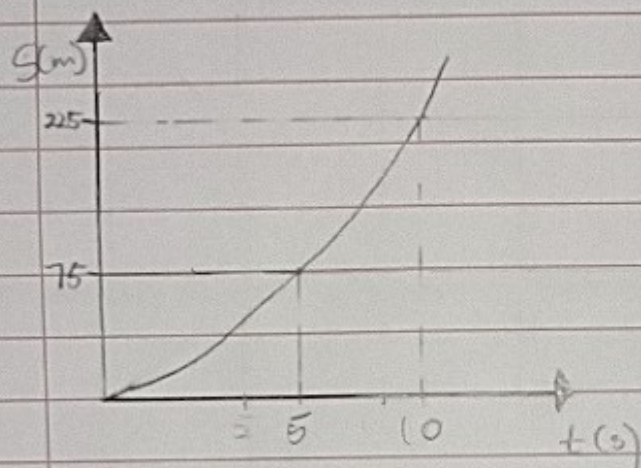


Q1 (F12-12)

Construct the  $v-t$  and  $a-t$  graph



Solutions:

$v-t$

$$v = \frac{ds}{dt}$$

at  $0 \leq t \leq 5$

$$s = 3t^2$$

$$v = 6t$$

at  $t = 5$ ,  $v = 30 \text{ m/s}$

at  $5 \leq t \leq 10$

$$s = 30t - 75$$

$$v = 30$$

at  $t = 10$ ,  $v = 30 \text{ m/s}$

$a-t$

$$a = \frac{dv}{dt}$$

at  $0 \leq t \leq 5$

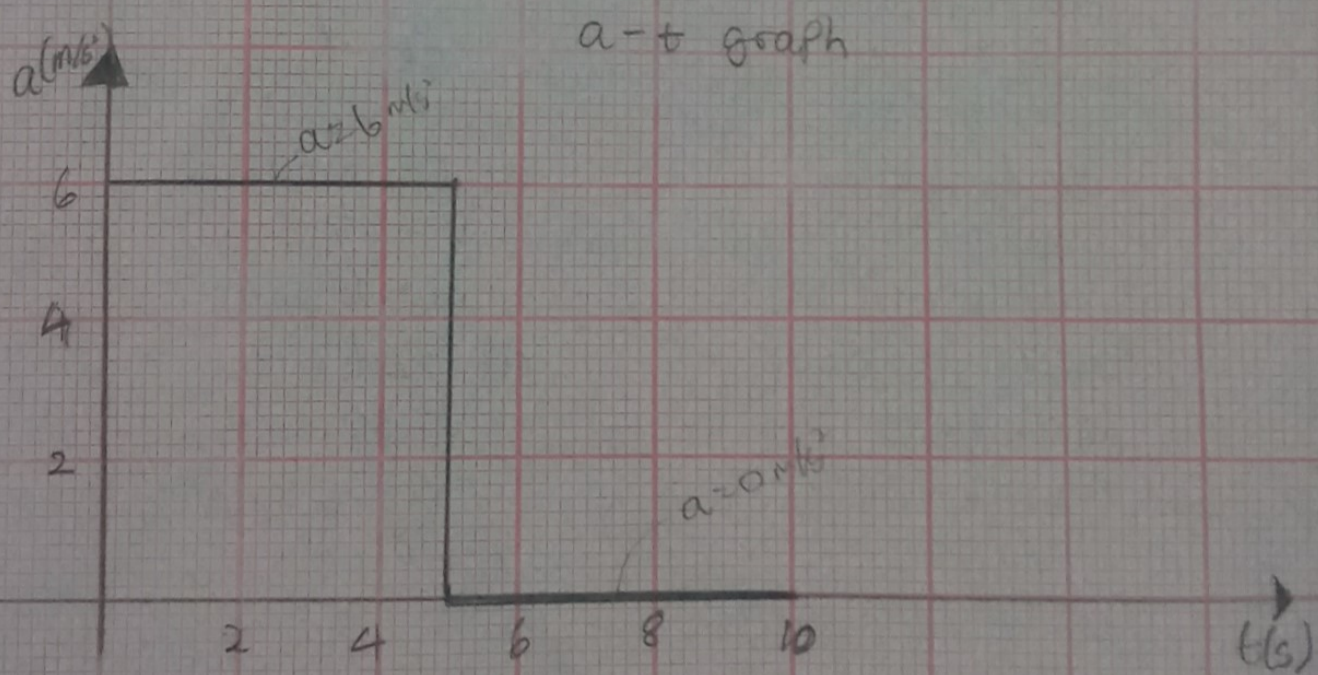
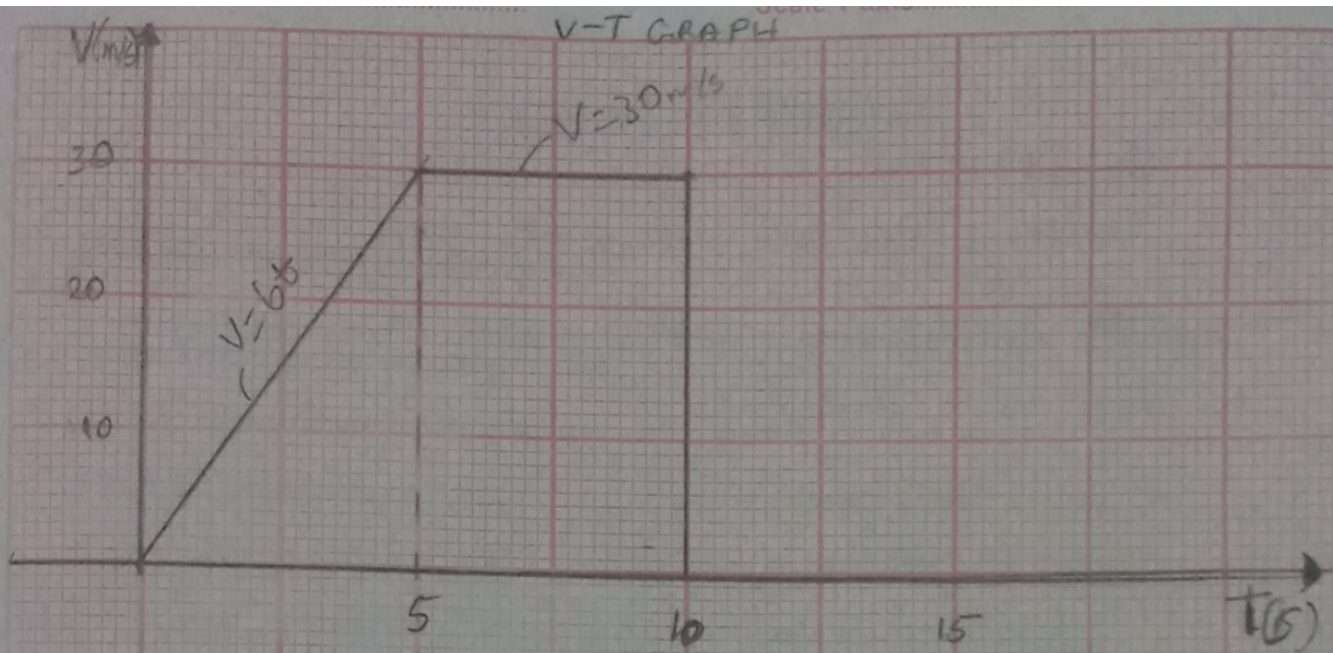
$$v = 6t$$

$$a = 6 \text{ m/s}^2$$

at  $5 \leq t \leq 10$

$$v = 30 \text{ m/s}$$

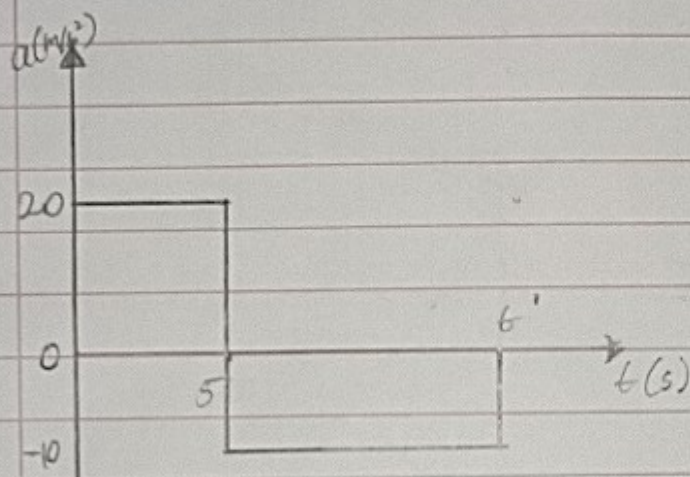
$$a = 0 \text{ m/s}^2$$





Q2 (F12-13)

Construct the  $V-t$  graph for  $0 \leq t \leq t'$



Solution:

at  $0 \leq t \leq 5$ ,

$$dv = a dt$$

$$\int_0^v dv = \int_0^t 20 dt$$

$$v = 20t$$

at  $t = 5$ ,

$$v = 20(5) = 100 \text{ m/s}$$

at  $5 \leq t \leq t'$

$$a = -10$$

$$\int_{100}^v dv = \int_5^t -10 dt$$

$$v - 100 = -10t + 50$$

$$v = -10t + 150$$

$$v = -10t + 150$$

$$\text{at } t = t', v = 0,$$

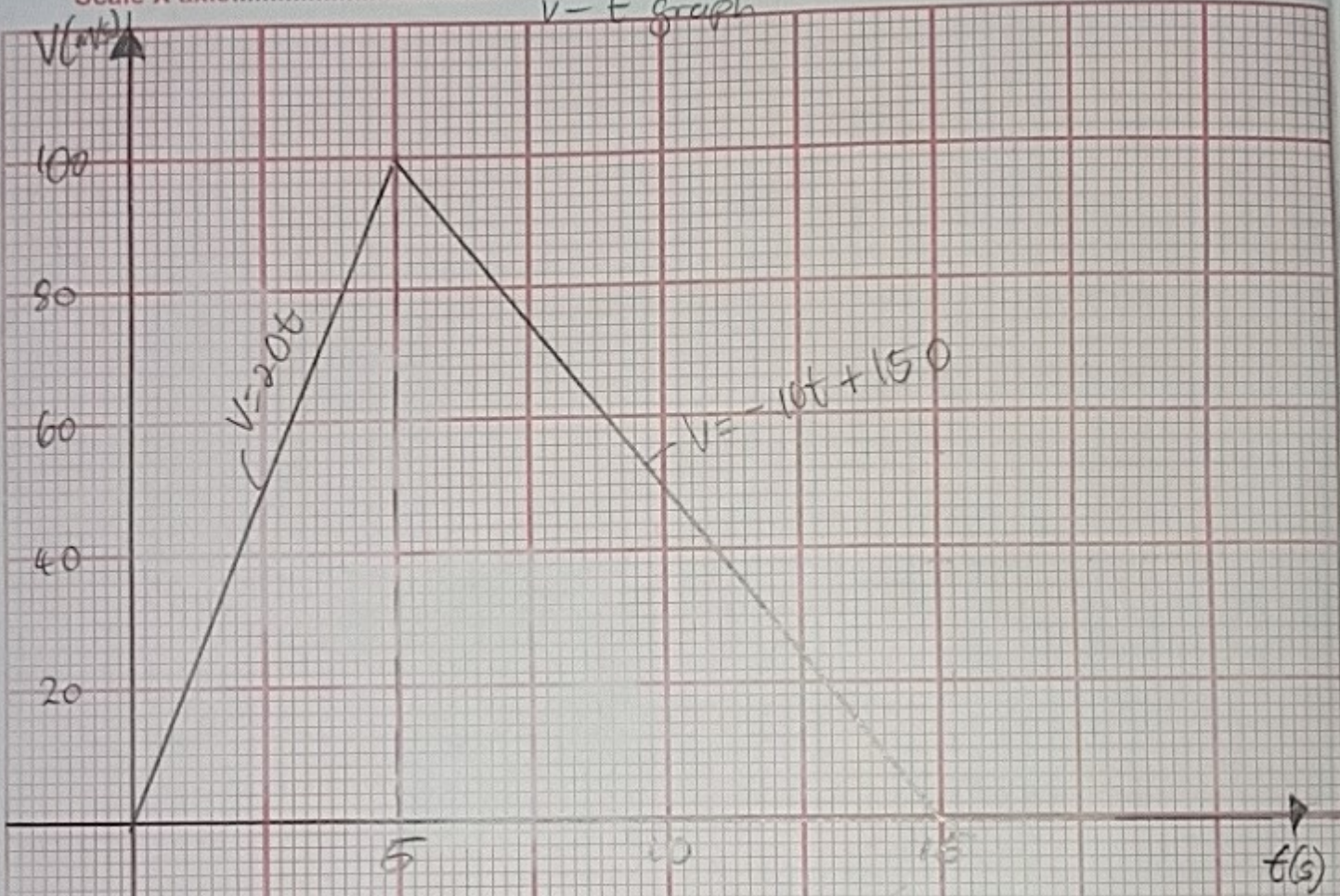
$$\therefore t = \frac{0 - 150}{-10} = 15$$



Scale X axis.....

Scale Y axis.....

v-t graph

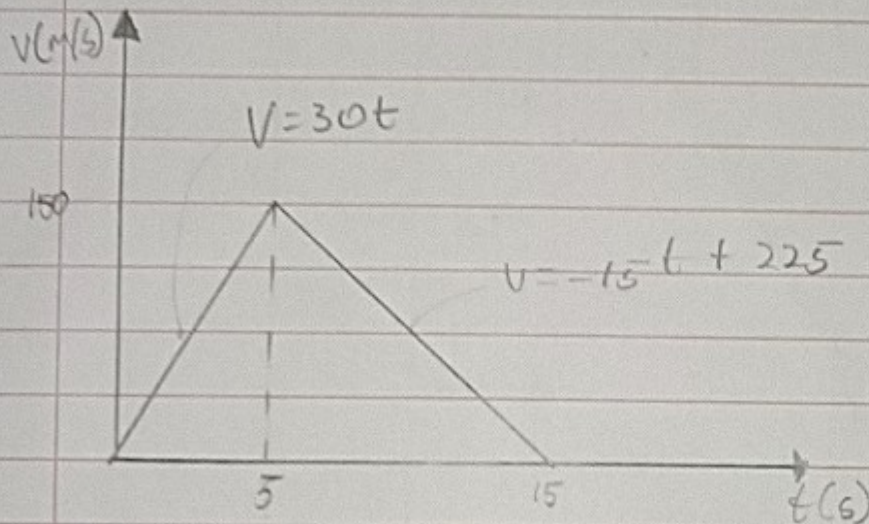




Q3 (F12-14)

Construct the  $s-t$  graph

$0 \leq t \leq 15s$ , find the total distance



Solution:

$$\int_{s_0}^s ds = \int_{t_0}^t v dt$$

$$0 \leq t \leq 5$$

$$v = 30t$$

$$\int_0^s ds = \int_0^t (30t) dt$$

$$s = 15t^2$$

$$\text{at } t = 5s, s = 15(5)^2 = 375m$$

$$\text{at } 5 \leq t \leq 15$$

$$v = -15t + 225$$

$$\int_{375}^s ds = \int_5^t (-15t + 225) dt$$

$$s - 375 = -15/2 t^2 + 225t \Big|_5^t$$

$$s - 375 = \frac{-15}{2} t^2 + 225t - \left( \frac{-15}{2} (5)^2 + 225(5) \right)$$

$$s - 375 = -\frac{15}{2} t^2 + 225t + \frac{15}{2} (5^2) - 225(5)$$

$$s - 375 = -\frac{15}{2} t^2 + 225t - 562.5$$

$$s = \frac{-15}{2} t^2 + 225t - 562.5$$

When  $t = 15s$ ,

$$s = \frac{-15}{2} (15)^2 + 225(15) - 562.5$$

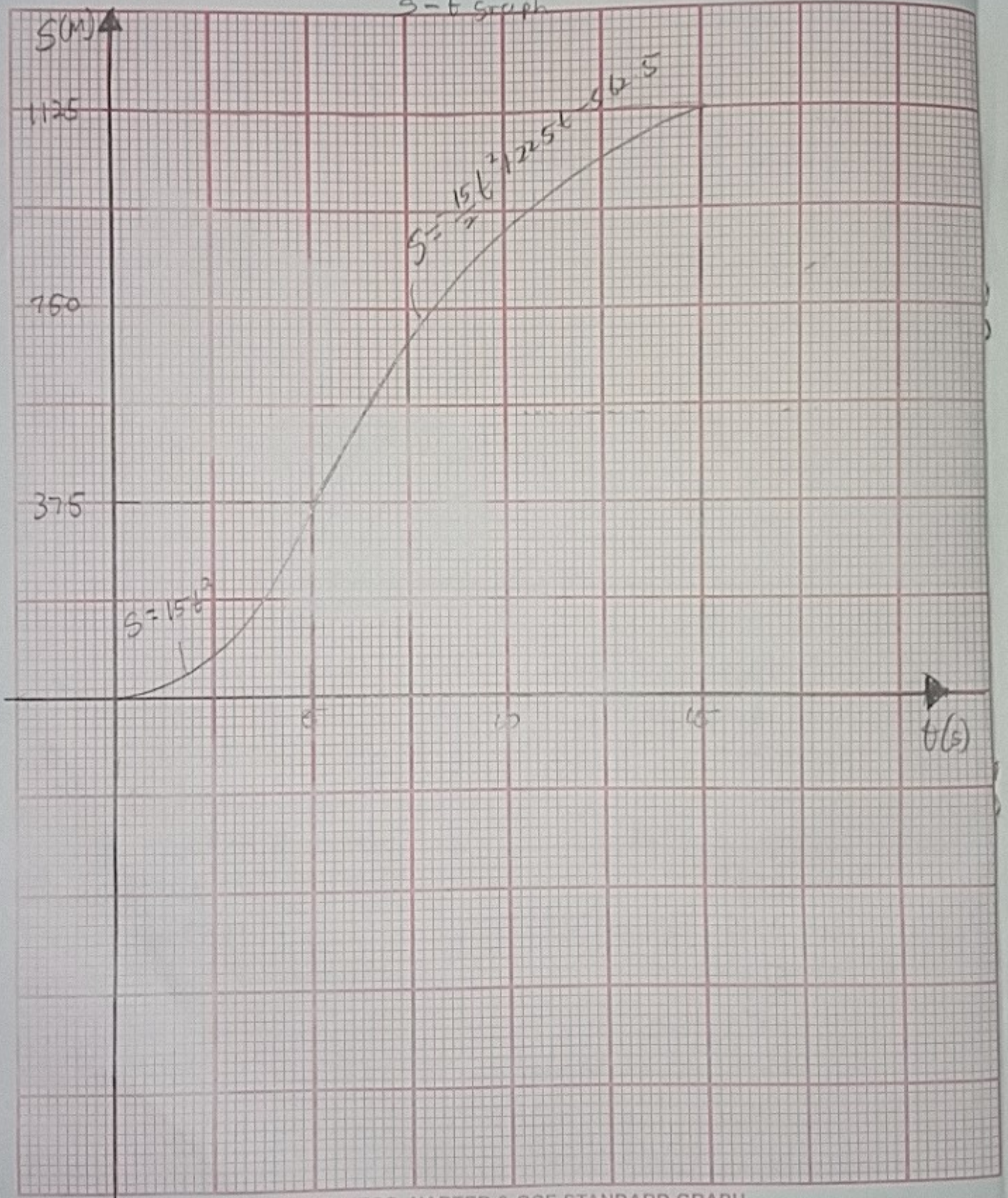
$$s = 1125m$$



Scale X axis.....

Scale Y axis.....

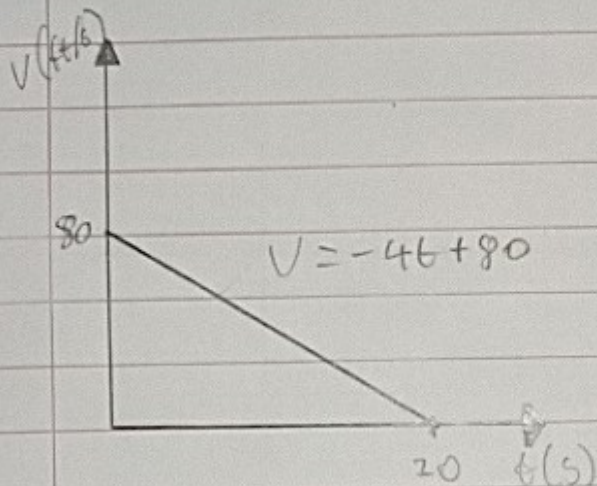
s - t graph





Q4 (F12-10)

Construct the  $s-t$  and the  $a-t$  graphs  
take  $s=0$ , when  $t=0$



$a-t$

$$a = dv/dt$$

$$V = -4t + 80, t = 20$$

$$a = -4 \text{ m/s}^2$$

$s-t$

$$v = ds/dt$$

$$\int_{s_0}^s ds = \int_{t_0}^t v dt$$

$$s = \int (-4t + 80) dt$$

$$s = -2t^2 + 80t - (-2(0)^2 + 80(0))$$

$$s = -2t^2 + 80t$$

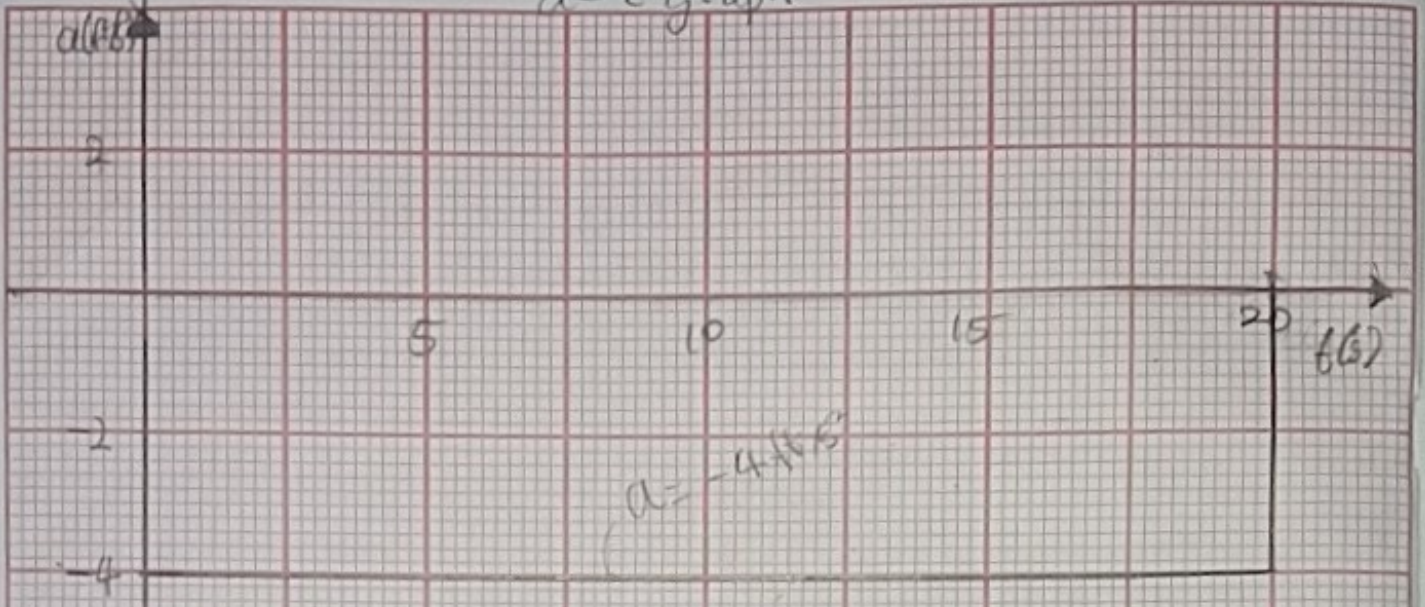
$$\text{When } t = 20\text{s}$$

$$s = -2(20)^2 + 80(20) = 800 \text{ ft}$$

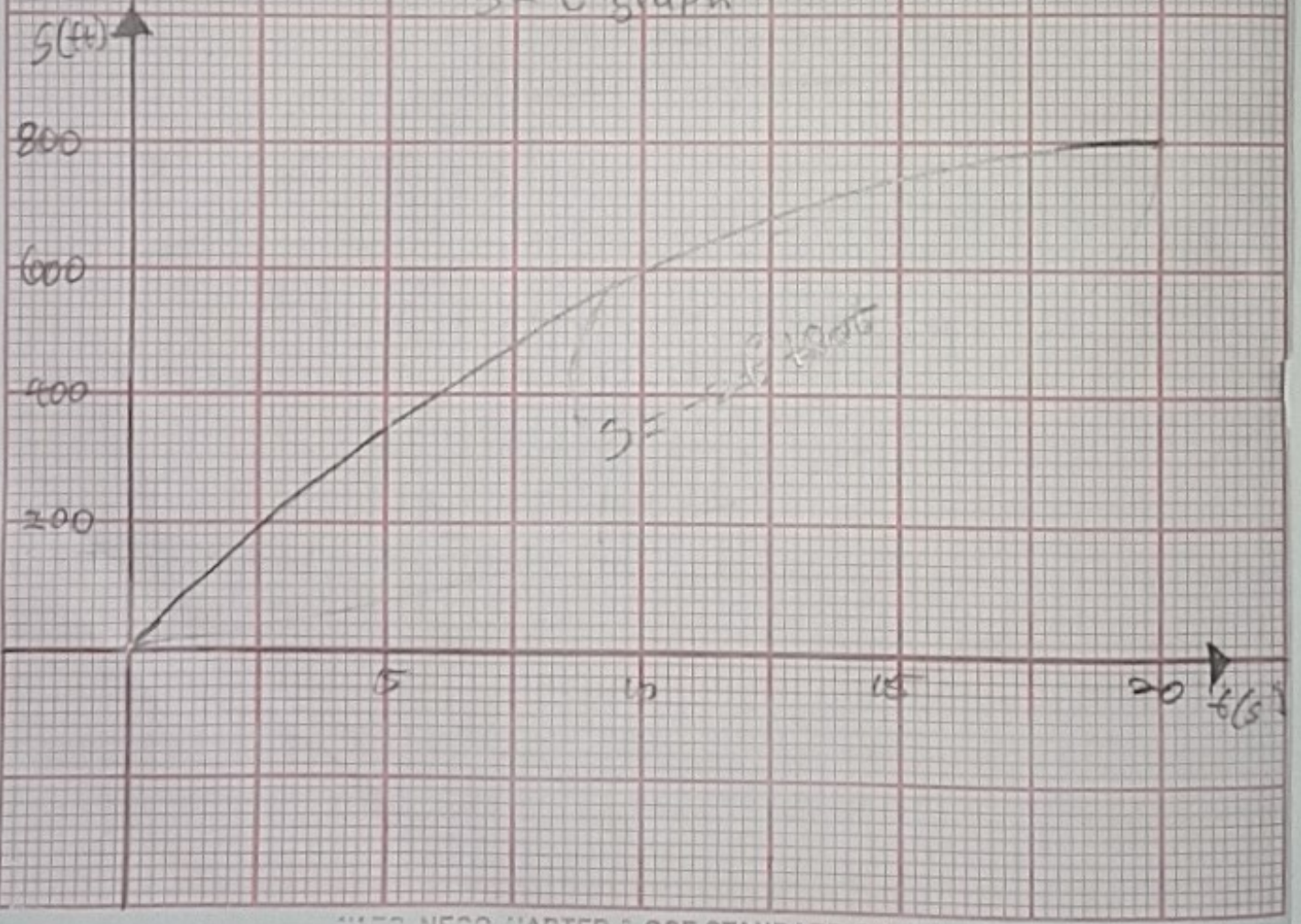


Scale X axis..... Scale Y axis.....

a-t graph



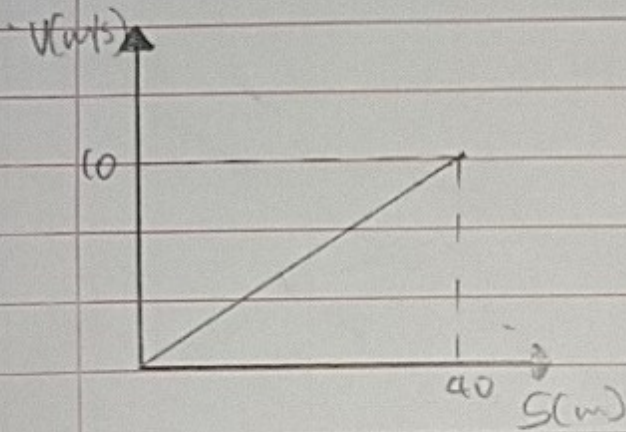
S-t graph





Q5 (F12-11)

Construct the  $a-s$  graph



Solution

$$v dv = a ds$$

$$v = 0.25s$$

$$dv/ds = 0.25$$

$$dv = 0.25 ds$$

$$a ds = v dv$$

$$a ds = (0.25s) \cdot (0.25 ds)$$

$$a = 0.25s \cdot 0.25$$

$$a = 0.0625s$$

$$\text{at } s=40, a = 0.0625(40)$$

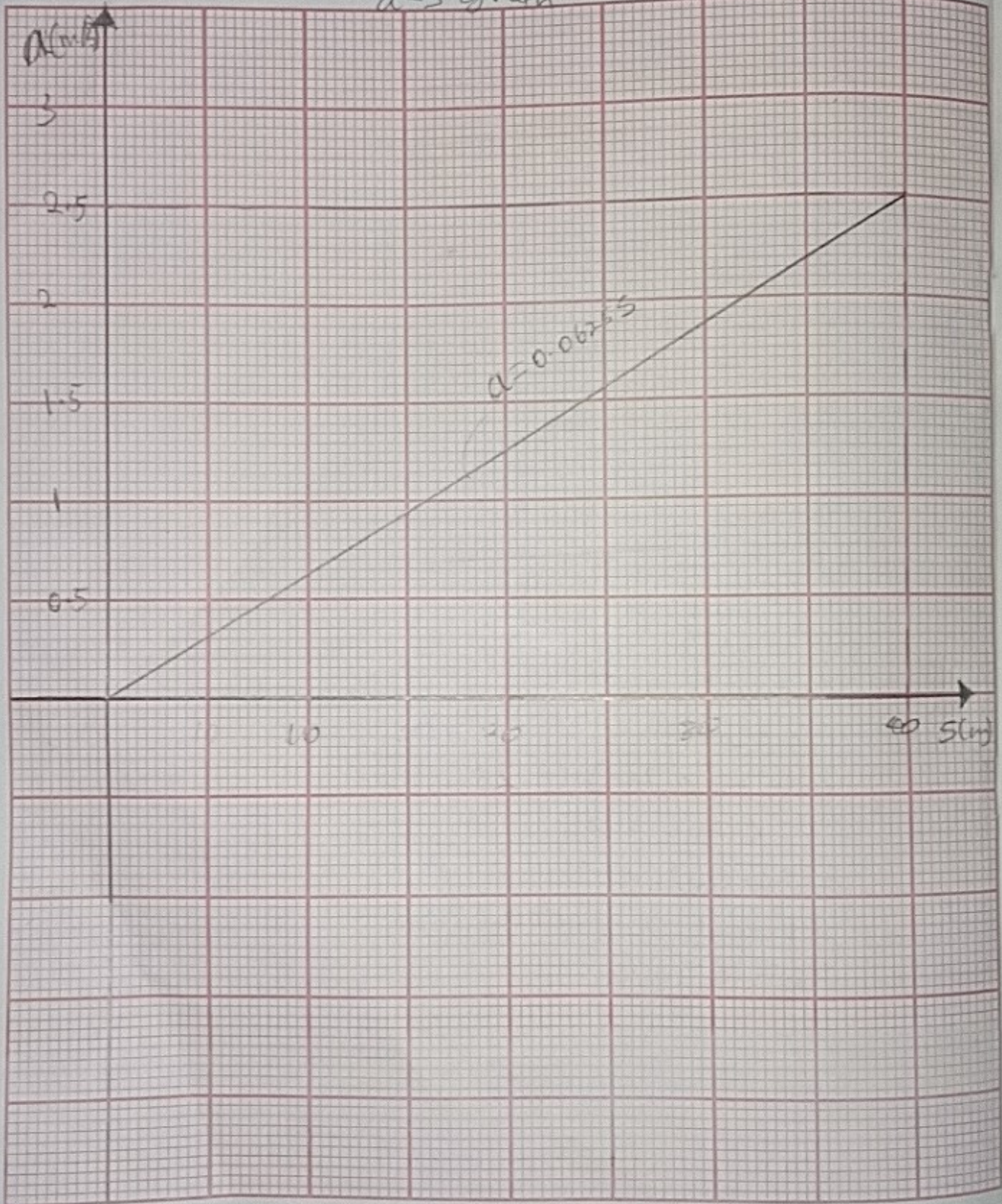
$$a = 2.5 \text{ m/s}^2$$



Scale X axis.....

Scale Y axis.....

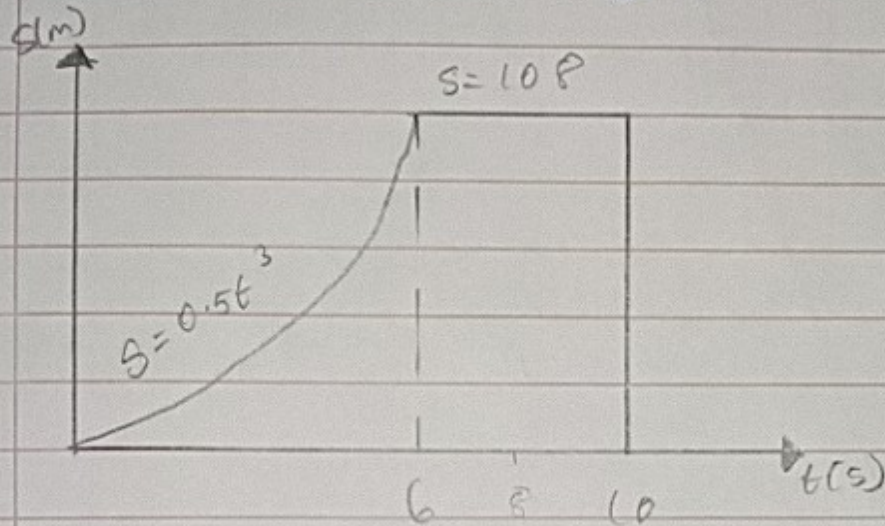
$a-s$  graph





Q6 (F12-9)

Construct the  $v-t$  graph



Solution

$v-t$

$$0 \leq t \leq 6$$

$$v = \frac{ds}{dt}, \quad s = 0.5t^3$$

$$v = 1.5t^2$$

at  $t = 6s$

$$v = 1.5(6)^2 = 54$$

$$6 \leq t \leq 10,$$

$$v = 0$$



