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ASSIGNMENT

Question 1:

Linear transformation is a function from one vector space to another that respects the underlying structure of each vector space.

Examples;

1. For all $x, y, \in V$ $T(x + y) = T(x) + T(y)$ (T is additive)
2. $X \in V$ $r \in R$ $T(Rx) = rT(x)$ (T is homogeneous).

Question2:

Given the linear transformation of matrix operator on a vector X
compute $T(x)$

If $A(1,9,3)$ $(-2,6,7)$ $(0,-1,3)$

$$b = (2b - 2a) + -(-a)$$

$$\begin{pmatrix} 1 & -2 & 0 \\ 9 & 6 & -1 \\ 3 & 7 & 3 \end{pmatrix} = \begin{pmatrix} -1 \\ 4 \\ -8 \end{pmatrix}$$

Compute $T(a) \Rightarrow T(x) = Ae$

$$\begin{pmatrix} 1 \\ 9 \\ 3 \end{pmatrix} \begin{matrix} 5 \\ 2 \\ 2 \end{matrix} + \begin{pmatrix} -2 \\ 6 \\ 7 \end{pmatrix} \begin{matrix} 4 \\ 4 \\ 4 \end{matrix} + \begin{pmatrix} 0 \\ -1 \\ 3 \end{pmatrix} \begin{matrix} -8 \\ -8 \\ -8 \end{matrix}$$

$$\begin{pmatrix} 1 \times 1 \\ 9 \times 1 \\ 3 \times 1 \end{pmatrix} + \begin{pmatrix} -2 \times 4 \\ 6 \times 4 \\ 7 \times 4 \end{pmatrix} + \begin{pmatrix} 0 \times -8 \\ -1 \times -8 \\ 3 \times -8 \end{pmatrix}$$

$$\begin{pmatrix} 1 \\ 9 \\ 3 \end{pmatrix} + \begin{pmatrix} -8 \\ 12 \\ 28 \end{pmatrix} + \begin{pmatrix} 0 \\ 8 \\ -24 \end{pmatrix}$$

$$1 - 8$$

$$9 + 12 + 8$$

$$3 + 28 - 24$$

$$= \begin{pmatrix} -7 \\ 39 \\ 7 \end{pmatrix}$$

3. X Type equation here. Question 3 ;

Rank of a matrix is the maximum number of linearly independent rows in a matrix A is called the row rank of A and the maximum number linearly independent columns in A is called the column rank of A. Example of a rank matrix

Find the rank of a matrix using normal form,

$$A = \begin{pmatrix} 2 & 3 & 4 & 5 \\ 3 & 4 & 5 & 6 \\ 4 & 5 & 6 & 7 \\ 9 & 10 & 11 & 12 \end{pmatrix}$$

Solution:

Reduce the matrix to echelon form,

$$\begin{pmatrix} 2 & 3 & 4 & 5 \\ 3 & 4 & 5 & 6 \\ 4 & 5 & 6 & 7 \\ 9 & 10 & 11 & 12 \end{pmatrix} \longrightarrow \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 2 & 3 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$