

NWOKORIE PASCAL CHINWAMI

MECHATRONICS ENGINEERING

19/ENG05/043

1) $e^{2x} \sin x \, dx$

let $u = e^{2x}$, $dv = \sin x$

$\frac{du}{dx} = 2e^{2x}$ $v = -\cos x$

Using UV - $\int v \, du$

$(e^{2x})(-\cos x) - \int (-\cos x)(2e^{2x}) \, dx$

$= -e^{2x} \cos x - \int -2e^{2x} \cos x \, dx$

$\int -2e^{2x} \cos x \, dx = \left[\begin{array}{l} \text{let } u = -e^{2x}, \, dv = \cos x \\ \frac{du}{dx} = -2e^{2x} \cdot v = \sin x \end{array} \right] \text{AE}$

$\left[(-e^{2x})(\sin x) - (-\cos x)(-e^{2x}) \right] \text{AE}$
 $(-e^{2x} \sin x - e^{2x} \cos x) + C$

$\int e^{2x} \sin x \, dx =$

$-e^{2x} \cos x + e^{2x} \sin x + e^{2x} \cos x + C$

$= e^{2x} \sin x + C$

2) $2x^2 \ln x \, dx$

let $u = 2x^2$, $dv = \ln x$

$\frac{du}{dx} = 4x$ $v = 1/x$

Using UV - $\int v \, du$

$(2x^2)(1/x) - \int (1/x)(4x) \, dx$

$\frac{2x^2}{x} - \int \frac{4x}{x} = \frac{2x^2}{x} - 4 \int \frac{x}{x} = \frac{2x^2}{x} - 4 \int 1$

$= 2x - 4x + C$

3) $x^2 \sin x \, dx$

let $u = x^2$, $dv = \sin x$

$\frac{du}{dx} = 2x$ $v = -\cos x$

Using UV - $\int v \, du$

$$(x^2) (-\cos x) - \int (-\cos x)(2x) dx$$

$$\int -2x \cos x dx = \begin{cases} \text{let } u = -2x, & dv = \cos x \\ \frac{du}{dx} = -2, & v = \sin x \end{cases}$$

$$(-2x)(\sin x) - \int \sin x (-2) dx$$

$$[-2x \sin x + 2(-\cos x)] + C$$

$$[-2x \sin x - 2 \cos x] + C$$

$$\int x^2 \sin x dx =$$

$$-x^2 \cos x + 2x \sin x + 2 \cos x + C$$

$$4) \int x \cos x dx$$

$$\text{let } u = x, \quad dv = \cos x$$

$$\frac{du}{dx} = 1, \quad v = \sin x$$

$$\text{Using } uv - \int v du$$

$$(x)(\sin x) - \int (\sin x)(1) dx$$

$$x \sin x - (-\cos x) + C$$

$$\int x \cos x dx$$

$$= x \sin x + \cos x + C$$