
$$V_D = \frac{wl}{2} = V_E$$

$$= \frac{40.68 \times 4.3}{2} = 87.462$$

$$V_{DE} = V_D - \left(\frac{72.06 + 45.97}{4.3} \right) = 60.73 \text{ kN}$$

$$V_{ED} = wL - V_{DE} = (40.68 \times 4.3) - 60.73 = 114.79 \text{ kN}$$

For E



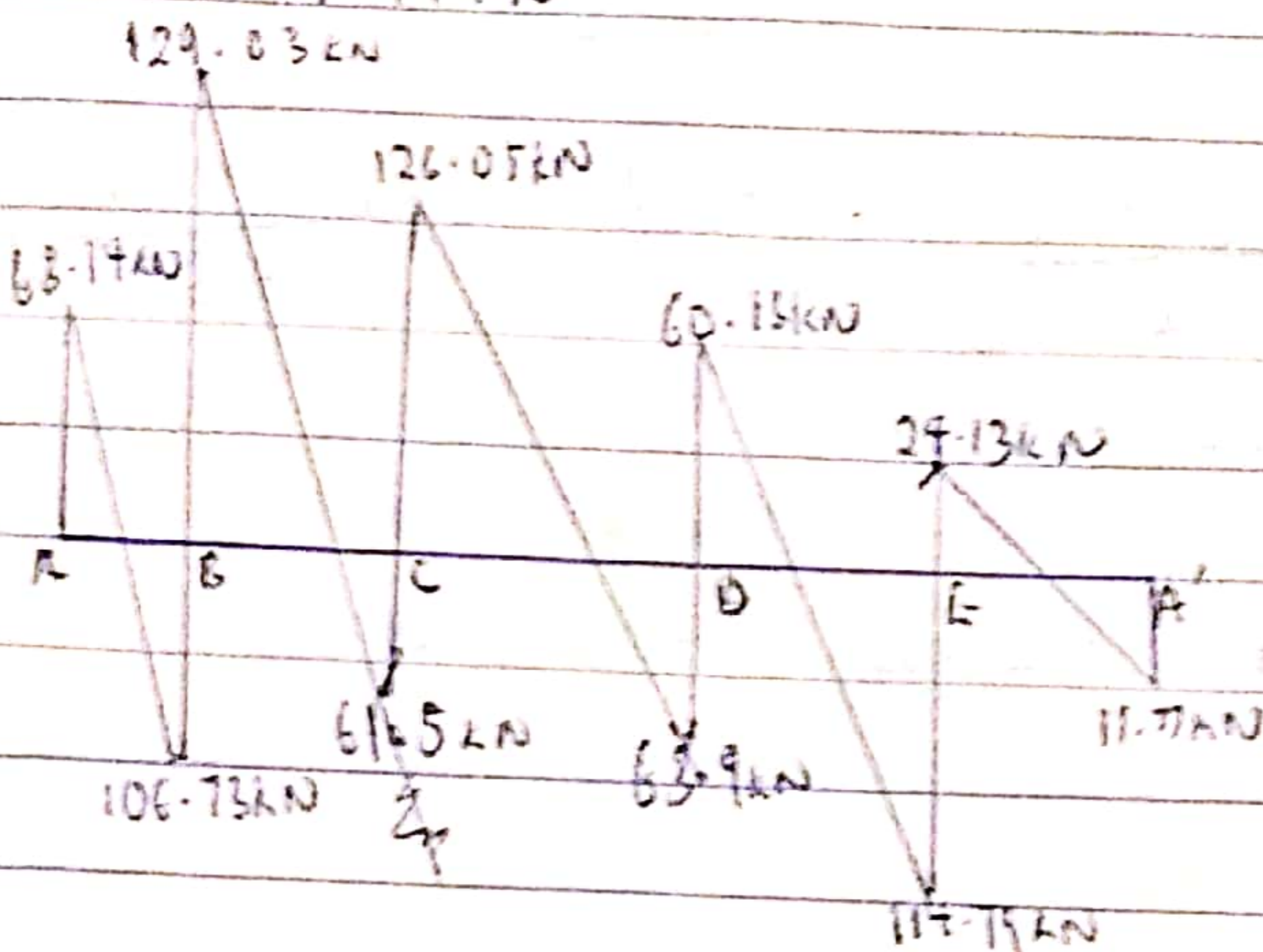
$$V_E = wL/2 = V_{A'}$$

$$= \frac{8.24 \times 1.5}{2} = 6.18 \text{ kN}$$

$$V_{EA'} = V_E - \left(\frac{m_E + m_{A'}}{L} \right) = 6.18 - \left(\frac{45.47 + 0}{1.5} \right) = 24.13 \text{ kN}$$

$$V_{A'E} = (8.24 \times 1.5) - 24.13$$

$$= 11.77 \text{ kN}$$



Number 2

Base design

$$N = 1200 \text{ kN}$$

$$\text{Strength} = 25 - 410 \text{ N/mm}^2$$

$$f_b = 150 \text{ kN/m}^2$$

$$\text{Area of base required} = \frac{N \times 1.1}{\lambda \times f_b} \quad \lambda = 1.46$$

$$\frac{1200 \times 1.1}{1.46 \times 150} = 6.027 \text{ m}^2$$

$$\sqrt{6.027} = 2.45 \text{ m} \approx 2.5$$

$$\text{Net pressure, } F_{net} = \frac{N \times 1.1}{B} = \frac{1200 \times 1.1}{2.5} - \frac{24 \times 0.66}{1.4}$$

$$= 505.824 \text{ kN/m}$$

$$\text{Moment, } M = \frac{F_{net} l^2}{2}$$

$$\text{where } L = \frac{1}{2}(b-h)$$

$$L = \frac{1}{2}(2.5 - 0.225) = 1.137 \approx 1.14 \text{ m}$$

$$\therefore M = \frac{505.824 \times 1.14^2}{2} = 328.62 \text{ kNm}$$

$$d = h - \text{cover} - \frac{1}{2} \phi$$
$$= 660 - 50 - 10 = 600 \text{ mm}$$

$$k = \frac{M}{bd^2 f_{cu}} = \frac{328.62 \times 10^6}{1000 \times 600^2 \times 25} = 0.037$$

$$R_u = 0.5 + \frac{\sqrt{0.25 + \frac{0.037}{0.9}}}{0.9} = 0.96 > 0.95$$

$$z = R_{ud} = 0.95 \times 600 = 570 \text{ mm}$$

$$A_s = \frac{M}{0.95 f_y z} = \frac{328.62 \times 10^6}{0.95 \times 410 \times 570} = 1790.46 \text{ mm}^2$$

Provide Y 25 @ 300 c/c (1600)

Punching Shear

$$\text{Column size} = 225 \times 450 \text{ mm}$$

$$f_{cu} - f_y = 25 - 410 \text{ mm}$$

$$\text{Area footing} = 6.027 \text{ m}^2$$

$$\text{Size of footing} = 2500 \times 2500$$

$$q_n, \text{ Net pressure} = 505.824 \text{ kNm}$$

$$\text{depth} = 600$$

$$\text{critical section, } d/2 = 300$$

$$300 + 300 + 225 = 825 \text{ mm}$$

$$300 + 300 + 450 = 1050 \text{ mm}$$

$$\text{Shear Force } V_R = q_n \times (\text{Area of footing} - (0.3 + d)^2)$$
$$= 505.824 (2.5 \times 2.5 - (0.3 + 0.6/2)^2)$$

$$V_u = 2751.68 \text{ kN}$$

$$\text{Normal shear stress, } \bar{\tau}_v = \frac{V_u}{b d}$$

b = perimeter of critical section

d = effective depth

$$\bar{\tau}_v = \frac{2751.68 \times 10^3}{(2 \times (825) + 2(1050)) \times 600}$$

$$\bar{\tau}_v = 1.223 \text{ N/mm}^2$$

Permissible shear stress

$$\bar{\tau}_c' = k_s \times \bar{\tau}_c$$

$k_s = (0.5 + \beta_c)$ but not greater than 1

β_c = Ratio of shorter to larger side of column

$$\bar{\tau}_c = 0.25 \sqrt{f_{ck}}$$

$$k_s = 1$$

$$\bar{\tau}_c' = 0.25 \sqrt{25} = 1.25 \text{ N/mm}^2$$

$$\bar{\tau}_v = 1.223 \text{ N/mm}^2$$

$$\bar{\tau}_v \leq \bar{\tau}_c'$$

Here depth assumed is ok

Checking for P_b with actual size of footing

Unit weight of concrete = 24 kN/m^3

Unit weight of soil = $1.091 \times 10^{-6} \text{ kN/m}^3$

Actual pressure footing below

$$q = (1200 \times 2.5) + (24 \times 0.620) + (1.091 \times 10^6 \times 0.68)$$

$$q = 214.94 \text{ kN/m}^2$$