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Answers

1. $\int e^x \sin x \, dx$

Using integration by Parts formula

$$\int u \, dv = uv - \int v \, du$$

$$u = \sin x \quad dv = e^x, \quad \frac{du}{dx} = \cos x \quad \therefore du = \cos x \, dx$$

$$v = \int e^x = e^x$$

$$\therefore \int \sin x e^x \, dx = \sin x \cdot e^x - \int e^x \cos x \, dx$$

$$= \sin x e^x - \int e^x \cos x \, dx$$

$$\int e^x \cos x \, dx =$$

$$u = \cos x \quad dv = e^x \quad \frac{du}{dx} = -\sin x \quad \therefore du = -\sin x \, dx$$

$$v = \int e^x = e^x$$

$$\int u \, dv = uv - \int v \, du$$

$$= \int \cos x e^x \, dx = \cos x \cdot e^x - \int e^x (-\sin x) \, dx$$

$$= \cos x e^x + \int \sin x e^x \, dx$$

$$\therefore \int \sin x e^{2x} dx = \sin x e^{2x} - (\cos x e^{2x} + \int \sin x e^{2x} dx)$$

$$\int \sin x e^{2x} dx = \sin x e^{2x} - \cos x e^{2x} - \int \sin x e^{2x} dx + C$$

$$2 \int \sin x e^{2x} dx = \sin x e^{2x} - \cos x e^{2x} + C_1$$

Divide through by 2

$$\int \sin x e^{2x} dx = \frac{1}{2} \sin x e^{2x} - \frac{1}{2} \cos x e^{2x} + \frac{C}{2}$$

$$\therefore \int \sin x e^{2x} dx = \frac{1}{2} \sin x e^{2x} - \frac{1}{2} \cos x e^{2x} + C$$

where $C = \frac{C}{2}$

2. $\int 2x^2 \ln x dx$

Using integration by parts formula

$$\int u dv = uv - \int v du$$

$$u = \ln x \quad dv = 2x^2 \quad du/dx = 1/x \quad \therefore du = 1/x dx$$

$$v = \int 2x^2 = 2x^3/3$$

$$\therefore \int \ln x \cdot 2x^2 dx = \ln x \cdot \frac{2x^3}{3} - \int \frac{2x^2}{3} \cdot \frac{1}{x} dx$$

$$\therefore \int \ln x \cdot 2x^2 dx = \frac{2x^3}{3} \ln x - \int \frac{2x^2}{3} dx$$

$$= \frac{2x^3 \ln x}{3} - \frac{2x^3}{9} + C$$

$$3. \int x^2 \sin x \, dx$$

Using the integral formula

$$\int u \, dv = uv - \int v \, du$$

$$\therefore u = x^2 \quad dv = \sin x \quad v = \int \sin x \, dx = -\cos x$$

$$\frac{du}{dx} = 2x \quad \therefore du = 2x \, dx$$

$$\begin{aligned} \int x^2 \sin x \, dx &= x^2 \cdot (-\cos x) - \int -\cos x \cdot 2x \, dx \\ &= -x^2 \cos x + \int 2x \cos x \, dx \\ &= -x^2 \cos x + \int 2x \cos x \, dx \end{aligned}$$

$$\int 2x \cos x \, dx$$

$$\int u \, dv = uv - \int v \, du$$

$$u = 2x, \quad dv = \cos x, \quad v = \int \cos x \, dx = \sin x, \quad du = 2 \, dx$$

$$\therefore \int 2x \cos x \, dx = 2x \sin x - \int 2 \sin x \, dx$$

$$= 2x \sin x - 2(-\cos x) + C$$

$$= 2x \sin x + 2 \cos x + C$$

$$\therefore \int x^2 \sin x \, dx = -x^2 \cos x + 2x \sin x + 2 \cos x + C$$

$$4. \int x \cos x \, dx$$

Using the integration by parts formula

$$\int u \, dv = uv - \int v \, du$$

$$u = x \quad dv = \cos x \quad \frac{du}{dx} = 1 \quad \therefore du = dx, \quad v = \int \cos x = \sin x$$

$$\therefore \int x \cos x \, dx = x \cdot \sin x - \int \sin x \cdot dx$$

$$\therefore \int x \cos x \, dx = x \sin x - (-\cos x) + C$$

$$= \int x \cos x \, dx = x \sin x + \cos x + C$$

