

$$u_t - C u_{xx} = 0$$

$$\frac{du}{dt} - C \frac{d^2u}{dx^2} = 0$$

$$\frac{du}{dt} = \frac{C d^2u}{dx^2}$$

$$\frac{u_{i,j+1} - u_{i,j}}{\Delta t} = C \frac{u_{i+1,j} - 2u_{i,j} + u_{i-1,j}}{\Delta x^2}$$

$$u_{i,j+1} - u_{i,j} = \frac{C \Delta t}{\Delta x^2} [u_{i+1,j} - 2u_{i,j} + u_{i-1,j}] \quad r = \frac{C \Delta t}{\Delta x^2}$$

$$u(x, 0) = x^4 k$$

$$\Delta x = 0.2 \text{ m}, \quad \Delta t = 0.02 \text{ day}$$

for initial conditions

$$\text{At } x=0 \rightarrow x^4 = 0$$

$$\text{At } x=0.2 \rightarrow 0.2^4 = 1.6 \times 10^{-3}$$

$$\text{At } x=0.4 \rightarrow 0.4^4 = 0.0256$$

$$\text{At } x=0.6 \rightarrow 0.6^4 = 0.1296$$

$$\text{At } x=0.8 \rightarrow 0.8^4 = 0.4096$$

$$\text{At } x=1 \rightarrow 1^4 = 1$$

$$u_{i,j+1} = u_{i,j} + r [u_{i+1,j} - 2u_{i,j} + u_{i-1,j}]$$

$$u_{i,j+1} = r u_{i-1,j} + (1-2r) u_{i,j} + r u_{i+1,j} \quad \leftarrow *$$

when $i=1, j=0$

$$u_{1,1} = 0.5 u_{0,0} + 0.5 u_{2,0}$$

$$= 0.5(0) + 0.5(0.0256)$$

$$u_{1,1} = 0.0128$$

when $i=2, j=0$

$$u_{2,1} = 0.5(u_{1,0}) + 0.5(u_{3,0})$$

$$= 0.5(1.6 \times 10^{-3}) + 0.5(0.1296)$$

$$u_{2,1} = 0.0656$$

$$\begin{aligned} \text{when } i=3, j=0 &= U_{3,1} = 0.5(U_{2,0}) + 0.5(U_{4,0}) \\ &= 0.5(0.0256) + 0.5(0.4096) \\ U_{3,1} &= 0.2176 \end{aligned}$$

$$\begin{aligned} \text{when } i=4, j=0 &= U_{4,1} = 0.5(U_{3,0}) + 0.5(U_{5,0}) \\ &= 0.5(0.0256) + 0.5(0.4096) \\ U_{4,1} &= 0.5648 \end{aligned}$$

for j=1.

$$\begin{aligned} \text{when } i=1 & \therefore U_{1,2} = 0.5(U_{0,1}) + 0.5(U_{2,1}) \\ &= 0.5U_{0,1} + 0.5U_{2,1} = 0 + 0.5(0.0656) \\ U_{1,2} &= 0.0328 \end{aligned}$$

$$\begin{aligned} \text{when } i=2 & \therefore U_{2,2} = 0.5(U_{1,1}) + 0.5(U_{3,1}) \\ &= 0.5(0.0128) + 0.5(0.2176) \\ U_{2,2} &= 0.1152 \end{aligned}$$

$$\begin{aligned} \text{when } i=3 & U_{3,2} = 0.5(U_{0,1}) + 0.5(U_{4,1}) \\ &= 0.5(0.0656) + 0.5(0.5648) \\ U_{3,2} &= 0.3152 \end{aligned}$$

$$\begin{aligned} \text{when } i=4 & U_{4,2} = 0.5(U_{2,1}) + 0.5(U_{5,1}) \\ &= 0.5(0.2176) + 0.5(1) \\ U_{4,2} &= 0.6088 \end{aligned}$$

for j=2

$$\begin{aligned} \text{when } i=1 & \therefore U_{1,3} = 0.5(U_{0,2}) + 0.5(U_{2,2}) \\ &= 0 + 0.5(0.1152) = 0.0576 \end{aligned}$$

$$\begin{aligned} \text{when } i=2 & U_{2,3} = 0.5(U_{1,2}) + 0.5(U_{3,2}) \\ &= 0.5(0.0328) + 0.5(0.3152) = 0.174 \end{aligned}$$

$$\begin{aligned} \text{when } i=3 & U_{3,3} = 0.5(U_{2,2}) + 0.5(U_{4,2}) \\ &= 0.5(0.1152) + 0.5(0.6088) = 0.362 \end{aligned}$$

$$= 0.5(0.3152) + 0.5(1)$$

$$U_{4,3} = 0.6576$$

for $J=3$

$$\text{when } i=1 \quad U_{1,4} = 0.5(U_{0,3}) + 0.5(U_{2,3})$$

$$= 0.5(0) + 0.5(0.174) = 0.087$$

$$\text{when } i=2 \quad U_{2,4} = 0.5(U_{1,3}) + 0.5(U_{3,3})$$

$$= 0.5(0.0576) + 0.5(0.362) = 0.2098$$

$$\text{when } i=3 \quad U_{3,4} = 0.5(U_{2,3}) + 0.5(U_{4,3})$$

$$= 0.5(0.174) + 0.5(0.6576) = 0.4158$$

$$\text{when } i=4 \quad U_{4,4} = 0.5(U_{3,3}) + 0.5(U_{5,3})$$

$$= 0.5(0.362) + 0.5(1)$$

$$= 0.681$$

for $J=4$

$$\text{when } i=1 \quad U_{1,5} = 0.5(U_{0,4}) + 0.5(U_{2,4})$$

$$= 0.5(0) + 0.5(0.087) = 0.0435$$

$$\text{when } i=2 \quad U_{2,5} = 0.5(U_{1,4}) + 0.5(U_{3,4})$$

$$= 0.5(0.0435) + 0.5(0.4158) = 0.22965$$

$$\text{when } i=3 \quad U_{3,5} = 0.5(U_{2,4}) + 0.5(U_{4,4})$$

$$= 0.5(0.2098) + 0.5(0.681)$$

$$= 0.4454$$

$$\text{when } i=4 \quad U_{4,5} = 0.5(U_{3,4}) + 0.5(U_{5,4})$$

$$= 0.5(0.4158) + 0.5(1)$$

$$= 0.7079$$

J Temp (K)						
5	0	0.1049	0.2514	0.4454	0.7079	1
4	0	0.087	0.2098	0.4158	0.681	1
3	0	0.0576	0.174	0.362	0.6576	1
2	0	0.0328	0.1152	0.3152	0.6008	1
1	0	0.0128	0.0656	0.2176	0.5648	1
0	0	0.0016	0.0256	0.1296	0.4096	1
	0	0.0	0.4	0.6	0.8	1