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DEPARTMENT: COMPUTER SCIENCE
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$$1. \int e^x \sin x \, dx$$

$$u = \sin x \quad dv = e^x$$

$$\frac{du}{dx} = \cos x \quad v = e^x$$

$$du = \cos x \, dx$$

$$\int u \, dv = uv - \int v \, du$$

$$= (\sin x)(e^x) - \int (e^x)(\cos x \, dx)$$

$$= e^x \sin x - \int e^x \cos x \, dx$$

$$u = \cos x \quad dv = e^x$$

$$\frac{du}{dx} = -\sin x \quad v = e^x$$

$$du = -\sin x \, dx$$

$$= e^x \cos x + \int e^x \sin x \, dx$$

$$= e^x \sin x - (e^x \cos x + \int e^x \sin x \, dx)$$

$$= e^x \sin x - e^x \cos x - \int e^x \sin x \, dx$$

$$I = e^x \sin x - e^x \cos x - \int e^x \sin x \, dx$$

$$\text{Let } I = \int e^x \sin x \, dx$$

$$I = e^x \sin x - e^x \cos x - I$$

$$\frac{2I}{2} = \frac{e^x \sin x - e^x \cos x}{2}$$

2

2

$$= \frac{e^x \sin x - e^x \cos x}{2}$$

2

$$2. \int 2x^2 \ln x \, dx$$

$$u = \ln x \quad dv = 2x^2$$

$$du/dx = \frac{1}{x}, \quad v = \frac{2x^3}{3}$$

$$du = \frac{dx}{x}$$

$$\begin{aligned} \int u \, dv &= uv - \int v \, du \\ &= \ln x \cdot \frac{2x^3}{3} - \int \frac{2x^3}{3} \cdot \frac{dx}{x} \\ &= \frac{2x^3 \ln x}{3} - \frac{2}{3} \int x^2 \, dx \end{aligned}$$

$$= \frac{2x^3 \ln x}{3} - \frac{2x^3}{9} + C$$

$$= \frac{2x^3 \ln x}{3} - \frac{2x^3}{9} + C$$

$$= \frac{2x^3 (3 \ln x - 1)}{9} + C$$

$$3. \int x^2 \sin x \, dx$$

$$u = x^2 \quad dv = \sin x$$

$$du/dx = 2x \quad v = -\cos x$$

$$du = 2x \, dx$$

$$\begin{aligned} \int u \, dv &= uv - \int v \, du \\ &= -x^2 \cos x + \int (\cos x)(2x \, dx) \\ &= -x^2 \cos x + \int 2x \cos x \, dx \end{aligned}$$

$$u = 2x \quad dv = \cos x$$

$$du/dx = 2 \quad v = \sin x$$

$$du = 2 \, dx$$

$$= 2x \sin x - \int 2 \sin x \, dx$$

$$= -x^2 \cos x + 2x \sin x - \int 2 \sin x dx$$

$$= -x^2 \cos x + 2x \sin x + 2 \cos x + C$$

$$= 2x \sin x + (2 - x^2) \cos x + C$$

$$4. \int x \cos x dx$$

$$u = x \quad dv = \cos x$$

$$du/dx = 1 \quad v = \sin x$$

$$du = dx$$

$$\int u dv = uv - \int v du$$

$$= x \sin x - \int \sin x dx$$

$$= x \sin x + \cos x + C$$