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Matric No - 19/Suger/016

MAT 104

1) $\int x^{1/2} \ln x$

$u = \ln x \quad dv = x^{1/2}$

$\frac{du}{dx} = \frac{1}{x} \quad dv = x^{1/2} \quad \int v \cdot \frac{du}{dx} = \frac{x^{3/2}}{3/2}$

$\int x^{1/2} \ln x = \ln x \cdot \frac{x^{3/2}}{3/2} - \int \frac{x^{3/2}}{3/2} \cdot \frac{1}{x}$

$\int x^{1/2} \ln x = \ln x \cdot \frac{x^{3/2}}{3/2} - \frac{x^{1/2}}{1/2} \ln x + C$

$= \ln x \left[\frac{2x^{3/2}}{3} - \frac{1}{2} x^{1/2} \right] + C$

2) $\int 2 \cos 6t \cos 4t$

$\cos A \cos B = \frac{1}{2} (\cos(A+B) + \cos(A-B))$

$A = 6t, B = 4t$

$= \frac{1}{2} \int 2 (\cos 7t + \cos 5t)$

$= \int (\cos 7t + \cos 5t)$

$= \frac{\sin 7t}{7} + \frac{\sin 5t}{5} + C$

$$\int \sin^3 x \cos^2 x \, dx$$
$$\int u^4 \sin^2 x \frac{du}{\sin x}$$

$$= \int u^4 \sin^2 x \, dx$$
$$= \int u^4 \sin^2 x \, du$$

recall that

$$\sin^2 x + \cos^2 x = 1$$

$$\sin^2 x = 1 - \cos^2 x$$

$$\int \sin^2 x \, dx$$

$$\int (1 - \cos^2 x) \, dx$$

$$= \int (1 - u^2) \, dx$$

$$= \int (u^4 - u^6) \, dx$$

$$= \left[\frac{u^{4+1}}{4+1} - \frac{u^{6+1}}{6+1} \right] + C$$

$$= \left[\frac{u^5}{5} - \frac{u^7}{7} \right] + C$$

$$= \left[\frac{(\cos x)^5}{5} - \frac{(\cos x)^7}{7} \right] + C$$