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1) Acceleration = $\frac{\Delta V}{\Delta t}$

Since we are dealing with position vectors.

Let $P(x, y, z)$ be any point on the given curve and $\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$ be the position vector of P relative to O as origin

Substituting x, y, z in \vec{r}

$$\text{we have } \vec{r} = (t)\hat{i} + (5t^2 + 7t)\hat{j} + (1 + 2t)\hat{k}$$

So acceleration vector \vec{a}

will be differential of \vec{r} with respect to t

$$\therefore \vec{a} = \frac{d\vec{r}}{dt} = 24\hat{i} + 10\hat{j} + 4\hat{k}$$

2) ~~If $P = t = t$~~

$$\begin{aligned} P \times Q &= (i - 9j - 4k) \times (8i - 3j + 6k) \\ &= 8i - 27j - 24k \end{aligned}$$

$$\begin{aligned} R \times P &= (i - 4j - 3k) \times (i - 9j - 4k) \\ &= (0 - 36j - 12k) \end{aligned}$$

$$\begin{aligned} (P \times Q) \cdot (R \times P) &= (8i - 27j - 24k) \cdot (0 - 36j - 12k) \\ &= 972j + 288k \end{aligned}$$

3) $F = 5\cos 7t \hat{i} + 2e^{3t} \hat{j} - 4t^3 \hat{k}$

$$R = 5\cos t \hat{i} - 2e^{3t} \hat{j} - 4t^3 \hat{k}$$

$$\int R dt = \frac{-5\sin 7t}{7} - \frac{2e^{4t}}{4} - \frac{4t^4}{4}$$