

- a) To design for Safety  
 b.) The design must be economical  
 c.) The deformation of the structure must not impure with the intensity of the structure.

1b Limit state designs considers the disadvantages of load factor design and other failure that can cause the structure to be structurally unfit while Elastic design is a method of analysis which the design of a structural member is based on a linear stress - strain relationship assuming that the working stress are only a fraction of the elastic limit of the material.

### STAIR CASE DESIGN

$$\text{Slope factor} = \frac{\sqrt{R^2 + T^2}}{T} = \frac{\sqrt{150^2 + 275^2}}{275} = 1.14$$

\* Load Analysis

$$\begin{aligned}
 \text{A. WAIST} &= R \times 24 \text{ kN/m}^2 \\
 &= 0.15 \times 24 = 3.6 \text{ kN/m}^2
 \end{aligned}$$

$$\text{B. FINISHES} = 1.2 \text{ kN/m}^2$$

$$\begin{aligned}
 \text{C. STEPS} &= T \times \frac{1}{2} \times 24 \text{ kN/m}^2 \\
 &= 0.275 \times 0.5 \times 24 = 3.3 \text{ kN/m}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{D. G.K} &= ((A+B) \times S_f) + C \\
 &= (4.8 \times 1.14) + 3.3 \\
 &= 8.77 \text{ kN/m}
 \end{aligned}$$

$$\begin{aligned}
 \text{D.L.F} &= 1.4 \text{ G.K} + 1.6 \text{ Q.K} \\
 &= 1.4 (8.77) + 1.6 (1.5) \\
 &= 14.68 \text{ kN/m}^2
 \end{aligned}$$

$$\text{Span} = \text{Total} + 0.5(10+16) = (275 \times 12) + 0.5(225+225) = 3525$$

$$d = n - (\text{cover} = \frac{1}{2} \phi)$$

$$= 150 - 25 - 6 = 119 \text{ mm}$$

$$M = \frac{FL^2}{10} = \frac{14.68 \times 3525^2}{10} = 18.24 \text{ kNm}$$

$$k = \frac{M}{bd^2 F_{cr}} = \frac{1824 \times 10^6}{1000 \times 119^2 \times 25} = 0.052$$

$$I_g = 0.15 + \sqrt{0.25 - \frac{k}{0.9}} = 0.15 + \sqrt{0.25 - \frac{0.052}{0.9}} = 0.938$$

$$z = I_g d = 0.938 \times 119 = 111.622 \text{ mm}$$

$$A_s = \frac{M}{0.95 f_y z} = \frac{18.24 \times 10^6}{0.95 \times 410 \times 111.622} = 419.53$$

$$A_{s, \text{prov}} = 452 \text{ mm}^2$$

provide  $\phi 25$  @ ~~259~~ 259 c/c ( $A_{s, \text{prov}} = 452 \text{ mm}^2$ )

Deflection check

$$F_s = \frac{2}{3} \times \frac{1}{3} \times \frac{A_{s, \text{req}}}{A_{s, \text{prov}}} \times f_y \sqrt{}$$

$$F_s = \frac{2}{3} \times \frac{1}{3} \times \frac{419.53}{452} \times 250$$

$$= 154.69 \text{ N/mm}^2$$

$$M_i F = 0.156 + \frac{477 - 154.69}{120 \left( 0.9 + \frac{18.24 \times 10^6}{1000 \times 119^2} \right)} = 1.78 \text{ ,,}$$

$$d_{\text{req}} = \frac{\text{span}}{9f \times e_{br}} = \frac{3525}{1.78 \times 26} = 76.47 \text{ mm}$$

Since  $d_{\text{req}} < d$ , Deflection is OK

$$2a \quad P_1 = P_2 = P_3 = \frac{4300}{4000} = 1.075 < 2 = \text{Two way slab}$$

$$P_7 = P_8 = P_9 = \frac{4800}{4000} = 1.125 < 2 = \text{Two way slab}$$

$$P_4 = P_5 = P_6 = \frac{4300}{4000} = 1.075 > 2 = \text{Two way slab}$$

$$P_{10} = P_{11} = P_{12} = \frac{4000}{7500} = 2.667 > 2 = \text{Two way slab}$$

2b

Designing to  $P_2$

$$\frac{L_y}{L_x} = \frac{4300}{4000} = 1.075 = \underline{\underline{1.1}}$$

$$\text{Shortspan coefficient} = \underline{\underline{0.054}}$$

$$\text{Longspan coefficient} = \underline{\underline{0.058}}$$

Assuming specification of slab thickness = 178mm

$$P_{ux} = 25 \text{ N/mm}^2$$

$$P_y = 41000 \text{ N/mm}^2$$

$$DL = 1.4 G_k + 1.6 Q_k$$

$$G_k = \text{weight of slab} = 0.175 \times 24$$

$$\text{Partition} = 1.0$$

$$\text{Finishes} = 1.2$$

$$\underline{\underline{6.4 \text{ kN/m}^2}}$$

Assuming factory  
 $DL = (1.4 \times 6.4) + (1.6 \times 5)$   
 $= 16.96 \approx 17 \text{ kN/m}^2$

Shortspan Coefficient = 0.044  
 0.033

Longspan Coefficient = 0.037  
 0.028

Short span mid = P

$$M = B \times w l^2 \times c = 0.044 \times 17 \times 4^2$$

$$= 11.968$$

$$d = h - \text{Cover} - \frac{1}{2} \phi = 144$$

$$k = \frac{M}{b d^2 f_{cu}} = \frac{11.968 \times 10^6}{1000 \times 144^2 \times 25} = 0.023$$

$$k = \phi a = 0.5 + \sqrt{0.25 - \frac{k}{0.9}} = 0.97 > 0.95 = 0.95$$

$$z = \phi a \cdot d = 0.95 \times 144 = 136.8$$

$$A_s = \frac{M}{0.95 \phi y z} = \frac{11.968 \times 10^6}{0.95 \times 410 \times 136.8} = 224.61$$

Provide  $y 12 \phi 377 \text{ mm}$

$$M = B \times w l^2 \times c = 0.033 \times 17 \times 4^2 = 8.976$$

$$d = 144$$

$$k = \frac{M}{b d^2 f_{cu}} = \frac{8.976 \times 10^6}{1000 \times 144^2 \times 25} = 0.0173$$

$$\phi a = 0.5 + \sqrt{0.25 - \frac{k}{0.9}} = 0.5 + \sqrt{0.25 - \frac{0.0173}{0.9}} = 0.9$$

$$z = \phi_{\text{aid}} = 0.83 \times 144 = 119.52$$

$$A_s = \frac{M}{0.95 f_y z} = \frac{8.776 \times 10^6}{0.95 \times 410 \times 119.52} = 172.81 \text{ mm}^2$$

Provide  $\phi 12 @ 377 \text{ mm}$

long span  
mid

$$d = d(\text{short span}) - \text{Steel thickness} = 144 - 12 = 132 \text{ mm}$$

$$M = \beta x w l^2 x = 0.037 \times 17 \times 4^2 = 10.864$$

$$k = \frac{M}{b d^2 f_{cu}} = \frac{10.064 \times 10^6}{1000 \times 132^2 \times 25} = 0.0231$$

$$\phi_a = 0.15 + \sqrt{0.25 - \frac{k}{0.9}} = 0.97 > 0.95 = 0.95$$

$$z = \phi_a \cdot d = 0.95 \times 132 = 125.4$$

$$A_s = \frac{M}{0.95 f_y z} = \frac{10.064 \times 10^3}{0.95 \times 125.4 \times 410} = 206.84$$

Provide  $\phi 12 @ 377 \text{ mm}$

long span Continuous

$$d = 132 \text{ mm}$$

$$M = \beta x w l^2 x = 0.028 \times 17 \times 4^2 = 7.616$$

$$k = \frac{M}{b d^2 f_{cu}} = \frac{7.616 \times 10^6}{1000 \times 132^2 \times 25} = 0.017$$

$$\phi_a = 0.15 + \sqrt{0.25 - \frac{k}{0.9}} = 0.98 > 0.95 = 0.95$$

$$z = \phi_a \cdot d = 125.4$$

$$A_s = \frac{M}{0.95 f_y z} = \frac{2.616 \times 10^6}{0.95 \times 410 \times 125.4} \approx 155.93$$

provide  $\phi 12 @ 377 \text{ mm}$

Deflection Check

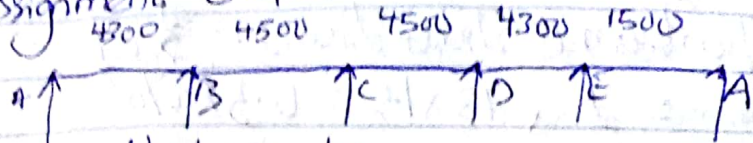
$$f_s = \frac{2}{3} P_{yv} B \cdot \frac{A_{req}}{A_{approved}}$$

$$f_s = \frac{2}{3} \times 250 \times 1 \times \frac{224.61}{377} = 99.3$$

$$m_k = 0.55 \cdot \frac{477 - 99.3}{120(0.19 + \frac{1.2968 \times 10^6}{1000 \times 144^2})} = 2.68 > 2$$

$$d_{req} = \frac{4 \times 1000}{2 \times 26} = 26.92 \approx 27$$

## Assignment 2 Q.1



Assuming thickness = 150mm

$$F_w = 25 \text{ N/mm}^2$$

$$F_y = 410 \text{ N/mm}^2$$

Slab loading

$$\text{Slab weight} = 0.15 \times 24 = 3.6 \text{ kN/m}^2$$

$$\text{Partition} = 1.0 \text{ kN/m}^2$$

$$\text{finishes} = 1.2 \text{ kN/m}^2$$

$$\text{Total G.K.} = 5.8 \text{ kN/m}^2$$

$$D.L = 1.4(5.8) + 1.6(3.0) = 13 \text{ kN/m}^2 \quad \text{--- assuming for classroom}$$

Beam loading

$$\text{Self wt of beam} = 0.225 \times 0.6 \times 24 = 3.24 \text{ kN/m}^2$$

$$\text{finishes} = 1.2 \text{ kN/m}^2$$

$$\text{Wall load} = 3 \times 3.47 = 10.41 \text{ kN/m}^2$$

$$\text{Total G.K.} = 14.85$$

$$D.L = 1.4(14.85) = 20.79 \text{ kN/m}^2$$

Slab load on beam in longer direction =  $\frac{1}{2} w_e l^2 \left(1 - \frac{l}{3x}\right)$

$$k = l_y$$

$$l_x$$

$$\frac{4300}{4000} = 1.075$$

$$4500$$

$$\frac{4500}{4000} = 1.125$$

$$4000$$

$$\frac{1}{2} \times 13 \times 4.3 \left(1 - \frac{1}{3 \times (1.075)^2}\right) = 19.89 \text{ kN/m}^2$$

$$\frac{1}{2} \times 13 \times 4.5 \left(1 - \frac{1}{3 \times (1.125)^2}\right) = 21.55 \text{ kN/m}^2$$

$$\text{Slab load on beam in shorter direction} = \frac{1}{3} w l x$$

$$= \frac{1}{3} \times 13 \times 1.5 = 6.5 \text{ kN/m}^2$$

$$\text{Total load} = 19.89 + 20.79 = 40.68 \text{ kN/m}$$

$$= 21.55 + 20.79 = 42.34 \text{ kN/m}$$

$$= 6.5 + 20.79 = 27.29 \text{ kN/m}$$

Distribution factor

$$K_{AB} = \frac{1}{K_{BA} + K_{BC} + K_{BD}}$$

$$K_{BA} = \frac{1}{K_{AB} + K_{BC} + K_{BD}} = 0.51$$

$$\frac{1}{K_{BA} + K_{BC} + K_{BD}} = \frac{1}{\frac{1}{4.2} + \frac{1}{4.5}}$$

$$K_{BC} = 1 - 0.51 = 0.49$$

$$K_{CB} = \frac{1}{\frac{1}{4.5} + \frac{1}{4.5}} = 0.5$$

$$K_{CD} = 1 - 0.5 = 0.5$$

$$K_{DC} = 0.49$$

$$K_{DE} = 0.51$$

$$K_{ED} = \frac{1}{\frac{1}{4.3} + \frac{1}{1.5}} = 0.26$$

$$K_{EA} = 1 - 0.26 = 0.74$$

$$K_{AE} = 1$$

F.E.M

$$W.D.L = \frac{wL^2}{12}$$

$$1) \frac{40.68 \times 4.3^2}{12} = 62.68 \text{ kN/m}$$

$$2) \frac{42.34 \times 4.5^2}{12} = 71.45 \text{ kN/m}$$



3.)  $27.89 \times 1.5^2 = 5.1 \text{ kN/m}$

	A	B	C	D	E	F
DF	0	0.1	0.1	0.1	0.1	0
EM	6.68	6.68	7.15	7.15	7.15	6.68
VM	6.68	8.27	0	8.27	5.9	5.9
RM	6.68	8.27	0	-8.27	5.9	5.9
DM	0	4.47	4.30	0	4.47	4.30
TM	2.08	3.81	2.15	-2.15	0.744	2.24
ORM	2.035	3.134	0	-7.44	-4.79	-21.305
RM	-2.235	-3.134	0	7.44	4.79	21.305
DM	0	2.235	1.78	0	3.67	3.51
TM	2.44	1.12	0	2.67	1.41	10.66
ORM	-7.44	-1.12	5.85	0.63	-12.52	1.77
RM	7.44	1.12	-5.85	-0.63	12.52	-1.77
DM	0	7.44	0.57	0.57	-0.57	-0.57
TM	0.57	3.08	1.47	0.28	-0.10	7.42
ORM	0.29	4.87	0.12	-0.12	-1.05	-4.65
RM	-0.29	-4.87	-0.12	0.12	1.05	4.65
DM	0	-0.29	-2.98	-2.98	-0.29	0.21
TM	0	2.98	2.98	69.06	69.05	72.06

Moments

$$M_a = 0 \text{ kNm}$$

$$M_b = 82.88 \text{ kNm}$$

$$M_c = 69.06 \text{ kNm}$$

$$M_d = 72.06 \text{ kNm}$$

$$M_e = 45.47 \text{ kNm}$$

$$M_A = 0 \text{ kNm}$$

Free moment

$$\text{For U.D.L} = \frac{WL^2}{8}$$

$$1.) \frac{40.68 \times 4.5^2}{8} = 94.02 \text{ kNm}^2$$

$$2.) \frac{42.84 \times 4.5^2}{8} = 107.17 \text{ kNm}^2$$

$$3.) \frac{27.27 \times 1.5^2}{8} = 8.24 \text{ kNm}^2$$

Span moment

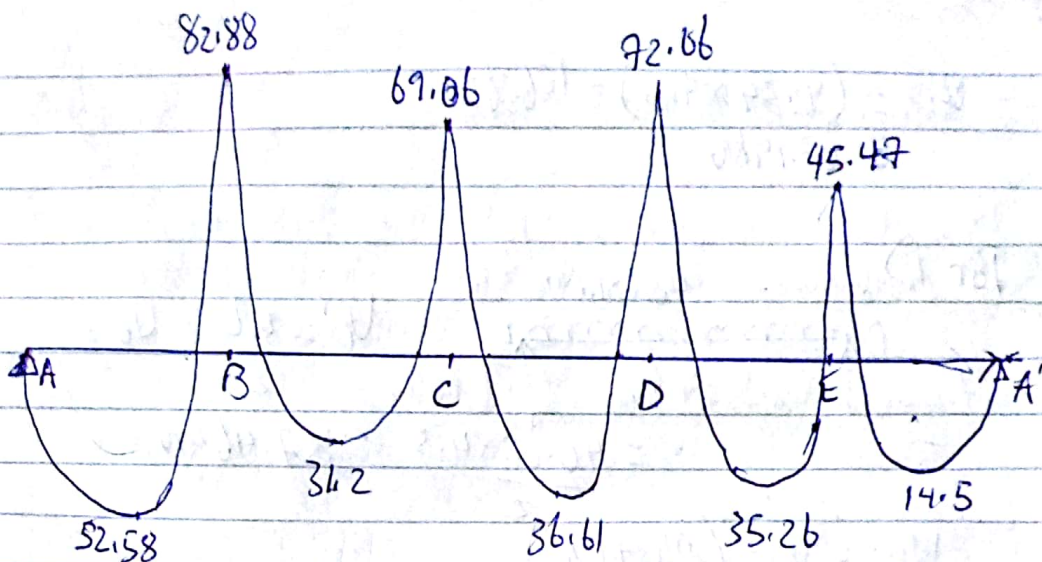
$$M_{AB} = M^F - \left( \frac{M_A + M_B}{2} \right) = 94.02 - \left( \frac{0 + 82.88}{2} \right) = 52.58 \text{ kNm}$$

$$M_{BC} = M^F - \left( \frac{M_B + M_C}{2} \right) = 107.17 - \left( \frac{82.88 + 69.06}{2} \right) = 36.2 \text{ kNm}$$

$$M_{CD} = M^F - \left( \frac{M_C + M_D}{2} \right) = 107.17 - \left( \frac{69.06 + 72.06}{2} \right) = 36.61 \text{ kNm}$$

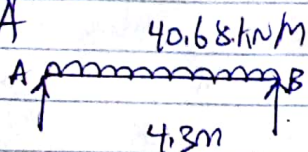
$$M_{DE} = M^F - \left( \frac{M_D + M_E}{2} \right) = 94.02 - \left( \frac{72.06 + 45.47}{2} \right) = 35.26 \text{ kNm}$$

$$M_{EA'} = M^F - \left( \frac{M_E + M_{A'}}{2} \right) = 8.24 - \left( \frac{45.47 + 0}{2} \right) = -14.5 \text{ kNm}$$



B.M.D

Shear force  
for A



$$V_A = \frac{wL}{2} = V_B$$

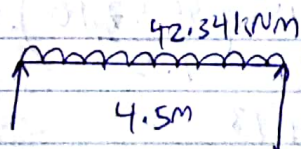
$$= \frac{40.68 \times 4.3}{2} = 87.462 \text{ kN}$$

$$V_{AB} = V_A + \left( \frac{M_A - M_B}{L} \right) = 87.462 + \left( \frac{0 - 82.88}{4.3} \right) = 68.17$$

$$V_{BA} = wL - V_{AB}$$

$$= (40.68 \times 4.3) - 68.17 = 106.73 \text{ kN}$$

For B



$$V_{BC} = \frac{wL}{2} = V_C$$

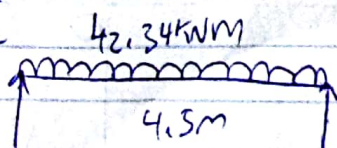
$$= \frac{42.34 \times 4.5}{2} = 95.27 \text{ kN}$$

$$V_{BC} = V_B + \left( \frac{M_B + M_C}{L} \right) = 95.27 + \left( \frac{82.88 + 69.06}{4.5} \right) = 129.03 \text{ kN}$$

$$V_{CB} = (42.34 \times 4.5) - 129.03$$

$$= 61.5 \text{ kN}$$

For C



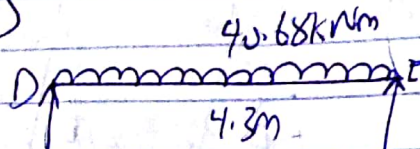
$$V_C = \frac{wL}{2} = V_D$$

$$= \frac{42.34 \times 4.5}{2} = 95.27 \text{ kN}$$

$$V_D = (42.34 \times 4.5) - 126.63$$

$$= 63.19 \text{ kN}$$

For D



$$V_D' = \frac{wL}{2} = V_E$$

$$= \frac{40.68 \times 4.3}{2} = 87.46 \text{ kN}$$

$$V_{DE} = V_D - \left( \frac{M_D + M_E}{L} \right)$$

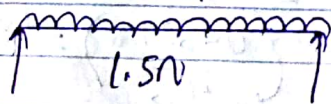
$$= 87.46 - \left( \frac{72.06 + 45.47}{4.3} \right) = 60.13 \text{ kN}$$

$$V_{ED} = wL = V_{DE}$$

$$= (40.68 \times 4.3) - 60.13$$

$$= 114.74 \text{ kN}$$

For E



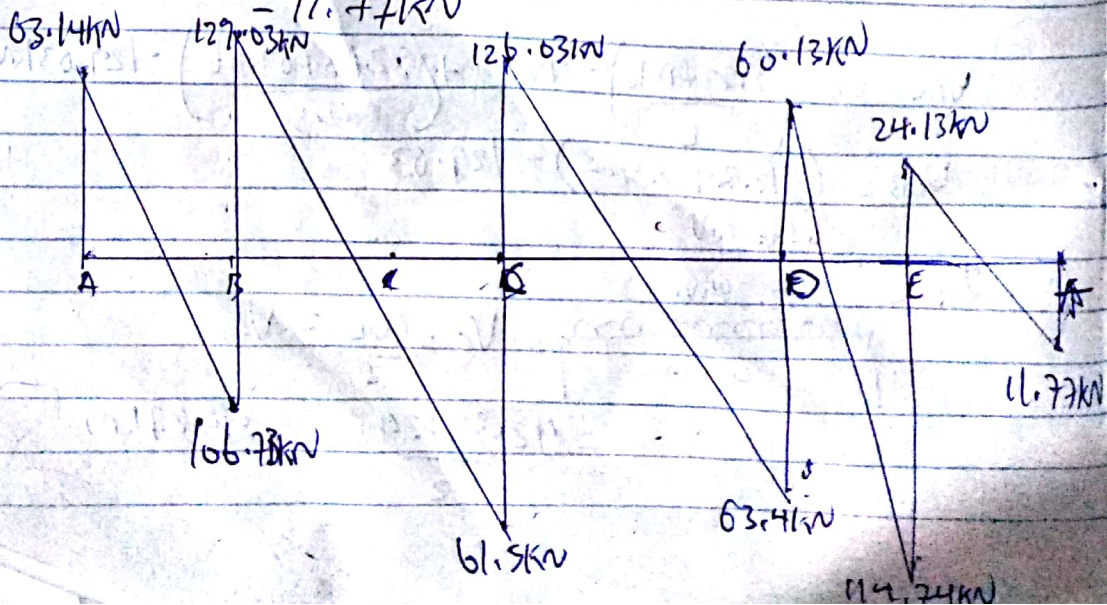
$$V_E' = \frac{wL}{2} = V_A'$$

$$= \frac{8.24 \times 1.5}{2} = 6.18 \text{ kN}$$

$$V_{EA}' = V_E' - \left( \frac{M_E + M_A}{L} \right) = 6.18 - \left( \frac{45.47 + 0}{1.5} \right) = 24.13 \text{ kN}$$

$$V_{AE}' = (8.24 \times 1.5) - 24.13$$

$$= 11.77 \text{ kN}$$



## Assignment 2 No 2

Base design

$$N = 1200 \text{ kN}$$

$$\text{Strength} = 25.410 \text{ N/mm}^2$$

$$f_b = 150 \text{ kN/m}^2$$

$$\text{Area of base req} = \frac{N \times 1.1}{f_b} \quad \lambda = 1.40$$

$$\frac{1200 \times 1.1}{1.46 \times 150} = 6.027 \text{ m}^2$$

$$\sqrt{6.027} = 2.45 \text{ m} \approx 2.5$$

$$\text{Net pressure } f_{\text{net}} = \frac{N \times 1.1}{B}$$

$$\frac{1200 \times 1.1}{2.5} = 24 \times 0.860 \times 1.4$$
$$= 505.824 \text{ kN/m}$$

$$\text{Moment } m = \frac{f_{\text{net}} L^2}{2}$$

$$\text{where } L = \frac{1}{2} (B - h) \text{ } \frac{1}{4} = \text{depth of base} = 660$$

$$L = \frac{1}{2} (2.5 - 0.225) = 1.138 \approx 1.14 \text{ m}$$

$$M = \frac{505.824 \times 1.14^2}{2} = 328.68 \text{ kNm}$$

$$d = h - \text{Cover} - \frac{1}{2} \phi$$
$$= 660 - 50 - 10 = 600 \text{ mm}$$

$$k = \frac{M}{5cl^3 f_{cu}} = \frac{328.68 \times 10^6}{1000 \times 600^2 \times 25} = 0.037$$

$$R_u = 0.15 + \sqrt{0.125 + \frac{0.037}{0.9}} = 0.96 > 0.95$$

$$z = R_{nd} = 0.95 \times 600 = 570 \text{ mm}$$

$$A_s = \frac{M}{0.95 f_y z} = \frac{328.68 \times 10^6}{0.95 \times 410 \times 570} = 1480.44 \text{ mm}^2$$

Provide  $4 \times 25 \text{ @ } 300 \text{ c/c}$  (1640)

Rectangular Slab

Column Size =  $225 \times 450 \text{ mm}$

Perly = 25 - 410 mm

Area Footing =  $6.027 \text{ m}^2$

Size of Footing =  $2500 + 2800$

Net pressure =  $508.824 \text{ kN/m}$

depth = 600

Critical section,  $\frac{d}{2} = 300$

$$300 + 300 + 225 = 825 \text{ mm}$$

$$300 + 300 + 450 = 1050 \text{ mm}$$

$$\text{Shear force } V_u = q_n \times [\text{Area of footing} - (0.3 + d)^2]$$

$$= 508.824 [2.5 \times 2.5 - (0.3 + 0.6)^2]$$

$$V_u = 2751.68 \text{ N}$$

$$\text{Nominal shear stress } \tau_v = \frac{V_u}{b_l}$$

$b$  = perimeter of critical section

$d$  = effective span / depth

$$\tau_v = \frac{2751.68}{7 \times 10^3}$$

$$= \frac{(2 \times (825) + 2(1050)) \times 600}{7 \times 10^3}$$

$$\tau_v = 1.223 \text{ N/mm}^2$$

Permissible Shear Stress

$$\tau_c = k_s \times \tau_c$$

$$k_s = (0.5 + \beta_c) \text{ but not greater than } 1$$

$\beta_c = \text{Ratio of Shorter to large side of column}$

$$\tau_c = 0.25 \sqrt{f_{ck}}$$

$$k_s = 1$$

$$\tau_c = 0.25 \sqrt{25} = 1.25 \text{ N/mm}^2$$

$$\tau_u = 1.223 \text{ N/mm}^2$$

$$\tau_u \leq \tau_c$$

Hence depth assumed is ok ✓

Checking for fb with actual size of footing

Unit weight of concrete =  $24 \text{ kN/m}^3$

Unit weight of soil =  $1.091 \times 10^{-6} \text{ kN/mm}^3$

Actual pressure footing below

$$q = (1200 \times 2.5 \times 2.5) + (24 \times 0.660) + (1.091 \times 10^{-6} \times 0.66)$$

$$q = 214.94 \text{ kN/m}^2$$