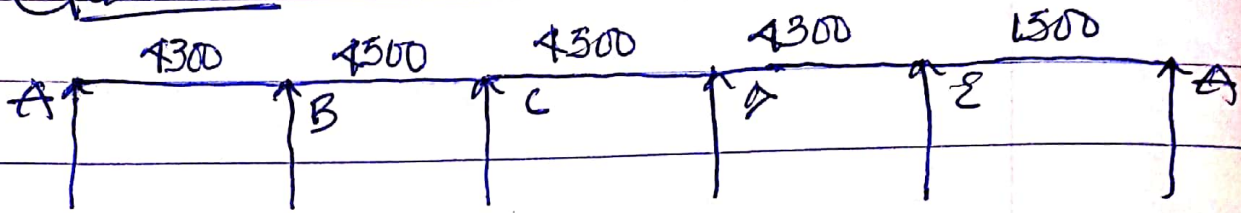


# Assignment 2

## Question 1



Assuming Thickness; 150 mm

$$f_{cu} = 25 \text{ N/mm}^2$$

$$f_y = 410 \text{ N/mm}^2$$

Slab loading

$$\text{Slab weight} = 0.15 \times 24 = 3.6 \text{ kN/m}^2$$

$$\text{Partitions} = 1.0 \text{ kN/m}^2$$

$$\text{Finishes} = 1.2 \text{ kN/m}^2$$

$$\text{Total G.K} = 5.8 \text{ kN/m}^2$$

$$Q.K = 3.0 \text{ (Assumed for classroom)}$$

$$\Delta.L = 1.4(5.8) + 1.6(3.0) = 13 \text{ kN/m}^2$$

Beam loading

$$\text{Self weight of beams} = 0.225 \times 0.6 \times 24 = 3.24 \text{ kN/m}^2$$

$$\text{finishes} = 1.2 \text{ kN/m}^2$$

$$\text{Klau load} = 3 \times 3.44 = 10.32 \text{ kN/m}^2$$

$$\text{Total G.K} = 14.85 \text{ kN/m}^2$$

$$\Delta.L = 1.4(14.85) = 20.79 \text{ kN/m}^2$$

Slab load on beam in longer direction =  $\frac{1}{2} w l_x \left(1 - \frac{1}{3K^2}\right)$

$$K = \frac{l_y}{l_x} = \frac{4300}{4000} = 1.075$$

$$\frac{4500}{4000} = 1.125$$

$$\frac{1}{2} \times 13 \times 4.3 \left(1 - \frac{1}{3 \times (1.075)^2}\right) = 19.89 \text{ kN/m}^2$$

$$\frac{1}{2} \times 13 \times 4.5 \left(1 - \frac{1}{3 \times (1.125)^2}\right) = 21.55 \text{ kN/m}^2$$

Slab load on beam in shorter direction =  $\frac{1}{3} w l_x$

$$= \frac{1}{3} \times 13 \times 1.5 = 6.5 \text{ kN/m}^2$$

$$\text{Total Load} = 19.89 + 20.79 = 40.68 \text{ kN/m}^2$$

$$= 21.55 + 20.79 = 42.34 \text{ kN/m}^2$$

$$= 6.5 + 20.79 = 27.29 \text{ kN/m}^2$$

△ Distribution factor:

$$K_{AB} = 1$$

$$K_{BA} = \frac{K_{BA}}{K_{BA} + K_{BC}} = \frac{K_{AB}}{K_{AB} + K_{BC}} = \frac{1}{1 + 1.125} = 0.51$$

$$K_{BC} = 1 - 0.51 = 0.49$$

$$K_{CB} = \frac{\frac{1}{4.5}}{\frac{1}{4.5} + \frac{1}{4.5}} = 0.5$$

$$K_{CA} = 1 - 0.5 = 0.5$$

$$K_{AC} = 0.49$$

$$K_{AE} = 0.51$$

$$K_{EA} = \frac{\frac{1}{4.3}}{\frac{1}{4.3} + \frac{1}{1.5}} = 0.26$$

$$K_{EA} = 1 - 0.26 = 0.74$$

$$K_{AE} = 1$$

F. E. M

$$U_{DL} = \frac{wL^2}{12}$$

$$\Rightarrow \frac{10.68 \times 4.3^2}{12} = 62.68 \text{ kNm}$$

$$\Rightarrow \frac{12.34 \times 4.5^2}{12} = 71.45 \text{ kNm}$$

$$\Rightarrow \frac{27.29 \times 1.5^2}{12} = 5.1 \text{ kNm}$$

	A	B	C	A	E	A
	AB	BA BC	CB CA	AC AE	EA EA	AA A
A.F	0 1	0.51 0.49	0.5 0.5	0.49 0.51	0.26 0.74	1 0
FEM	-62.68	62.68 -71.15	-71.15 -71.15	71.15 -62.68	62.68 -5.1	5.1
OBM	-62.88	-8.77	0	8.77	57.58	-5.1
BM	62.68	8.77	0	-8.77	-57.58	5.1
DM	0 62.68	← 4.97 4.30	← 0 0	← 4.30 -4.97	← 1.44 -2.61	5.1
TM	2.235	31.34 0	2.15 -2.15	0 -7.49	-2.49 -2.55	-2.31
OBM	2.235	31.34	0	-7.49	-4.79	-21.305
BM	-2.235	-31.34	0	7.49	4.79	21.305
DM	0 -2.235	← -15.88 -15.36	← 0 0	← 3.67 3.82	← 1.25 3.54	2.30 0
TM	-7.49	-1.12 0	-7.49 1.57	0 0.63	1.91 10.66	1.77
OBM	-7.49	-1.12	-3.55	0.63	12.57	1.77
BM	7.49	1.12	3.55	-0.63	-12.57	-1.77
DM	0 7.49	← 0.57 0.53	← 2.13 2.43	← -0.31 -0.32	← -3.27 -9.29	-1.77 0
TM	0.24	3.40 1.47	0.28 -0.16	1.47 -1.64	-0.16 -0.87	-1.65
OBM	0.24	4.57	0.28	-0.17	-1.05	-4.65
BM	-0.24	-4.57	-0.12	0.17	1.05	4.65
DM	0 -0.29	← -2.48 -2.39	← -0.06 -0.06	← 0.06 0.09	← 0.27 0.78	4.65 0
<del>OBM</del>						
Sum(Σ) =	0	22.88 -82.88	69.05 -69.05	72.06 -72.06	45.16 -45.16	0

Moments:

$$M_A = 0 \text{ kNm}$$

$$M_B = 82.88 \text{ kNm}$$

$$M_C = 69.06 \text{ kNm}$$

$$M_D = 72.06 \text{ kNm}$$

$$M_E = 45.47 \text{ kNm}$$

$$M_F = 0 \text{ kNm}$$

Free Moment:

$$UqL = \frac{wL^2}{8}$$

$$i) \frac{40.68 \times 4.3^2}{8} = 98.02 \text{ kNm}^2$$

$$ii) \frac{42.34 \times 4.5^2}{8} = 107.17 \text{ kNm}^2$$

$$iii) \frac{27.28 \times 1.5^2}{8} = 8.27 \text{ kNm}^2$$

Span Moment:

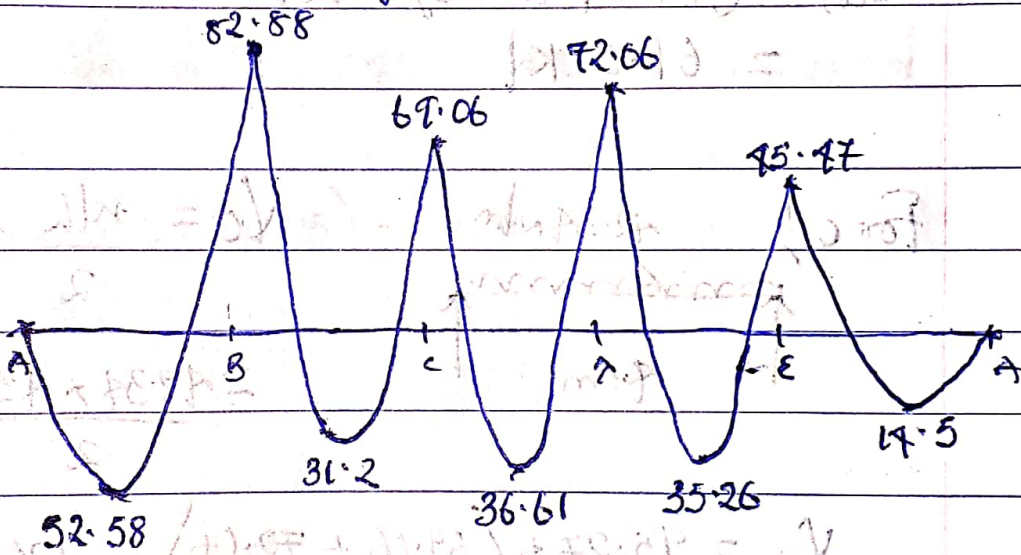
$$M_{AB} = M^F - \left( \frac{M_A + M_B}{2} \right) = 98.02 - \left( \frac{0 + 82.88}{2} \right) = 52.58 \text{ kNm}$$

$$M_{BC} = M^F - \left( \frac{M_B + M_C}{2} \right) = 107.17 - \left( \frac{82.88 + 69.06}{2} \right) = 31.2 \text{ kNm}$$

$$M_{CB} = M^R - \left( \frac{M_C + M_A}{2} \right) = 107.17 - \left( \frac{67.07 + 72.06}{2} \right) = 36.61 \text{ kNm}$$

$$M_{DE} = M^R - \left( \frac{M_D + M_E}{2} \right) = 94.02 - \left( \frac{72.06 + 45.47}{2} \right) = 35.26 \text{ kNm}$$

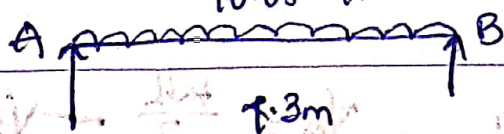
$$M_{EA} = M^F - \left( \frac{M_E + M_A}{2} \right) = 8.24 - \left( \frac{45.47 + 0}{2} \right) = -14.5 \text{ kNm}$$



BMD

Shear Force:

For A:  $40.68 \text{ kN/m}^2$   $V_A = \frac{wL}{2} = \frac{1}{2}$



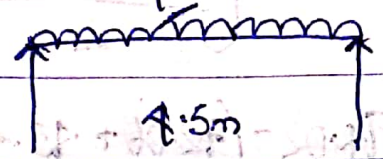
$$= \frac{40.68 \times 4.3}{2} = 87.462 \text{ kN}$$

$$V_{AB} = V_A + \left( \frac{M_A - M_B}{L} \right) = 87.462 + \left( \frac{0 - 82.88}{4.3} \right) = 68.19$$

$$V_{BA} = wL - V_{AB}$$

$$= (40.68 \times 4.3) - 68.19 = 106.73 \text{ kN}$$

For B:  $42.34 \text{ kNm}$



$$V_B = \frac{wL}{2} = V_C$$

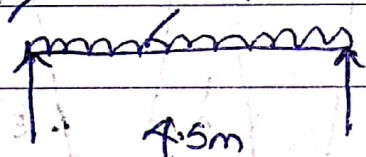
$$= \frac{42.34 \times 4.5}{2} = 95.27 \text{ kN}$$

$$V_{BC} = V_B + \left( \frac{M_B + M_C}{L} \right) = 95.27 + \left( \frac{82.68 + 69.06}{4.5} \right) = 129.03 \text{ kN}$$

$$V_{CB} = (42.34 \times 4.5) - 129.03$$

$$= 61.57 \text{ kN}$$

For C:  $42.34 \text{ kNm}$



$$V_C = \frac{wL}{2} = V_A$$

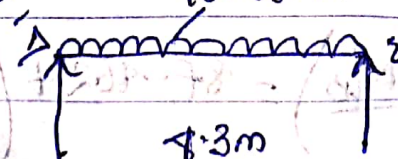
$$= \frac{42.34 \times 4.5}{2} = 95.27 \text{ kN}$$

$$V_{CD} = 95.27 + \left( \frac{69.06 + 72.06}{4.5} \right) = 126.63 \text{ kN}$$

$$V_{DC} = (42.34 \times 4.5) - 126.63$$

$$= 63.17 \text{ kN}$$

For D:  $40.68 \text{ kNm}$



$$V_D = \frac{wL}{2} = V_E$$

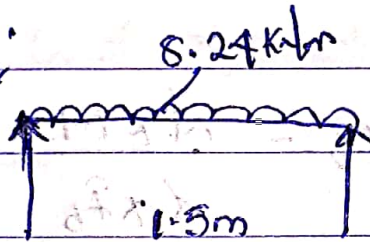
$$= \frac{40.68 \times 4.3}{2} = 87.46 \text{ kN}$$

$$V_{DE} = 87.46 - \left( \frac{72.06 + 75.47}{4.3} \right) = 60.13 \text{ kN}$$

$$V_{E2} = (40.68 \times 1.5) - 60.13$$

$$= 11.77 \text{ kN}$$

For  $\Sigma$ :



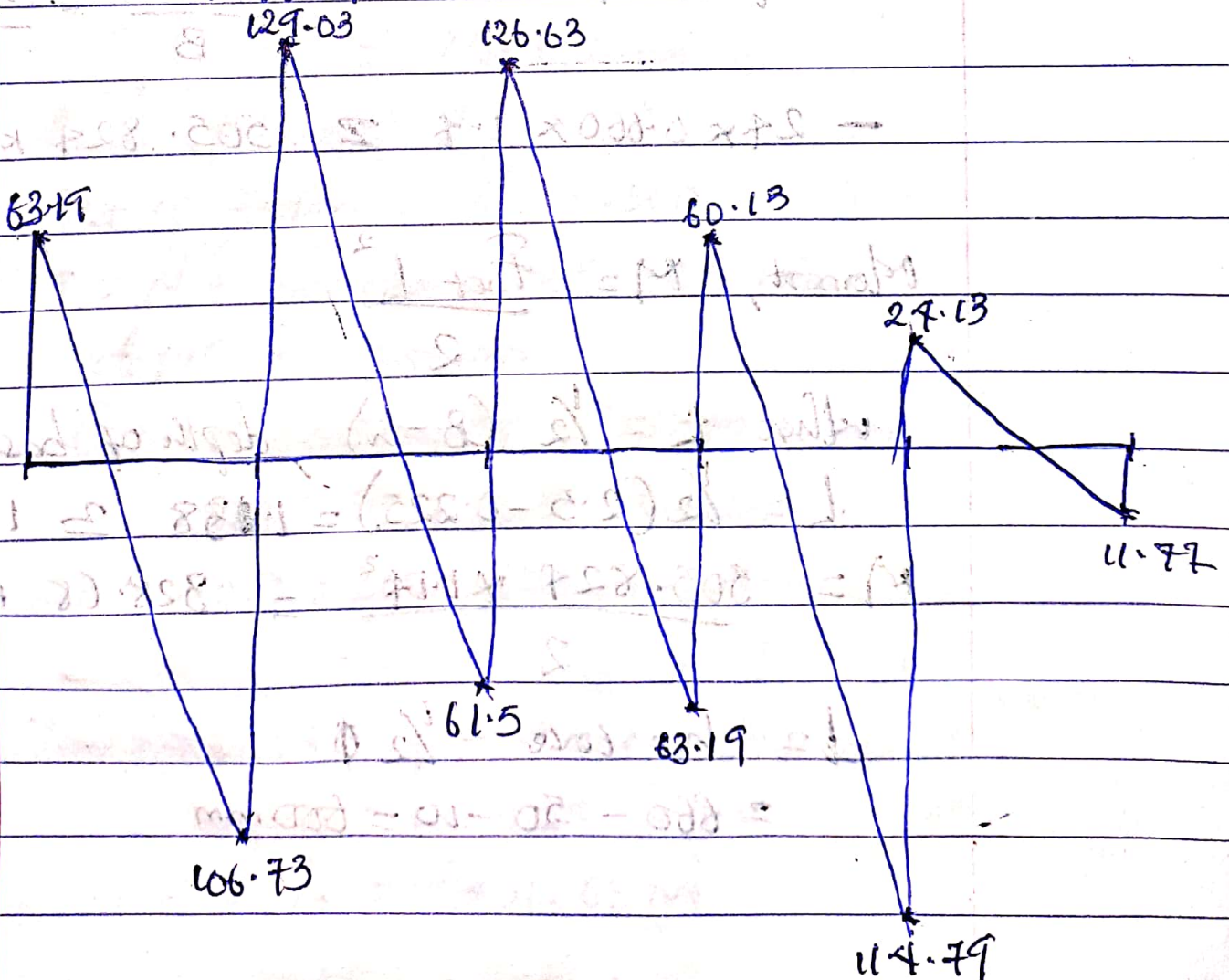
$$V_E = \frac{wL}{2} = V_A$$

$$= \frac{8.24 \times 1.5}{2} = 6.18 \text{ kN}$$

$$V_{E1} = 6.18 + \left( \frac{45.47 \times 1.5}{1.5} \right) = 24.13 \text{ kN}$$

$$V_{E2} = (8.24 \times 1.5) - 24.13$$

$$= 11.77 \text{ kN}$$





## Question 2

Base design

$$N = 1200 \text{ kN}$$

$$\text{Strength} = 25 - 410 \text{ N/mm}^2$$

$$f_b = 150 \text{ kN/m}^2$$

$$\text{Area of base req} = \frac{N \times 1.1}{1 \times f_b} \quad L = 1.46$$

$$= \frac{1200 \times 1.1}{1.46 \times 150} = 6.027 \text{ m}^2$$

$$B = \sqrt{6.027} = 2.45 \text{ m} \approx 2.5 \text{ m}$$

$$\text{Net Pressure, } F_{\text{net}} = \frac{N \times 1.1}{B} = \frac{1200 \times 1.1}{2.5}$$

$$= 24 \times 0.660 \times 1.1 = 505.824 \text{ kNm}$$

$$\text{Moment, } M = \frac{F_{\text{net}} L^2}{2}$$

where  $L = \frac{1}{2}(B - h)$ , depth of base = 660

$$L = \frac{1}{2}(2.5 - 0.225) = 1.138 \approx 1.14 \text{ m}$$

$$M = \frac{505.824 \times 1.14^2}{2} = 328.68 \text{ kNm}$$

$$d = h - \text{cover} - \frac{1}{2} \phi$$

$$= 660 - 50 - 10 = 600 \text{ mm}$$

$$K = \frac{M}{bd^2 f_{cu}} = \frac{328.68 \times 10^6}{1000 \times 600^2 \times 25} = 0.037$$

$$\lambda_a = 0.5 + \sqrt{0.25 + \frac{0.037}{0.9}} = 0.96 > 0.95$$

$$Z = \lambda_a d = 0.95 \times 600 = 570 \text{ mm}$$

$$A_s = \frac{M}{0.95 f_y Z} = \frac{328.68 \times 10^6}{0.95 \times 410 \times 570} = 1480.44 \text{ mm}^2$$

Provide 725 @ 300 c/c (1640)

Punching Shear: (2.5 x 2.5) = 2.5

Column Size = 225 x 450 mm

$f_{cu}, f_y = 25 - 410 \text{ mm}$

Area footing = 6.027 m<sup>2</sup>

Size of footing = 2500 x 2500

$q = \text{Net Pressure} = 505.824 \text{ kN/m}^2$

depth = 600 mm

Critical Section,  $\frac{d}{2} = 300 \text{ mm}$

$$300 + 300 + 225 = 825 \text{ mm}$$

$$300 + 300 + 450 = 1050 \text{ mm}$$

$$\text{Shear force } V_n = q \times [\text{Area of footing} - (0.3 + d)^2]$$

$$V_n = 505.824 [2.5 \times 2.5 - (0.3 + 0.6)^2]$$

$$V_n = 2751.68 \text{ kN}$$

Normal Shear Stress  $\tau_v = \frac{V_u}{bd}$

$b =$  perimeter of cross section

$d =$  effective span / depth

$$\tau_v = \frac{2751.68 \times 10^3}{\dots}$$

$$\tau_v = \frac{2751.68 \times 10^3}{[(2 \times 825) + 2 \times 1050] \times 600}$$

$$\tau_v = 1.223 \text{ N/mm}^2$$

Permissible Shear Stress;

$$\tau_c' = K_s \times \tau_c$$

$K_s = (0.5 + \rho_c)$  but not greater than 2

$\rho_c =$  Ratio of shorter to larger side of column

$$\tau_c = 0.25 \sqrt{f_c k}$$

$$K_s = 1$$

$$\tau_c' = 0.25 \sqrt{25} = 1.25 \text{ N/mm}^2$$

$$\tau_v = 1.223 \text{ N/mm}^2$$

there depth assumed is OK

Checking for  $F_b$  with actual size of footing;

char weight of concrete =  $24 \text{ kN/m}^3$

char weight of soil =  $1.091 \times 10^{-6} \text{ kN/m}^3$

Actual pressure footing;

$$q = (1200 \times 2.5 \times 2.5) + (24 \times 0.660) + (1.091 \times 10^{-6} \times 0.660)$$

$$q = 218.94 \text{ kN/m}^2$$