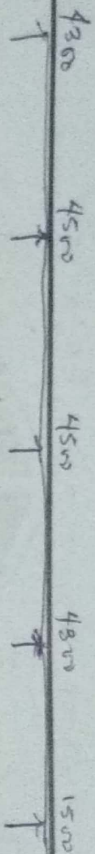


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Question 1



Assuming dimensions to be 1500mm

$$f_{cu} = 25 \text{ N/mm}^2$$

$$f_y = 410 \text{ N/mm}^2$$

Slab loading:

$$\text{Slab weight} = 0.15 \times 24 = 3.6 \text{ kN/m}^2$$

$$\text{Particular} = 1.0 \text{ kN/m}^2$$

$$\text{Finishes} = 1.2 \text{ kN/m}^2$$

$$\text{Total reqd} = 5.8$$

$$\text{DL} = 1.4(5.8) + 1.6(8.0) = 13 \text{ kN}$$

Beam loading:

$$\text{Self weight of beam} = 0.225 \times 0.6 \times 24 = 3.24 \text{ kN/m}^2$$

$$\text{Finishes} = 1.2 \text{ kN/m}^2$$

$$\text{Wind load} = 3 \times 3.44 = 10.31 \text{ kN/m}^2$$

$$\text{Total load} = 14.75$$

$$\text{DL} = 1.4(14.75) = 20.65 \text{ kN/m}^2$$

Slab load in beam in longer direction

$$= \frac{1}{2} w dx (1 - \frac{1}{3} k^2)$$

$$k = \frac{l_y}{l_x}$$

$$\frac{4.3}{4.0} = 1.075$$

$$4.0$$

$$\frac{4.5}{4.0} = 1.125$$

$$4.0$$

$$\frac{1}{2} \times 13 \times 4.3 \left(1 - \frac{1}{3 \times (1.075)^2} \right) = 19.89 \text{ kN/m}^2$$

$$\frac{1}{2} \times 13 \times 4.5 \left(1 - \frac{1}{3 \times (1.125)^2} \right) = 21.55 \text{ kN/m}^2$$

Slab load in beam in shorter direction

$$= w l_x$$

$$= \frac{1}{3} \times 13 \times 1.5 = 6.5 \text{ kN/m}^2$$

$$\text{Total load} = 19.89 + 20.79 = 40.68 \text{ kN/m}^2$$

$$= 21.55 + 20.79 = 42.34 \text{ kN/m}^2$$

$$= 6.5 + 20.79 = 27.29 \text{ kN/m}^2$$

Distribution factor

$$K_{a2} = 1$$

$$K_{b2} = \frac{1}{4.5} = \frac{1}{4.5} = 0.51$$

$$\frac{1}{4.5} = \frac{1}{4.5} \quad \frac{1}{4.5} = \frac{1}{4.5}$$

$$K_{RC} = 1 - 0.51 = 0.49$$

$$K_{a3} = \frac{1}{4.5} = 0.5$$

$$\frac{1}{4.5} = \frac{1}{4.5}$$

$$K_{a4} = 1 - 0.5 = 0.5$$

$$K_{BC} = 0.49$$

$$K_{AC} = 0.51$$

$$K_{CD} = \frac{4 \times 3}{12} = 0.26$$

$$\frac{4 \times 3}{12} = 0.26$$

$$K_{BA} = 1 - 0.26 = 0.74$$

$$K_{AC} = 0$$

$$I = 2.07$$

$$u_{DL} = \frac{w L^2}{12}$$

$$1) \frac{40.68 \times 4.3^2}{12} = 262.4 \text{ kNm}^2$$

$$\frac{42.34 \times 4.5^2}{12} = 71.45 \text{ kNm}^2$$

$$\frac{24.27 \times 5^2}{12} = 50 \text{ kNm}^2$$

	A	B	C	D	E	F					
	AB	BA BC	CB CD	DC DE	ED EA	EA FA					
Δ -f	0	0.51	0.49	0.3	0.5	0.49	0.51	0.26	0.74	1	0
10m	62.68	62.68	21.45	21.45	42.68	62.68	62.68	5.1	5.1		
00m	62.68	-8.77	0	0	8.77	58.58	58.58			-5.1	
8m	62.68	8.77	0	0	-8.77	-58.58	-58.58			5.1	
10m	0	62.68	47.45	0	0	-4.30	4.47	14.72	-42.61	-4	0
1m		2.23	8.77	2.15	21.45	0	2.44	-2.24	-2.55	-2.50	
08m	2.23	-2.22	-3.55	0	6.25	12.57	12.57			1.27	
8m	-2.23	1.22	0.55	0	0.2	-12.57	-12.57			-1.27	
10m	0	5.14	0.54	2.45	0.25	0.25	-1.23	-9.29	-1.23	0	0
1m		0.23	1.40	1.40	0.25	0.15	1.47	1.64	0.14	0.19	-4.05

OBM	0.24	4.89	0.12	-0.12	-1.05	-9.65						
BM	-0.25	-4.89	0.12	0.12	1.05	9.65						
DM	0	-0.29	-2.91	-2.35	0.06	0.04	0.04	0.09	0.27	0.38	9.65	0
Σ	=	0	22.88	-82.88	69.06	-69.05	22.06	-22.09	49.4	45.46	0	0

Monoc

$$M_A = 0 \text{ kNm}$$

$$M_B = 82.88 \text{ kNm}$$

$$M_C = 69.06 \text{ kNm}$$

$$M_D = 72.06 \text{ kNm}$$

$$M_E = 45.47 \text{ kNm}$$

$$M_F = 0 \text{ kNm}$$

Free end

$$\text{For D.L.} = \frac{wL^2}{8}$$

$$\frac{40.31 \times 4.3^2}{8} = 94.02 \text{ kNm}$$

$$\frac{42.54 \times 4.3^2}{8} = 109.17 \text{ kNm}$$

$$\frac{27.29 \times 1.5^2}{8} = 8.24 \text{ kNm}$$

Spine moment

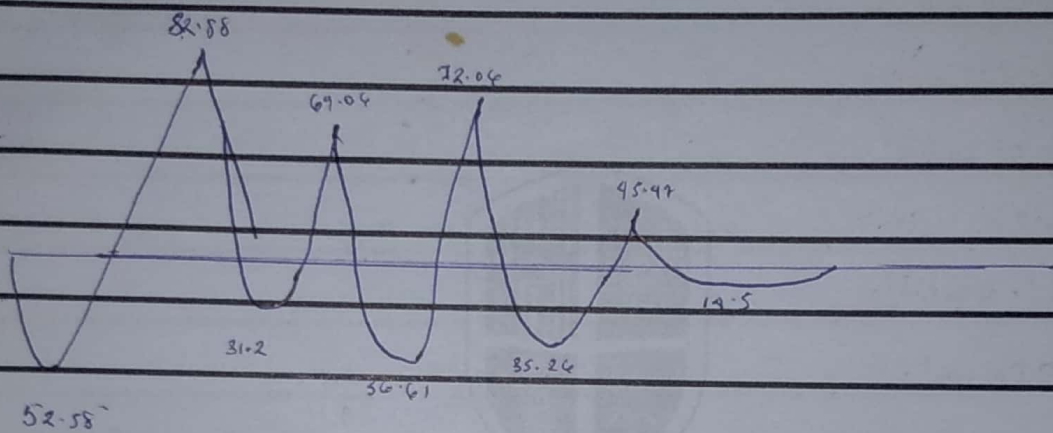
$$M_{AB} = M^* - \left(\frac{M_A + M_B}{2} \right) = 94.02 - \left(\frac{0 + 82.88}{2} \right) = 52.58 \text{ kNm}$$

$$M_{BC} = M^* - \left(\frac{M_B + M_C}{2} \right) = 109.17 - \left(\frac{82.88 + 69.06}{2} \right) = 31.2 \text{ kNm}$$

$$M_{C\theta} = M^F - \left(\frac{M_C + M_B}{2} \right) = 109.17 - \left(\frac{67.04 + 72.04}{2} \right) = 36.61 \text{ kNm}$$

$$M_{DE} = M^F - \left(\frac{M_D + M_E}{2} \right) = 74.02 - \left(\frac{92.06 + 45.47}{2} \right) = 35.26 \text{ kNm}$$

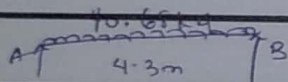
$$M_{EA} = M^F - \left(\frac{M_E + M_A}{2} \right) = 8.24 - \left(\frac{45.47 + 0}{2} \right) = -14.5 \text{ kNm}$$



BMD.

Shear force.

For A



$$V_A = \frac{wL}{2} = V_B$$

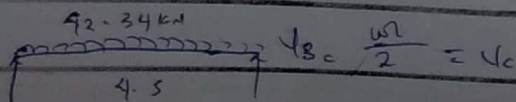
$$= \frac{40.68 \times 4.3}{2} = 87.462 \text{ kN}$$

$$V_{AB} = V_A + \left(\frac{M_A - M_B}{L} \right) = 87.462 + \left(\frac{0 - 82.88}{4.3} \right) = 68.19$$

$$V_{BA} = wL - V_{AB}$$

$$= (40.68 \times 4.3) - 68.19 = 106.73 \text{ kN}$$

For B



$$V_B = \frac{wL}{2} = V_C$$

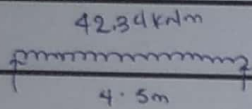
$$= \frac{42.34 \times 4.5}{2} = 95.27 \text{ kN}$$

$$V_{BC} = V_B + \left(\frac{M_B + M_C}{L} \right) = 95.27 + \left(\frac{82.68 + 69.09}{4.5} \right) = 129.03 \text{ kN}$$

$$V_{CB} = (42.34 \times 4.5) - 129.03$$

$$= 61.5 \text{ kN}$$

For C



$$V_C = \frac{wL}{2} = V_D$$

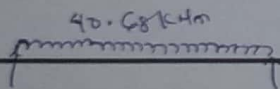
$$= \frac{42.34 \times 4.5}{2} = 95.27 \text{ kN}$$

$$V_{CD} = 95.27 + \left(\frac{69.66 + 92.09}{4.5} \right) = 120.63 \text{ kN}$$

$$V_{DC} = (42.34 \times 4.5) - 120.63$$

$$= 63.17 \text{ kN}$$

For D



$$V_D = \frac{wL}{2} = V_E$$

$$= \frac{40.68 \times 4.5}{2} = 91.46 \text{ kN}$$

$$V_{DE} = V_D + \left(\frac{M_D + M_E}{L} \right)$$

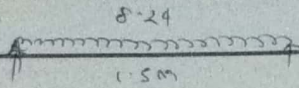
$$= 91.46 + \left(\frac{92.06 + 45.97}{4.5} \right) = 60.13 \text{ kN}$$

$$V_{ED} = wL - V_{DE}$$

$$= (40.68 \times 4.5) - 60.13$$

$$= 114.24 \text{ kN}$$

For E



$$V_E' = wL = 11.8$$

$$= \frac{8.24 \times 1.5}{2} = 6.18 \text{ kN}$$

$$V_{AE} = V_E' - \left(\frac{M_E + M_A'}{L} \right) = 6.18 - \left(\frac{45.42 + 0}{1.5} \right) = 24.13 \text{ kN}$$

$$V_{AE} = (8.24 \times 1.5) = 24.13$$
$$= 11.72 \text{ kN}$$

Question 2

Base design

$$N \geq 1200 \text{ kN}$$

$$\text{Strength} = 25 - 460 \text{ all mm}^2$$

$$F_b = 157 \text{ kN/mm}^2$$

$$\text{Area of base req} = \frac{N \times 1.1}{F_b} = 1046$$

$$\frac{1200 \times 1.1}{1.96 \times 150} = 6.027 \text{ m}^2$$

$$1.96 \times 150$$

$$\sqrt{6.027} = 2.45 \text{ m} \approx 2.5$$

$$\text{Net pressure, } f_{zf} = \frac{N \times 1.1}{B}$$

$$\frac{1200 \times 1.1}{2.5} = 24 \times 0.660 \times 1.4$$

$$= 2505.824 \text{ kNm}$$

$$\text{Moment } M = \frac{F_{zf} \times l}{2}$$

$$\text{where } l = \frac{1}{2} (B + A)$$

$$L = \frac{1}{2}(3.5 - 0.225) = 1.138 \approx 1.14 \text{ m}$$

$$m = \frac{505.824 \times 1.14^2}{2} = 328.68 \text{ kNm}$$

$$d = h - \text{Cover} - \frac{1}{2} \phi$$

$$= 660 - 50 - 10 = 600 \text{ mm}$$

$$k = \frac{m}{bd^2 I_{cu}} = \frac{328.68 \times 10^6}{1000 \times 600^2 \times 25} = 0.032$$

$$j = 0.5 + \sqrt{0.25 - \frac{0.032}{0.9}} = 0.76 > 0.95$$

$$Z = j \cdot d = 0.75 \times 600 = 590 \text{ mm}$$

$$A_s = \frac{M}{0.75 f_y Z} = \frac{328.68 \times 10^6}{0.75 \times 400 \times 590} = 1480.44 \text{ mm}^2$$

Punch shear

$$\text{Column size} = 225 \times 450 \text{ mm}$$

$$I_{cu} - z_j = 25 - 40 \text{ mm}$$

$$\text{Area footing} = 6020 \text{ mm}^2$$

$$z_j = \text{slab footing} = 2500 \times 2500$$

$$q = \text{net pressure} = 505.824 \text{ kNm}$$

$$\text{depth} = 600$$

$$\text{Critical Section} = \frac{d}{2} = 300$$

300

$$300 + 300 + 225 = 825 \text{ mm}$$

$$300 + 300 + 450 = 1050 \text{ mm}$$

$$\text{Shear force} = q \times [\text{Area of slab} - (0.3 + d)]$$

$$= 505.824 [2.5 \times 2.5 - (0.3 + 0.4)]$$

$$V_u = 2251.08$$

Normal shear stress $\tau_v = V/bd$

$b =$ Parameter of critical section

$d =$ effective depth

$$V_u = 2451.68 \times 10^3$$

$$\left[(2 \times 825) + 2(1050) \right] \times 600$$

$$\tau_v = 1.223 \text{ N/mm}^2$$

Permissible shear stress

$$\tau_c = k_s \times E$$

$$k_s = (0.5 + \beta_c) \text{ but not } > 1$$

$\beta_c =$ Ratio of shorter to larger side of column

$$\tau_c = 0.25 \sqrt{f_{ck}}$$

$$k_s = 1$$

$$\tau_c = 0.25 \sqrt{25} = 1.25 \text{ N/mm}^2$$

$$\tau_v = 1.223 \text{ N/mm}^2$$

$$\tau_v \leq \tau_c$$

slenderness depth assumed is ok

checking for F_b with actual size of footing

Unit weight of concrete = 24 kN/m^3

weight of soil = $1.021 \times 10^{-6} \text{ kN/m}^3$

Actual pressure footing below

$$q = (1200 \times 2.5 \times 2.5) + (24 \times 0.660) + (1.021 \times 10^{-6} \times 0.660)$$

$$q = 214.74 \text{ kN/m}^2$$