

SN: 206

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Matric No: 19/ENGO4/032

1. a) $x = t$

$$y = t^2$$

$$z = t^3$$

$$r = t\mathbf{i} + t^2\mathbf{j} + t^3\mathbf{k}$$

$$\frac{dr}{dt} = \mathbf{i} + 2t\mathbf{j} + 3t^2\mathbf{k}$$

When $t = 1$

$$\left| \frac{dr}{dt} \right| = \mathbf{i} + 2\mathbf{j} + 3\mathbf{k}$$

$$\left| \frac{dr}{dt} \right| = \sqrt{(1)^2 + (2)^2 + (3)^2}$$

$$= \sqrt{1 + 4 + 9}$$

$$= \sqrt{14} = 3.74$$

$$T = \frac{da/dt}{|dn/dt|}$$

$$= \frac{\mathbf{i} + 2\mathbf{j} + 3\mathbf{k}}{3.74}$$

$$= \frac{\mathbf{i}}{3.74} + \frac{2\mathbf{j}}{3.74} + \frac{3\mathbf{k}}{3.74}$$

$$= \frac{\mathbf{i}}{3.74} + \frac{2\mathbf{j}}{3.74} + \frac{3\mathbf{k}}{3.74}$$

$$20 \quad A = 4t^3 \mathbf{j} + 5\mathbf{k}$$

$$B = 2t^2 \mathbf{i} + 4t \mathbf{j}$$

$$G = A \times B$$

$$G = \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ 0 & 4t^3 & 5 \\ 2t^2 & 4t & 0 \end{vmatrix}$$

$$G = \mathbf{i} \begin{vmatrix} 4t^3 & 5 \\ 4t & 0 \end{vmatrix} - \mathbf{j} \begin{vmatrix} 0 & 5 \\ 2t^2 & 6 \end{vmatrix} + \mathbf{k} \begin{vmatrix} 0 & 4t^3 \\ 2t^2 & 4t \end{vmatrix}$$

$$G = \mathbf{i}(0 - 20t) - \mathbf{j}(0 - 10t^2) + \mathbf{k}(0 - 8t^5)$$

$$G = -20t \mathbf{i} + 10t^2 \mathbf{j} - 8t^5 \mathbf{k}$$

$$\int G = \int -20t \mathbf{i} + 10t^2 \mathbf{j} - 8t^5 \mathbf{k} \, dt$$

$$= \left[\frac{-20t^2 \mathbf{i}}{2} + \frac{10t^3 \mathbf{j}}{3} - \frac{8t^6 \mathbf{k}}{6} \right]$$

$$= \left[-10t^2 \mathbf{i} + \frac{10t^3 \mathbf{j}}{3} - \frac{4t^6 \mathbf{k}}{3} \right]$$

$$= \left[-10(1)^2 \mathbf{i} + \frac{10(1)^3 \mathbf{j}}{3} - \frac{4(1)^6 \mathbf{k}}{3} \right] - [0]$$

$$= 10 \mathbf{i} + \frac{10 \mathbf{j}}{3} - \frac{4 \mathbf{k}}{3}$$

$$= 10 \mathbf{i} + 3.33 \mathbf{j} - 1.33 \mathbf{k}$$