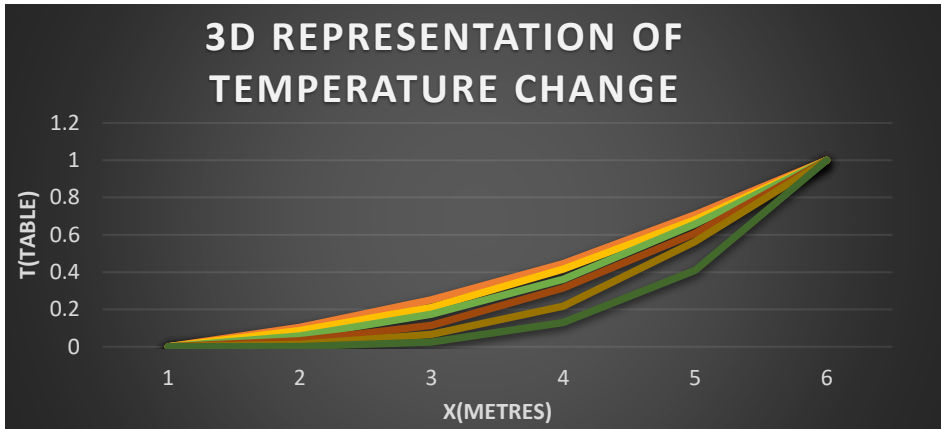


	0.1	0	0.1049	0.2514	0.4454	0.7079	1
	0.08	0	0.087	0.2098	0.4158	0.681	1
	0.06	0	0.0576	0.174	0.362	0.6576	1
	0.04	0	0.0328	0.1152	0.3152	0.6088	1
	0.02	0	0.0128	0.0656	0.2176	0.5648	1
	0	0	0.0016	0.0256	0.1296	0.4096	1
		0	0.2	0.4	0.6	0.8	1
0.5							



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MATRIC NO: 18/ENG02/102

DEPARTMENT: COMPUTER ENGINEERING

ENGINEERING MATHEMATICS (VI)

$$u_t - (u_{xx}) = 0$$

$$\frac{du}{dt} - C \frac{d^2u}{dx^2} = 0$$

$$\frac{du}{dt} = C \frac{d^2u}{dx^2}$$

$$\frac{u_{i,j+1} - u_{i,j}}{\Delta t} = C \frac{u_{i+1,j} - 2u_{i,j} + u_{i-1,j}}{\Delta x^2}$$

$$u_{i,j+1} - u_{i,j} = \frac{C \Delta t}{\Delta x^2} [u_{i+1,j} - 2u_{i,j} + u_{i-1,j}]$$

$$u_{i,j+1} - u_{i,j} = \frac{C \Delta t}{\Delta x^2} [u_{i+1,j} - 2u_{i,j} + u_{i-1,j}] \cdot r_2 \frac{\Delta t}{\Delta x^2} = 1$$

$$u[x, 0] = x^4 K$$

$$\Delta x = 0.2 \text{ m}, \Delta t = 0.02 \text{ day}$$

for initial conditions

$$\text{At } x = 0 \rightarrow x^4 = 0$$

$$\text{At } x = 0.2 \rightarrow 0.2^4 = 1.6 \times 10^{-3}$$

$$i=2, u_{2,1} = r u_{1,0} + (1-2r) u_{2,0} + r u_{3,0}$$

$$= 0.5(0.4) + (1-2 \times 0.8) 0.8 + 0.5(0.8)$$

$$= 0.2 + 0.4 = 0.6$$

$$i=3, u_{3,1} = r u_{2,0} + (1-2r) u_{3,0} + r u_{4,0}$$

$$= 0.5(0.8) + (0) 0.8 + 0.5(0.4)$$

$$= 0.4 + 0 + 0.2 = 0.6$$

$$i=4, u_{4,1} = r u_{3,0} + (1-2r) u_{4,0} + r u_{5,0}$$

$$j=1$$

$$u_{i,2} = r u_{i+j,1} + (1-2r) u_{i,1} + r u_{i+1,1}$$

$$i=1 \quad u_{1,2}$$

$$i=2 \quad u_{2,2}$$

$$i=3 \quad u_{3,2}$$

$$i=4 \quad u_{4,2}$$

$$j=2 \dots$$

$$u_{i,j+1} = r u_{i-1,j} + (1-2r) u_{i,j} + r u_{i+1,j}$$

for $j=1$

$$\begin{aligned}\text{when } i=1 & \therefore U_{1,2} = 0.5(U_{0,1}) + 0.5(U_{2,1}) \\ & = 0.5U_{0,1} + 0.5U_{2,1} = 0 + 0.5(0.0656)\end{aligned}$$

$$U_{1,2} = 0.0328$$

$$\text{when } i=2 \therefore U_{2,2} = 0.5(U_{1,1}) + 0.5(U_{3,1})$$

$$= 0.5(0.0128) + 0.5(0.2176)$$

$$U_{2,2} = 0.1152$$

$$\text{when } i=3 \therefore U_{3,2} = 0.5(U_{0,1}) + 0.5(U_{4,1})$$

$$= 0.5(0.0656) + 0.5(0.5648)$$

$$U_{3,2} = 0.3152$$

$$\text{when } i=4 \therefore U_{4,2} = 0.5(U_{2,1}) + 0.5(U_{5,1})$$

$$= 0.5(0.2176) + 0.5(1)$$

$$U_{4,2} = 0.6088$$

for $J=2$

$$\text{when } i=1 \therefore U_{1,3} = 0.5(U_{0,1}) + 0.5(U_{2,2})$$

$$= 0 + 0.5(0.1152) = 0.0576$$

$$\text{when } i=2 \therefore U_{2,3} = 0.5(U_{1,2}) + 0.5(U_{3,2})$$

$$= 0.5(0.0328) + 0.5(0.3152) = 0.174$$

$$\text{when } i=3 \therefore U_{3,3} = 0.5(U_{2,2}) + 0.5(U_{4,2})$$

$$= 0.5(0.1152) + 0.5(0.6088) = 0.362$$

$$\text{when } i=4 \therefore U_{4,3} = 0.5(U_{3,2}) + 0.5(U_{5,2})$$

$$= 0.5(0.3152) + 0.5(1)$$

$$u_{4,3} = 0.6576$$

For $J=3$

$$\text{when } i=1 \quad u_{1,4} = 0.5(u_{0,3}) + 0.5(u_{2,3})$$

$$= 0.5(0) + 0.5(0.174) = 0.087$$

$$\text{when } i=2 \quad u_{2,4} = 0.5(u_{1,3}) + 0.5(u_{3,3})$$

$$= 0.5(0.0576) + 0.5(0.362) = 0.2098$$

$$\text{when } i=3 \quad u_{3,4} = 0.5(u_{2,3}) + 0.5(u_{4,3})$$

$$= 0.5(0.174) + 0.5(0.6576) = 0.4158$$

$$\text{when } i=4 \quad u_{4,4} = 0.5(u_{3,3}) + 0.5(u_{5,3})$$

$$= 0.5(0.362) + 0.5(0)$$

$$= 0.181$$

For $J=4$

$$\text{when } i=1 \quad u_{1,5} = 0.5(u_{0,4}) + 0.5(u_{2,4})$$

$$= 0.5(0.2098) = 0.1049$$

$$\text{when } i=2 \quad u_{2,5} = 0.5(u_{1,4}) + 0.5(u_{3,4})$$

$$= 0.5(0.087) + 0.5(0.4158) = 0.2514$$

$$\text{when } i=3 \quad u_{3,5} = 0.5(u_{2,4}) + 0.5(u_{4,4})$$

$$= 0.5(0.2098) + 0.5(0.681)$$

$$= 0.4454$$

when $i=4$

$$u_{4,5} = 0.5(u_{3,4}) + 0.5(u_{5,4})$$

$$= 0.5(0.24158) + 0.5(1)$$

$$= \underline{\underline{0.7079}}$$