

BAKARE KEHINDE HAMMEEDAT

19/ENG03/032

CIVIL ENGINEERING

ENG 234: ENG MECHANICS

1. For the $v-t$ graph
At time $0 \leq t < 6$ secs
 $s = 0.5t^3$

using the relationship $v = \frac{ds}{dt}$

$$v = 1.5t^2$$

At time $6 \leq t \leq 10$ secs

$$s = 108$$

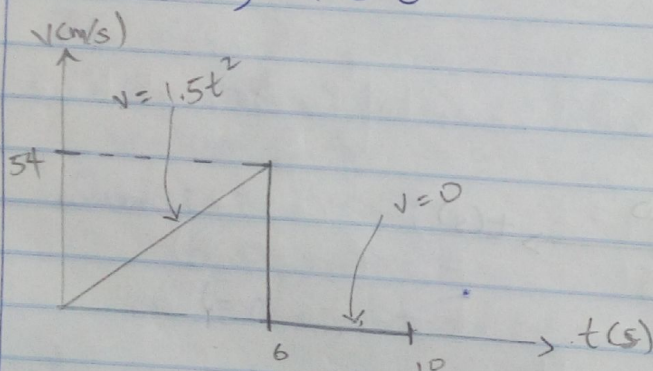
$$\therefore v = 0$$

$$\text{At } t=0, v=0$$

$$t=6, v=54$$

$$t=8, v=0$$

$$t=10, v=0$$



2. For the $s-t$ graph

At time $0 \leq t < 20$ secs

using the relationship $s = \int v dt$

$$v = -4t + 80$$

$$s = \int -4t + 80 dt$$

$$s = -2t^2 + 80t + C$$

since $s=0$ when $t=0$

$$0 = 0 + 0 + C$$

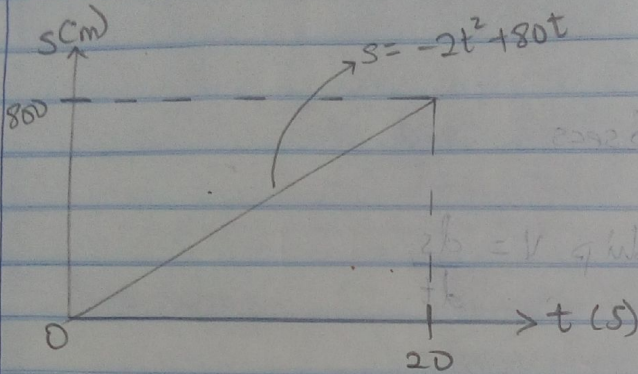
$$C = 0$$

$$\therefore s = -2t^2 + 80t$$

When $t=0, s=0$

$t=10, s=60$

$t=20, s=80$



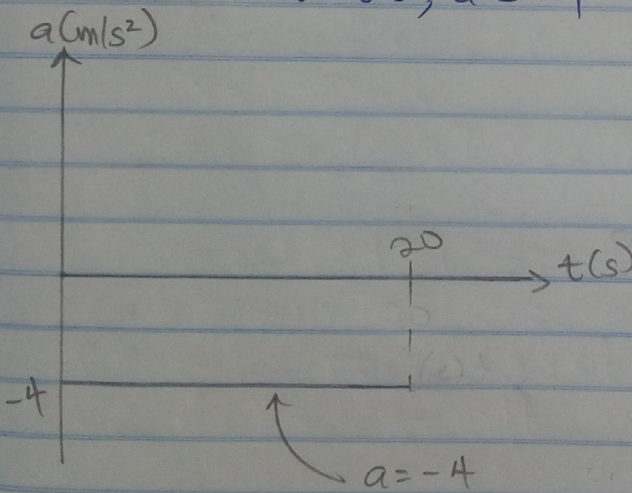
For the a-t graph

$$a = \frac{dv}{dt}$$

$$a = -4$$

at time $t=0, a = -4$

$t=20, a = -4$



3. For the a-s graph

at $0 \leq t \leq 40$

$$v = 0.25s$$

using the relationship

$$ads = v dv$$

$$a = v \cdot \frac{dv}{ds}$$

$$\frac{dv}{ds} = 0.25$$

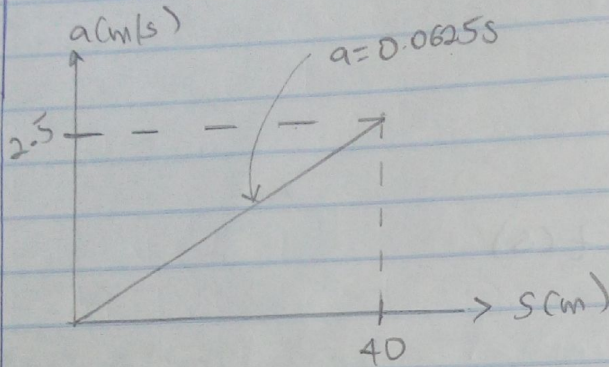
$$a = 0.25 \times 0.25 s$$

$$a = 0.0625 s$$

$$\text{at } s=0, a=0$$

$$s=20, a=1.25 \text{ m/s}^2$$

$$\text{at } s=40, a=2.5 \text{ m/s}^2$$



4. For the v-t graph

At time $0 \leq t < 5$ secs

$$s = 3t^2$$

$$v = 6t$$

At time $5 \leq t \leq 10$ secs

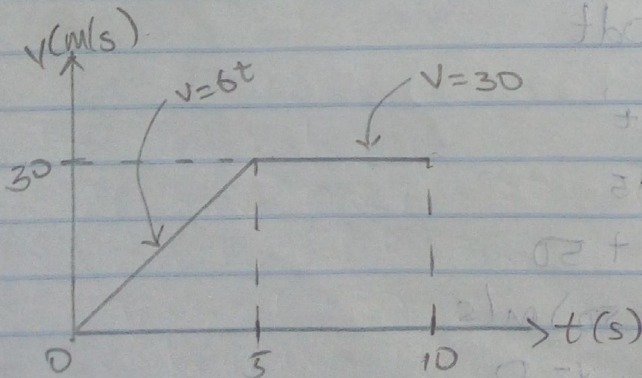
$$s = 30t - 75$$

$$v = 30 \text{ (m/s)}$$

When $t=0, v=0$

$$t=5, v=30$$

$$t=10, v=30$$



For the a-t graph

At time $0 \leq t < 5$

$$v = 6t$$

$$a = 6$$

At time $5 \leq t \leq 10$

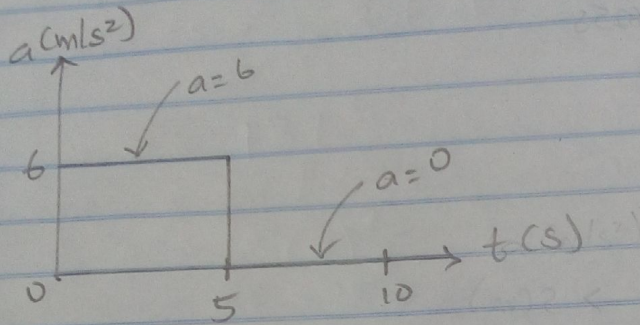
$$v = 30$$

$$a = 0$$

When $t = 0, a = 6$

$t = 5, a = 6$

$t = 10, a = 0$



5 $0 \leq t < 5$

$$v = \int_0^5 20 dt$$

$$v = 20t \Big|_0^5$$

$$v = 100 \text{ m/s}$$

using this as the initial condition for the next time period

$5 \leq t < t'$

$$a = -10 \text{ m/s}^2$$

$$\int_{100}^v dv = \int_5^{t'} -10 dt$$

$$v - 100 = -10 \Big|_5^{t'}$$

$$v - 100 = -10t' + 50$$

$$v = (-10t' + 150) \text{ m/s}$$

when $t = t', v = 0$

$$0 = -10t' + 150$$

$$10t' = 150$$

$$t' = 15 \text{ s}$$

$$220.0 \times 20.0 = 0$$

$$2200.0 = 0$$

$$0 = 2 \text{ to}$$

$$0.0 = 2$$

$$0 = 2 \text{ to}$$

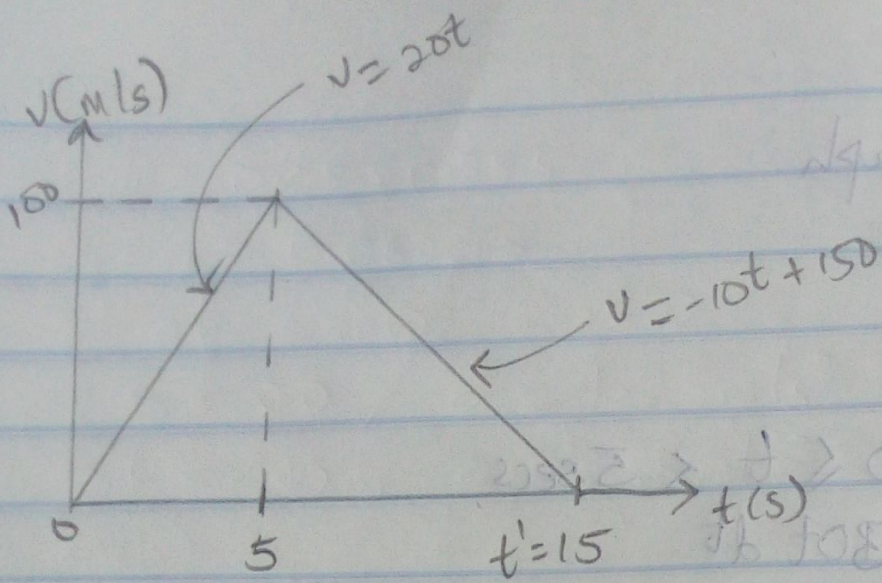
$$0 = 2 \text{ to}$$

For the v-t graph
At time $0 \leq t < 5$
 $\frac{dv}{dt} = 20$
 $v = 20t$

At time $5 \leq t < 10$
 $\frac{dv}{dt} = -10$
 $v = -10t + 150$
 $0 = -10t + 150$
 $10t = 150$
 $t = 15$

For the a-t graph
At time $0 \leq t < 5$
 $\frac{da}{dt} = 0$
 $a = 6$

At time $5 \leq t < 10$
 $\frac{da}{dt} = 0$
 $a = 0$



$$2b = v$$

$$\frac{2b}{t} = v$$

$$2b = vt$$

$$2b = vt$$

$$2b = 20t \cdot t$$

$$2b = 20t^2$$

$$t^2 = \frac{2b}{20}$$

$$t = \sqrt{\frac{2b}{20}}$$

6. For the s-t graph
 At time $v = 30t$
 $s = \int_0^5 30t dt$

$$2b = vt$$

$$2b = 20t^2$$

$$t = \sqrt{\frac{2b}{20}}$$

6. For the s-t graph

$$v = \frac{ds}{dt}$$

$$\int ds = \int v dt$$

At time $0 \leq t < 5$ secs

$$\int_0^5 ds = \int_0^5 30t dt$$

$$s = 15t^2$$

when $t = 5$ s

$$s = 15(5)^2$$

$$s = 375 \text{ m}$$

using this as the initial condition for the next time frame.

at time $5 \leq t \leq 15$ secs

$$v = (-15t + 225) \text{ m/s}$$

$$\int_{375}^s ds = \int_5^t (-15t + 225) dt$$

$$s - 375 = -7.5t^2 + 225t \Big|_5^t$$

$$s - 375 = (-7.5t^2 + 225t) - [(-7.5 \times 5^2) + (225 \times 5)]$$

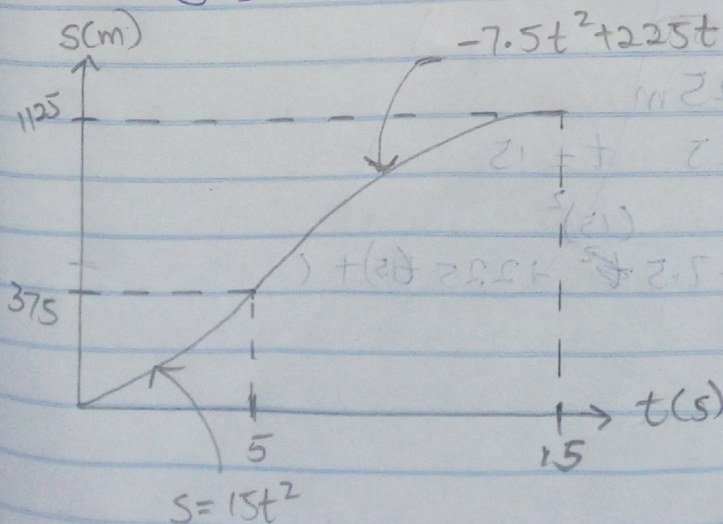
$$s - 375 = -7.5t^2 + 225t - (-937.5)$$

$$s = (-7.5t^2 + 225t + 562.5) \text{ m}$$

when $t = 15$ s

$$s = (-7.5(15^2) + 225(15) + 562.5)$$

$$s = 1125 \text{ m}$$



ALL GRAPHICAL SOLUTIONS DRAWN TO SCALE

