

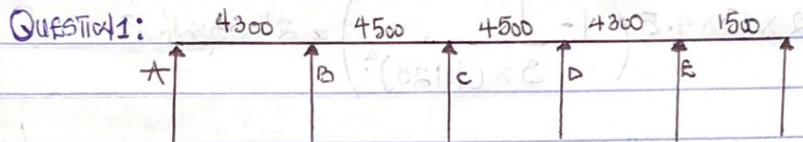
NAME: ZIBIRI MIRACLE

MATRIC NUMBER: 17/EKG03/059

ASSIGNMENT TITLE: ASSIGNMENT 2 BEAM

COURSE TITLE: STRUCTURAL DESIGN 1

COURSE CODE: CVE 308



Assuming thickness: 150mm

$$f_{cu} = 25 \text{ N/mm}^2$$

$$f_y = 410 \text{ N/mm}^2$$

Slab loading

$$\text{Slab weight} = 0.15 \times 24 = 3.6 \text{ kN/m}^2$$

$$\text{Partition} = 1.0 \text{ kN/m}^2$$

$$\text{Finishes} = 1.2 \text{ kN/m}^2$$

$$\text{Total G-K} = 5.8 \text{ kN/m}^2$$

$$D.L = 1.4(5.8) + 1.6(3.0) = 13 \text{ kN/m}^2$$

Beam loading

$$\text{Self wt of beam} = 0.225 \times 0.6 \times 24 = 3.24 \text{ kN/m}^2$$

$$\text{Finishes} = 1.2 \text{ kN/m}^2$$

$$\text{Wall load} = 3 \times 3.47 = 10.41 \text{ kN/m}^2$$

$$\text{Total G-K} = 14.85$$

$$D.L = 1.4(14.85) = 20.79 \text{ kN/m}^2$$

$$\text{Slab load on beam in longer direction} \\ = \frac{1}{2} w_l a (1 - \frac{1}{3} \frac{a}{l})$$

$$k = \frac{l_y}{2l_x}$$

$$\frac{4300}{4000} = 1.075, \quad \frac{1}{2} \times 13 \times 4.3 \left(1 - \frac{1}{3 \times (1.075)^2} \right) = 19.89 \text{ kN/m}^2$$

$$\frac{4500}{4000} = 1.125, \quad \frac{1}{2} \times 13 \times 4.5 \left(1 - \frac{1}{3 \times (1.125)^2} \right) = 21.55 \text{ kN/m}^2$$

$$\begin{aligned} \text{Slab load on beam in shorter direction} &= \frac{1}{3} w l_x \\ &= \frac{1}{3} \times 13 \times 1.5 \\ &= 6.5 \text{ kN/m}^2 \end{aligned}$$

$$\begin{aligned} \text{Total load} &= 19.89 + 20.79 = 40.68 \text{ kN/m} \\ &= 21.55 + 20.79 = 42.34 \text{ kN/m} \\ &= 6.5 + 20.79 = 27.29 \text{ kN/m} \end{aligned}$$

Distribution Factor

$$K_{AB} = 1$$

$$K_{BA} = \frac{l_{BC}}{l_{BA} + l_{BC}} = \frac{4.3}{4.3 + 4.5} = 0.51$$

$$K_{BC} = 1 - 0.51 = 0.49$$

$$K_{CB} = \frac{l_{BA}}{l_{CB} + l_{BA}} = 0.5$$

$$K_{CB} = 1 - 0.5 = 0.5$$

$$K_{DC} = 0.49$$

$$K_{DE} = 0.51$$

$$K_{ED} = \frac{l_{DC}}{l_{ED} + l_{DC}} = 0.26$$

$$K_{R1} = 1 - 0.26 = 0.79$$

$$K_{R2} = 1$$

F.E.M

$$UDL = \frac{wL^2}{12}$$

$$1) \frac{40.68 \times 4.3^2}{12} = 62.68 \text{ kN/m}$$

$$a) \frac{42.34 \times 4.5^2}{12} = 71.45 \text{ kN/m}$$

$$b) \frac{27.29 \times 1.5^2}{12} = 5.11 \text{ kN/m}$$

	A	B	C	D	E	A'					
	AB	BA BC	CB CD	DC DE	ED EA'	A'E A'					
D-F	0	0.51	0.49	0.5	0.5	0.49	0.51	0.26	0.79	1	0
FEM	-62.68	62.68	-71.45	71.45	-71.45	71.45	-62.68	62.68	5.1	5.1	0
OBM	-62.68	-8.77	0	0	8.77	57.58	-5.1				
DM	-62.68	8.77	0	0	8.77	-57.58	5.1				
TM	0	62.68	4.97	4.30	0	0	-4.30	-4.41	-14.98	-42.61	-5.1
		2.235	31.34	0	2.15	-2.15	0	2.49	-2.24	-2.55	-21.30
OBM	2.235	0	81.34	0	-7.49	-4.79	-4.79	-21.305			
BM	-2.235	-31.34	0	0	7.49	4.79	4.79	21.305			
DM	0	2.235	-15.98	-15.36	0	0	3.67	3.82	1.25	8.54	21.31
TM	-7.99	-1.12	0	-7.69	1.84	0	0.63	1.41	10.66	1.77	0
OBM	-7.99	-1.12	-5.85	0.63	12.57	1.77					
BM	7.99	1.12	5.85	-0.63	-12.57	-1.77					
DM	0	7.99	0.57	0.55	2.93	2.93	-0.31	6.32	-3.27	-9.29	-1.77
TM	0.29	3.40	1.42	0.28	-0.16	1.47	1.64	-0.16	-0.89	-7.65	0
OBM	0.29	4.87	0.12	-0.17	-1.05	-4.65					
BM	-0.29	-4.87	-0.12	0.17	1.05	4.65					
DM	0	0.29	-2.48	-2.39	-0.06	-0.06	0.09	-0.09	0.27	0.78	4.66
Σ	0	22.88	-82.88	69.05	-69.05	72.66	-72.66	45.6	-45.46	0	0

Moments

$$M_A = 0 \text{ kNm}$$

$$M_B = 82.88 \text{ kNm}$$

$$M_C = 69.06 \text{ kNm}$$

$$M_D = 72.06 \text{ kNm}$$

$$M_E = 45.47 \text{ kNm}$$

$$M_{A'} = 0 \text{ kNm}$$

Free moment

$$\text{For UDL} = \frac{wL^2}{8}$$

$$1.) \frac{40.68 \times 4.3^2}{8} = 94.02 \text{ kNm}^2$$

$$2.) \frac{42.34 \times 4.5^2}{8} = 107.17 \text{ kNm}^2$$

$$2.) \frac{27.29 \times 1.5^2}{8} = 7.68 \text{ kNm}^2$$

Span moment

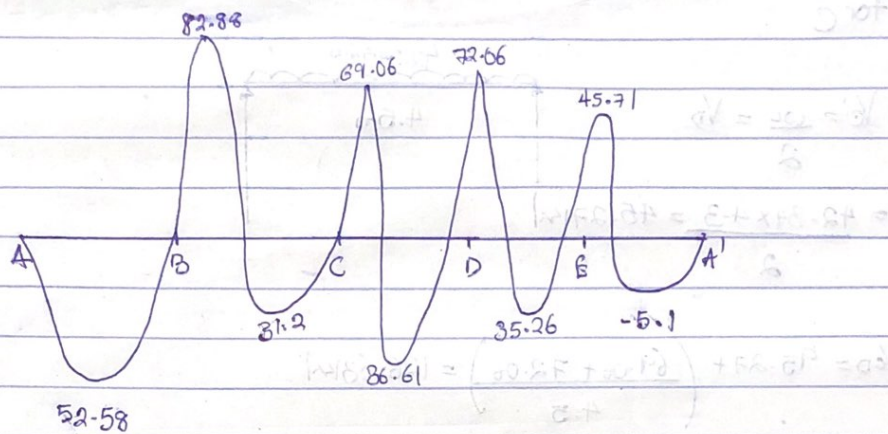
$$M_{AB} = M^F - \left(\frac{M_A + M_B}{2} \right) = 94.02 - \left(\frac{0 + 82.88}{2} \right) = 52.58 \text{ kNm}$$

$$M_{BC} = M^F - \left(\frac{M_B + M_C}{2} \right) = 107.17 - \left(\frac{82.88 + 69.06}{2} \right) = 31.2 \text{ kNm}$$

$$M_{CD} = M^F - \left(\frac{M_C + M_D}{2} \right) = 107.17 - \left(\frac{69.06 + 72.06}{2} \right) = 26.61 \text{ kNm}$$

$$M_{DE} = M^F - \left(\frac{M_D + M_E}{2} \right) = 94.02 - \left(\frac{72.06 + 45.47}{2} \right) = 35.26 \text{ kNm}$$

$$M_{EA'} = M^F - \left(\frac{M_E + M_{A'}}{2} \right) = 8.68 - \left(\frac{45.47 + 0}{2} \right) = -15.1 \text{ kNm}$$



B.M.D

Shear force

For A

$$V_A = \frac{wL}{2} = V_B$$

$$= \frac{40.68 \times 4.2}{2} = 87.462 \text{ kN}$$

$$V_{AB} = V_A + \left(\frac{M_A - M_B}{L} \right) = 87.462 + \left(\frac{0 - 82.88}{4.3} \right) = 68.19$$

$$V_{BA} = wL - V_{AB}$$

$$= (40.68 \times 4.3) - 68.19 = 106.73 \text{ kN}$$

For B

$$V'_B = \frac{wL}{2} = V'_C$$

$$= \frac{42.34 \times 4.5}{2} = 95.27 \text{ kN}$$

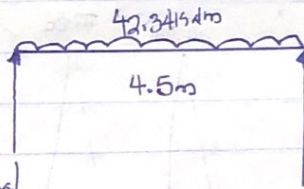
$$V_{BC} = V'_B + \left(\frac{M_B + M_C}{L} \right) = 95.27 + \left(\frac{82.68 + 69.06}{4.5} \right)$$

$$V_{CB} = (42.34 \times 4.5) - 129.03 = 61.5 \text{ kN}$$

For C

$$V_C' = \frac{wL}{2} = V_D$$

$$= \frac{42.34 \times 4.3}{2} = 45.271 \text{ kN}$$

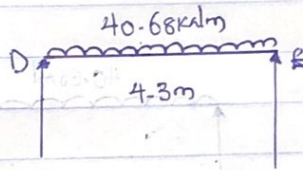


$$V_{CD} = 95.27 + \left(\frac{69.06 + 72.06}{4.5} \right) = 126.63 \text{ kN}$$

For D

$$V_D' = \frac{wL}{2} = V_E$$

$$= \frac{40.68 \times 4.3}{2} = 87.461 \text{ kN}$$



$$V_{DE} = V_D - \left(\frac{M_D + M_E}{L} \right)$$

$$= 87.46 - \left(\frac{72.06 + 45.47}{4.3} \right) = 60.131 \text{ kN}$$

$$V_{ED} = wL = V_{DE}$$

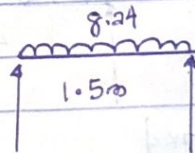
$$= (40.68 \times 4.3) - 60.13$$

$$= 114.791 \text{ kN}$$

For E

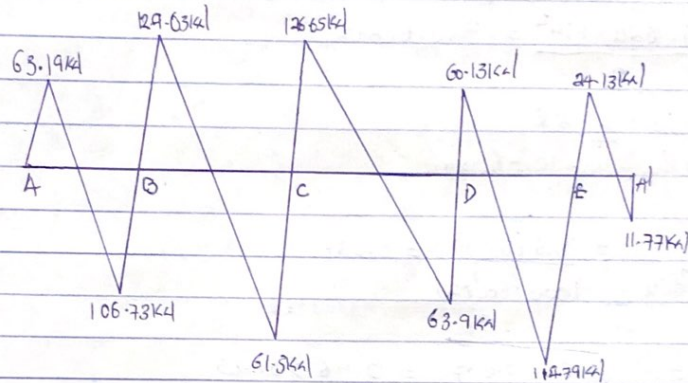
$$V_E' = \frac{wL}{2} = V_F$$

$$= \frac{8.24 \times 1.5}{2} = 6.181 \text{ kN}$$



$$V_{EA} = V_E = \left(\frac{M_E + M_A}{L} \right) = 6.18 - \left(\frac{45.47 + 0}{1.5} \right) = 24.13 \text{ kN}$$

$$V_{AE} = (8.24 \times 1.5) - 24.13 \\ = 11.77 \text{ kN}$$



Question 2

Base design

$$M = 1200 \text{ kNm}$$

$$\text{Strength} = 25.41 \text{ kN/mm}^2$$

$$f_b = 150 \text{ kN/mm}^2$$

$$\text{Area of base req} = \frac{N \times 1.1}{\lambda \times f_b} \quad N = 1.46$$

$$\frac{1200 \times 1.1}{1.46 \times 180} = 6.027 \text{ m}^2$$

$$1.46 \times 180$$

$$\sqrt{6.027} = 2.45 \text{ m} \rightarrow 2.5$$

$$\text{Net pressure, } F_{net} = \frac{N \times 1.1}{B}$$

$$\frac{1200 \times 1.1}{2.5} = 24 \times 0.660 \times 1.4$$

$$2.5$$

$$= 505.804 \text{ kN/m}$$

$$\text{Moment} = M = \frac{f_{cr} z^2}{2}$$

where $z = \frac{1}{2}(B-h)$ and $d = \text{depth of base} = 660$

$$z = \frac{1}{2}(2.5 - 0.225) = 1.138 \approx 1.14 \text{ m}$$

$$M = \frac{505.824 \times 1.14^2}{2} = 328.684 \text{ kNm}$$

$$d = h - \text{cover} - \frac{1}{2}\phi$$

$$= 660 - 50 - 10 = 600 \text{ mm}$$

$$k = \frac{M}{bd^2 f_{cu}} = \frac{328.68 \times 10^6}{1000 \times 600^2 \times 25} = 0.037$$

$$R_a = 0.5 + \frac{\sqrt{0.25 + 0.037}}{0.9} = 0.96 > 0.95$$

$$z = I_{ad} = 0.95 \times 600 = 570 \text{ mm}$$

$$A_s = \frac{M}{0.958 y^2} = \frac{328.68 \times 10^6}{0.95 \times 410 \times 510} = 1480.44 \text{ mm}^2$$

Provide $Y_{25} @ 300 \text{ c/c}$ (1640)

Punching shear

$$\text{column size} = 225 \times 450 \text{ mm}$$

$$R_{\text{eff}} = 25 - 410 \text{ mm}$$

$$\text{Area footing} = 6.027 \text{ m}^2$$

$$\text{Size of loading} = 2500 \times 2500$$

$$q^2, \text{ net pressure} = 505.824 \text{ kN/m}^2$$

$$d/2, \text{ critical section} = 300$$

$$300 + 300 + 225 = 825 \text{ mm}$$

$$300 + 300 + 450 = 1050 \text{ mm}$$

$$\begin{aligned} \text{Shear force } V_a &= q_s \times (\text{Area of loading} - (0.3+d)) \\ &= 505.82 \text{ kN} [2.5 \times 2.5 - (0.3+0.6)^2] \\ V_0 &= 2751.684 \text{ kN} \end{aligned}$$

$$\text{Normal shear stress } \tau_v = \frac{V_s}{bd}$$

b = Parameter of critical section, d = effective pen or depth

$$\begin{aligned} \tau_v &= \frac{2751.68 \times 10^3}{[(2 \times (825) + 2(1050)) \times 600]} \\ \tau_v &= 1.2234 \text{ N/mm}^2 \end{aligned}$$

Permissible shear stress

$$\tau_c' = k_s \times \tau_c$$

$k_s = (0.5 + \beta_c)$ but not greater than 1

β_c = Ratio of shorter to larger side of columns

$$\tau_c = 0.25 \sqrt{f_{ck}}$$

$$k_s = 1$$

$$\tau_c' = 0.25 \sqrt{25} = 1.25 \text{ N/mm}^2$$

$$\tau_v = 1.2234 \text{ N/mm}^2$$

$$\tau_v \leq \tau_v'$$

\therefore Hence depth assumed is ok

checking for f_b with actual size of loading

unit weight of concrete = 24 kN/m^3

unit weight of soil = $1.091 \times 10^{-6} \text{ kN/mm}^3$

Actual pressure loading below;

$$q_s = (1200 \times 2.5 \times 2.5) + (24 \times 0.660)$$

$$q_s = 214.94 \text{ kN/m}^2$$